

# Efficient palette-based decomposition and recoloring of images via RGBXY-space geometry

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**Jose Echevarria**      Adobe Research

**Yotam Gingold**      George Mason University



# Motivation: Layers Organize Images





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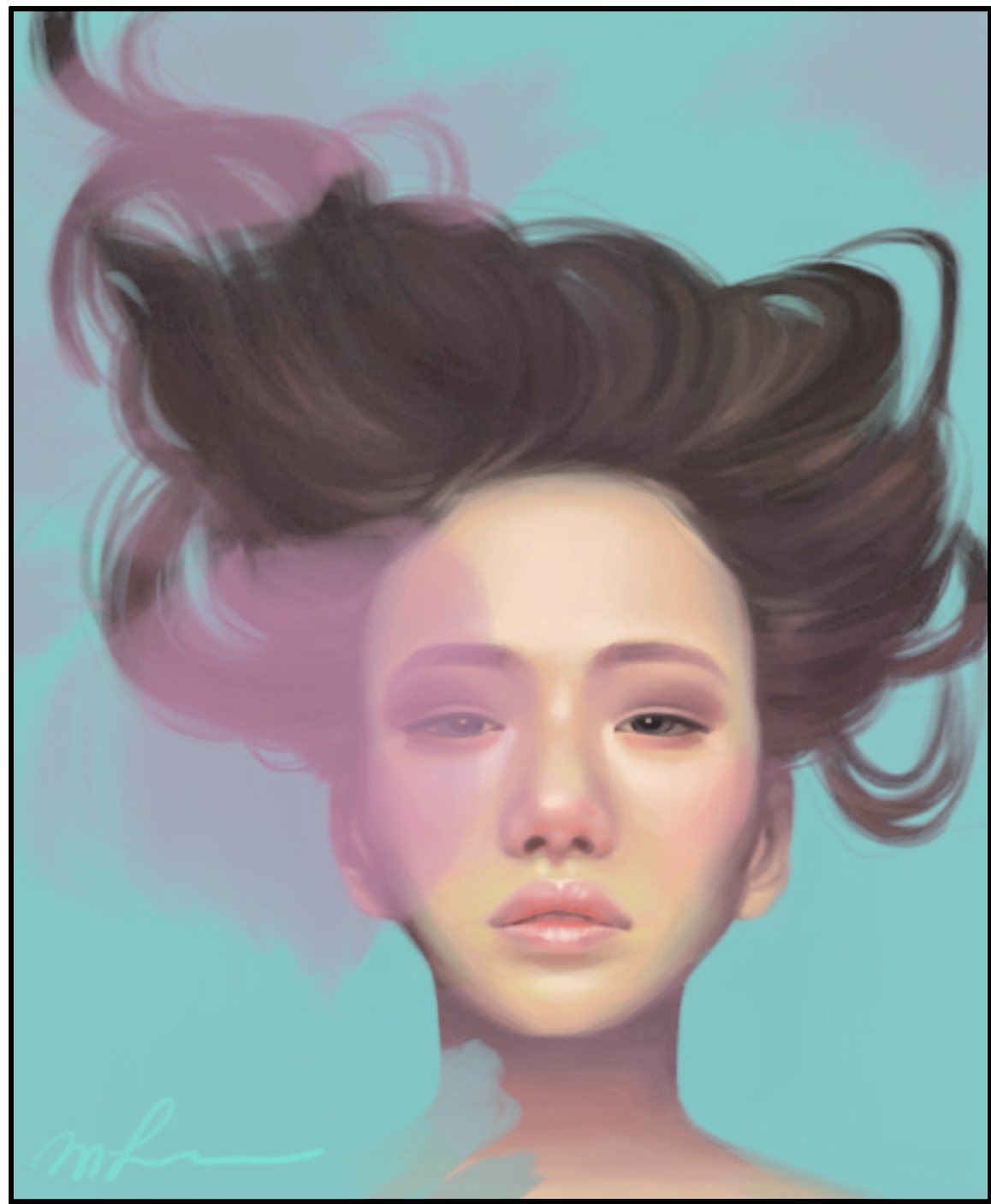


# Motivation: Layers Organize Images





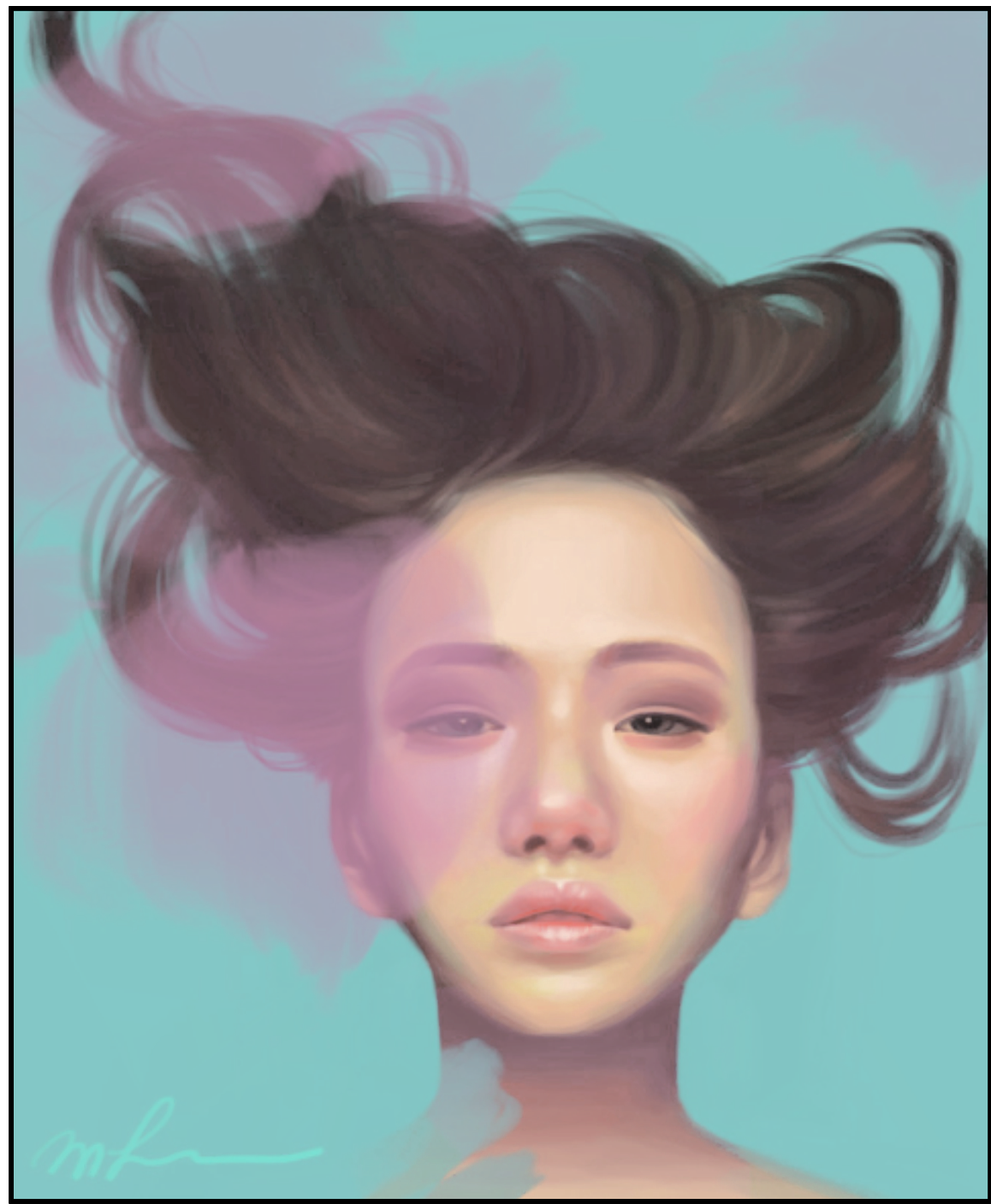
Input



Goal

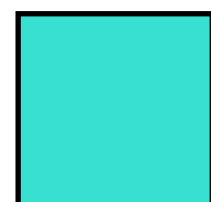
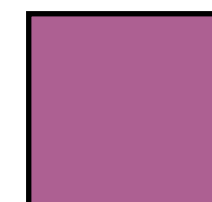
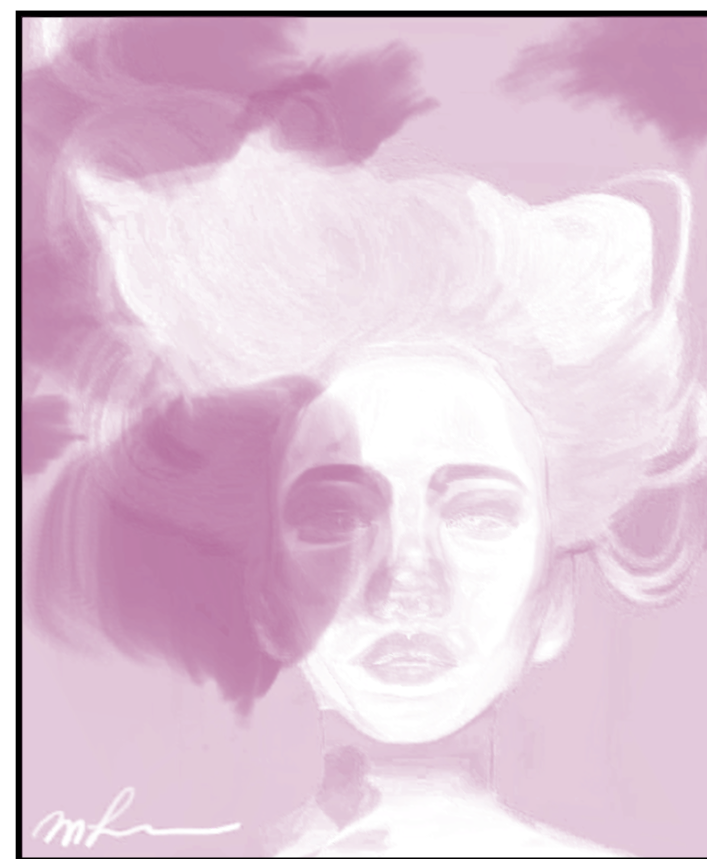
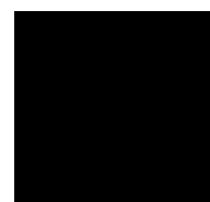
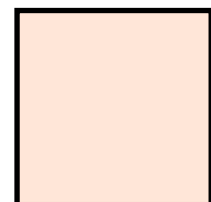
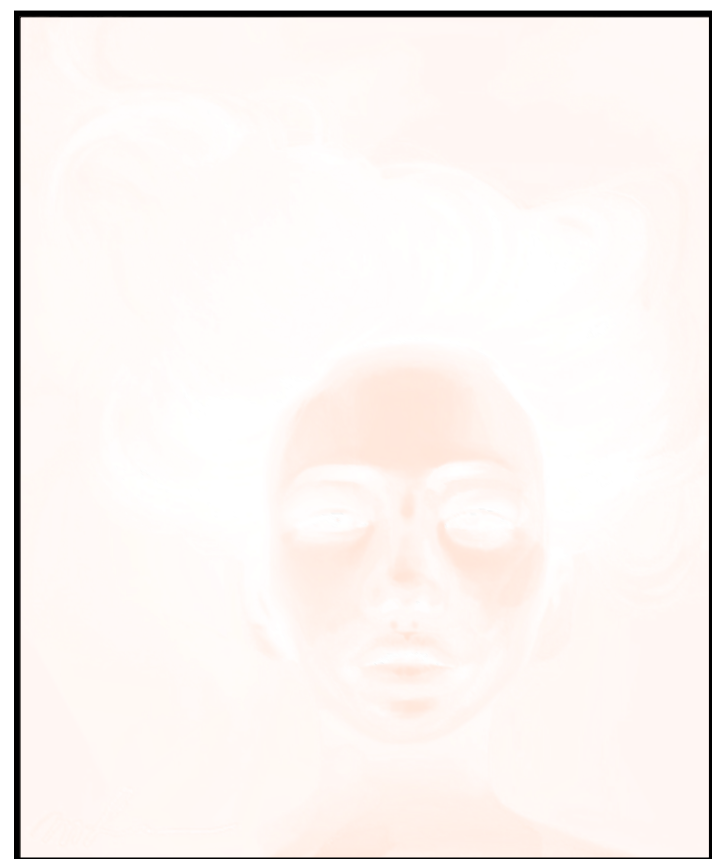


Input



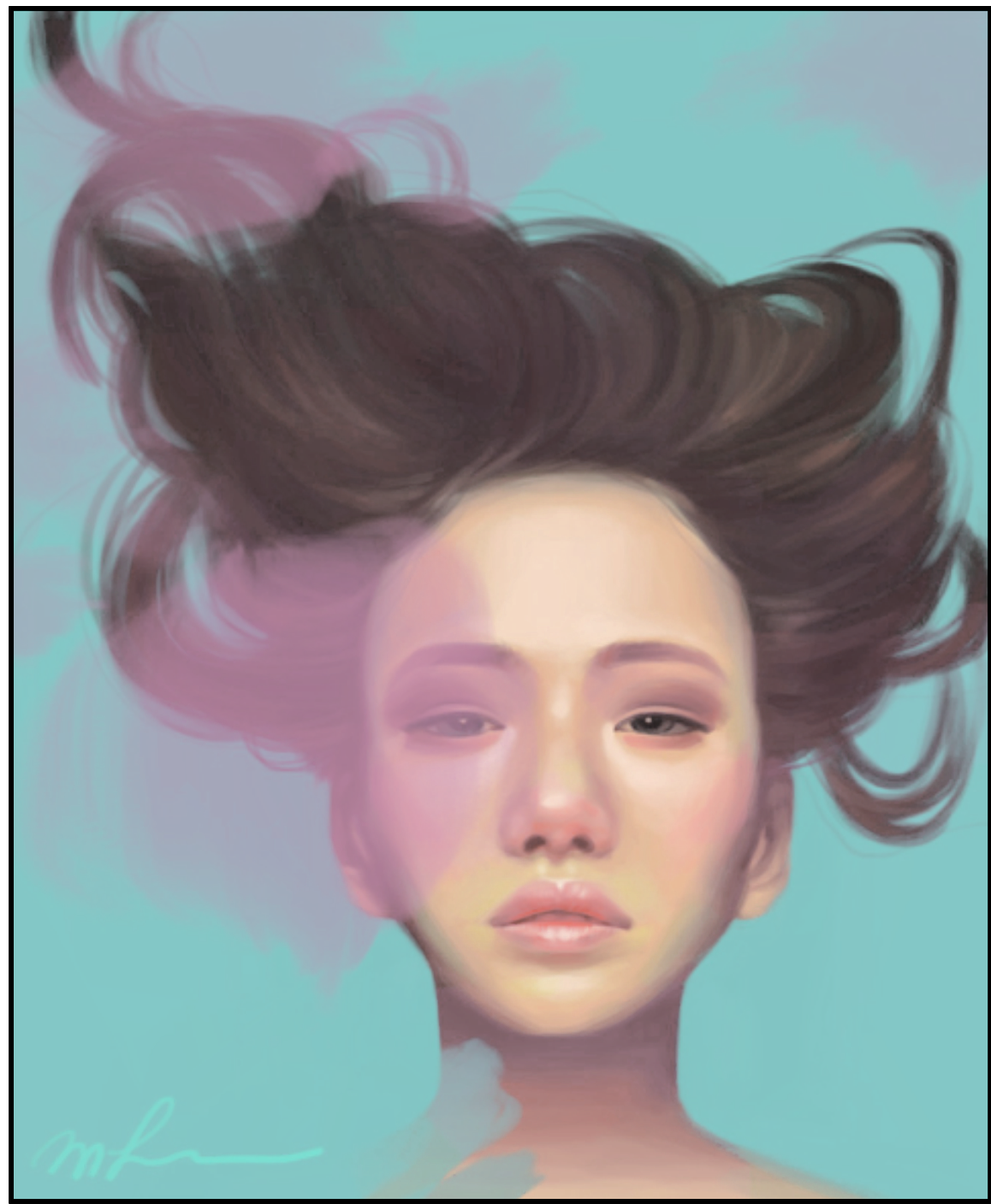
Goal

Layers



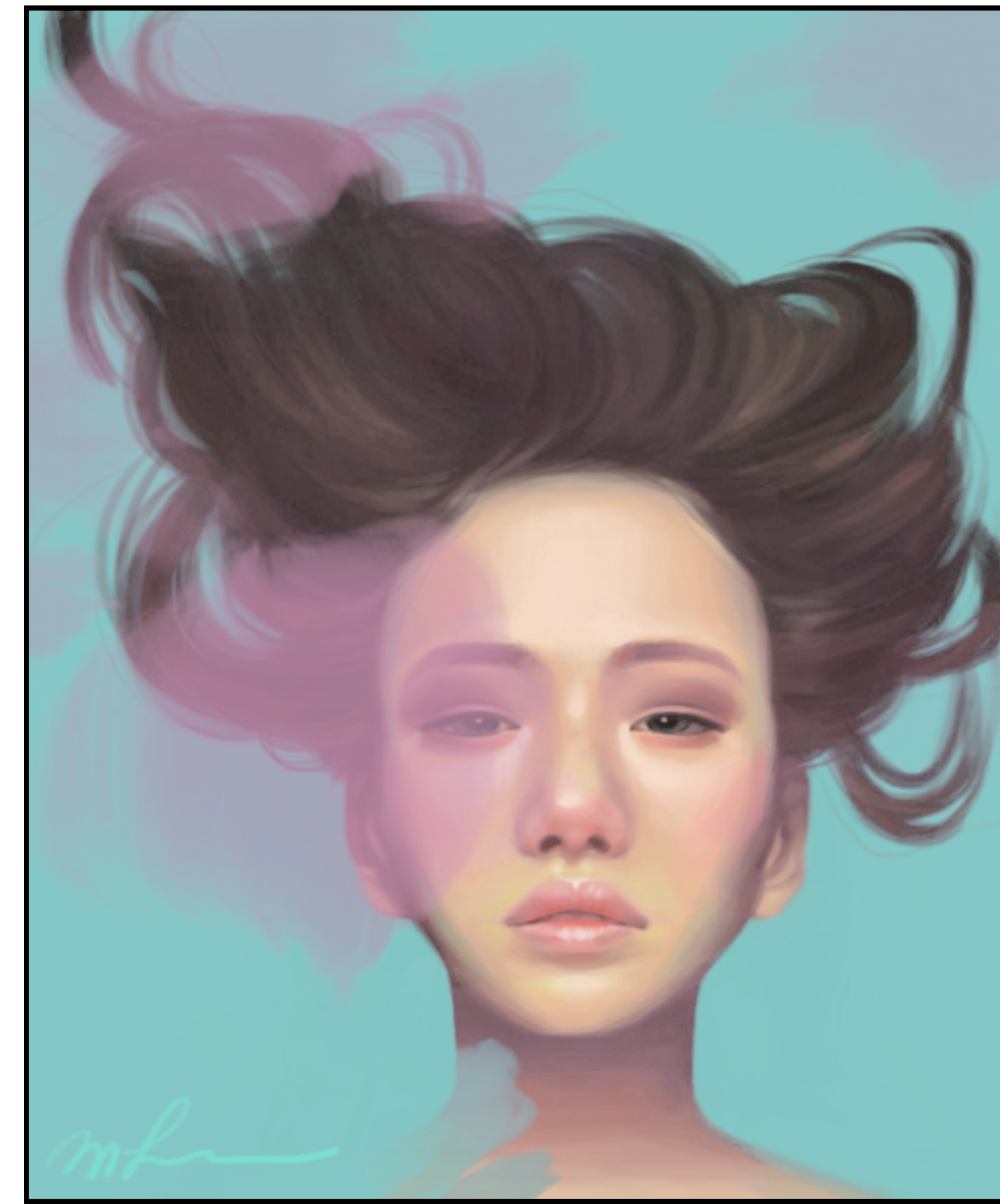


Input

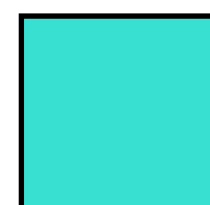
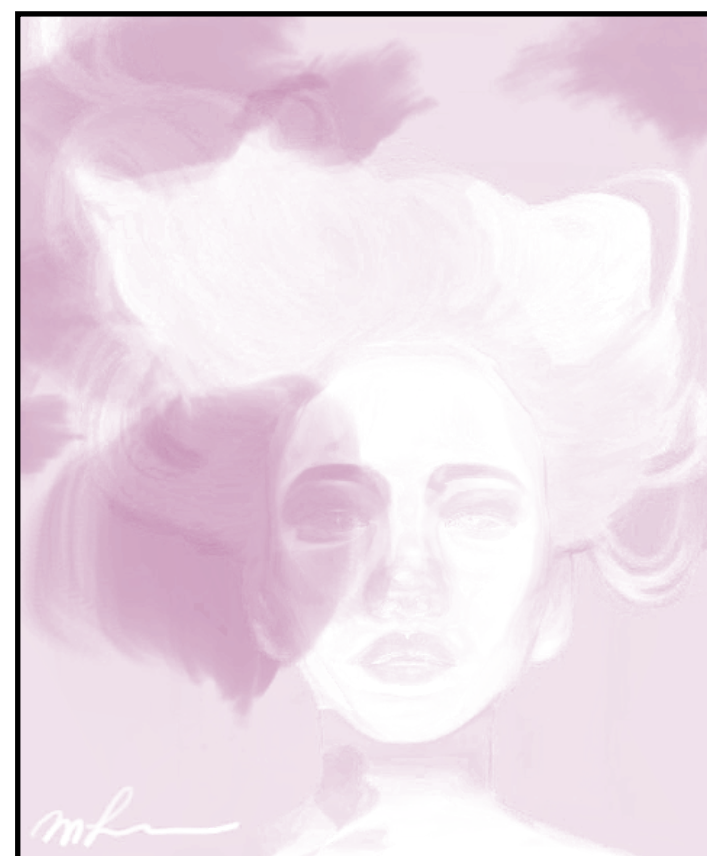
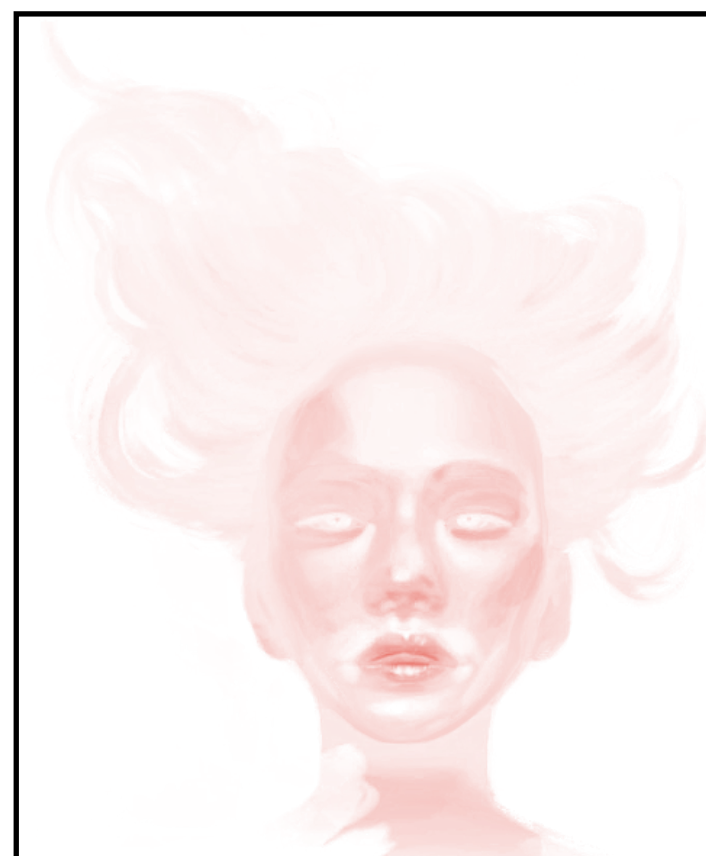
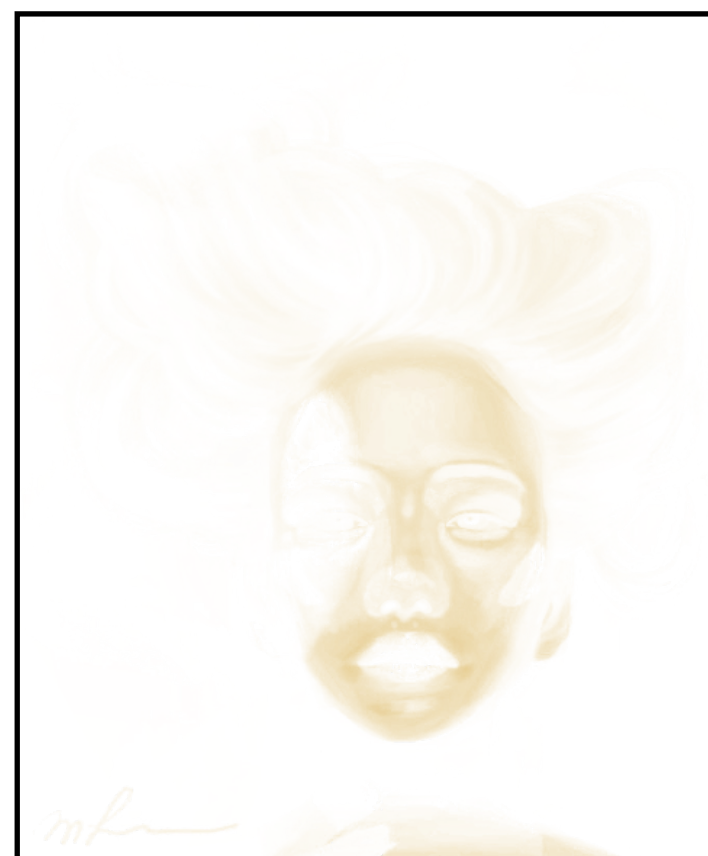
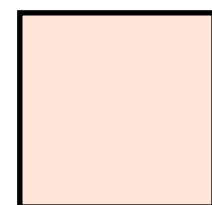
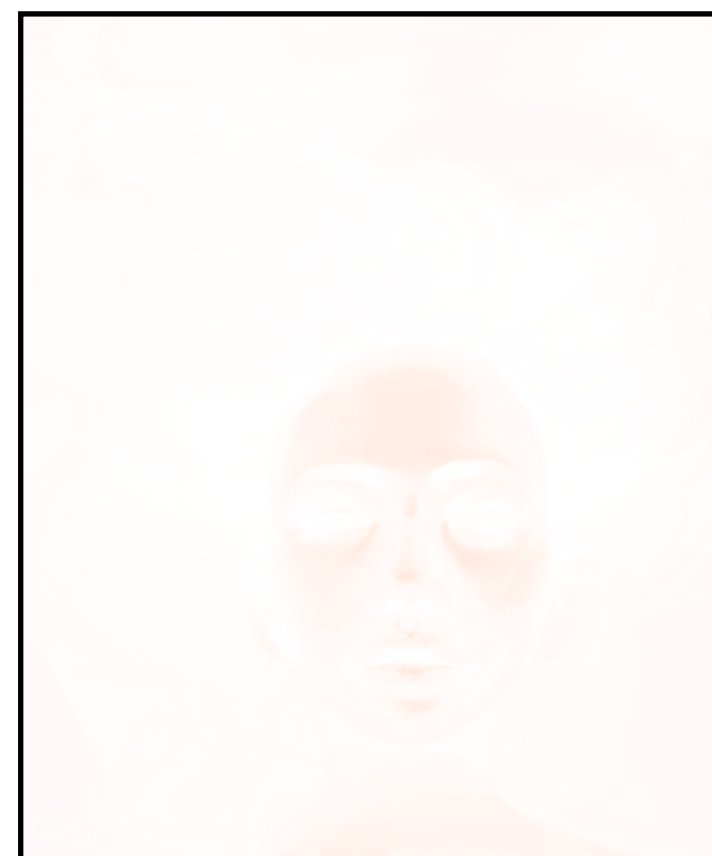


Goal

Reconstruction

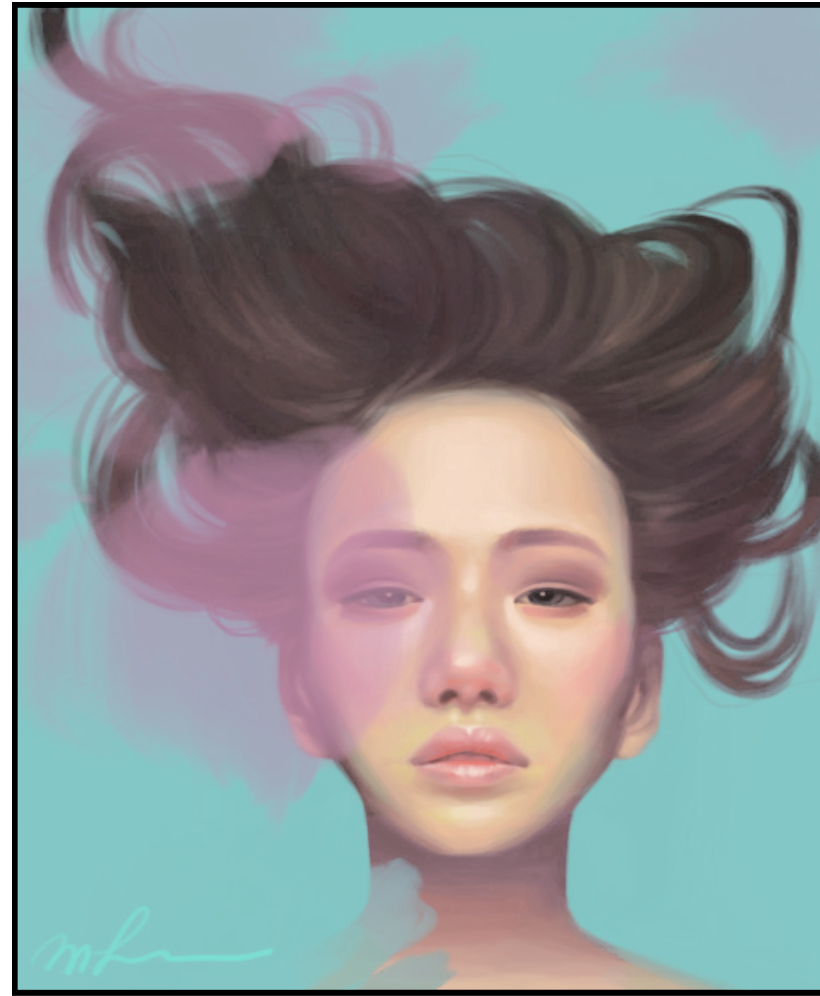


Layers





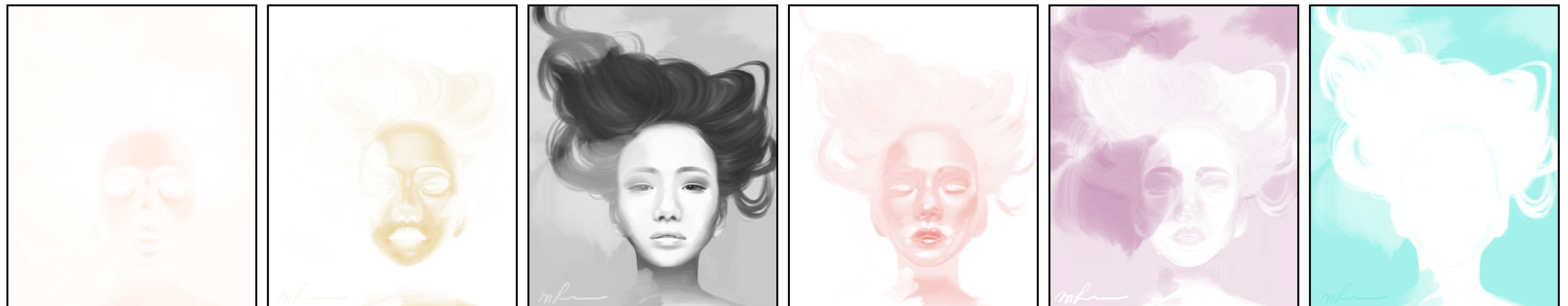
# Subproblems



## 1. Palette extraction



## 2. Palette-based layer decomposition

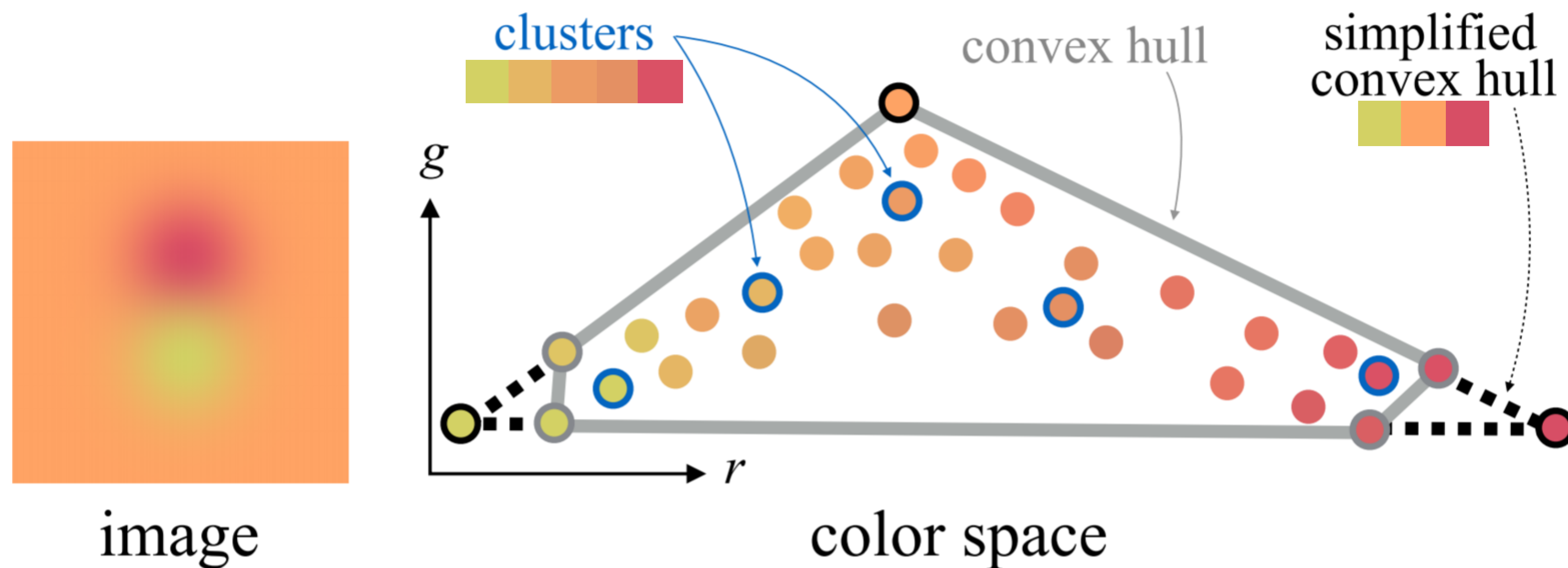




# Related Work

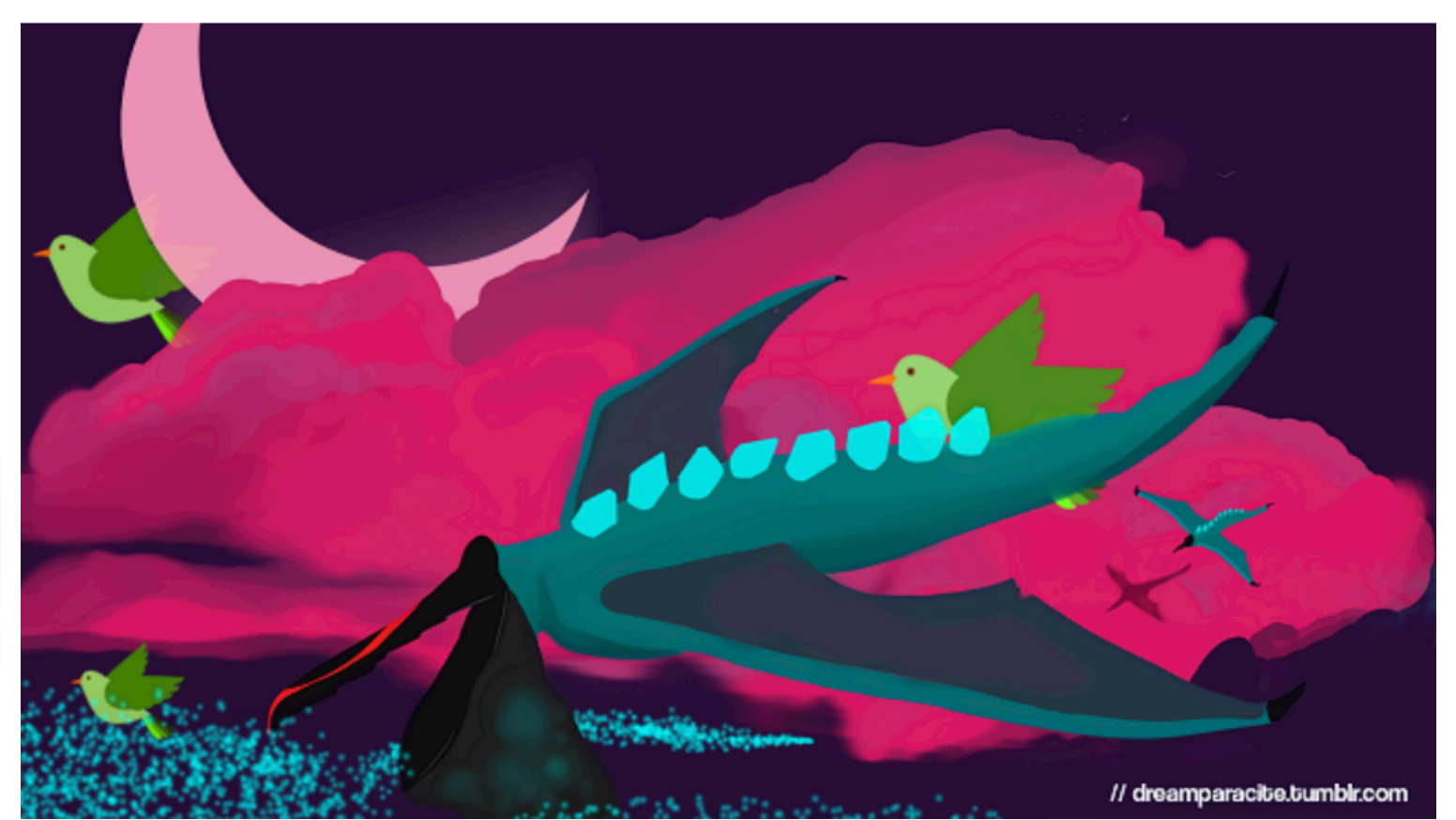
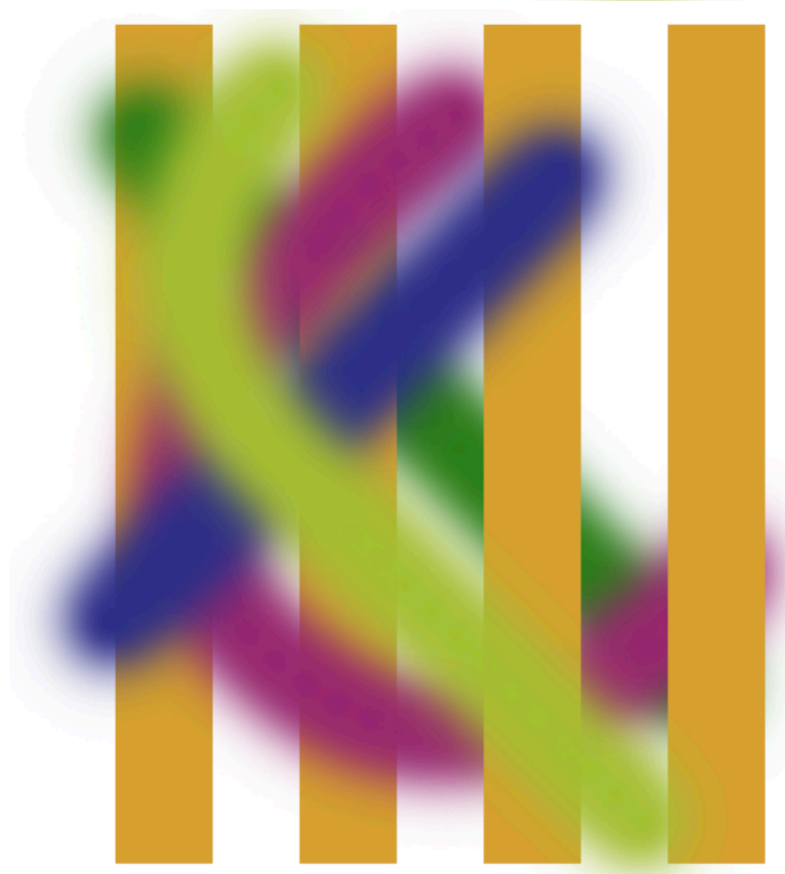
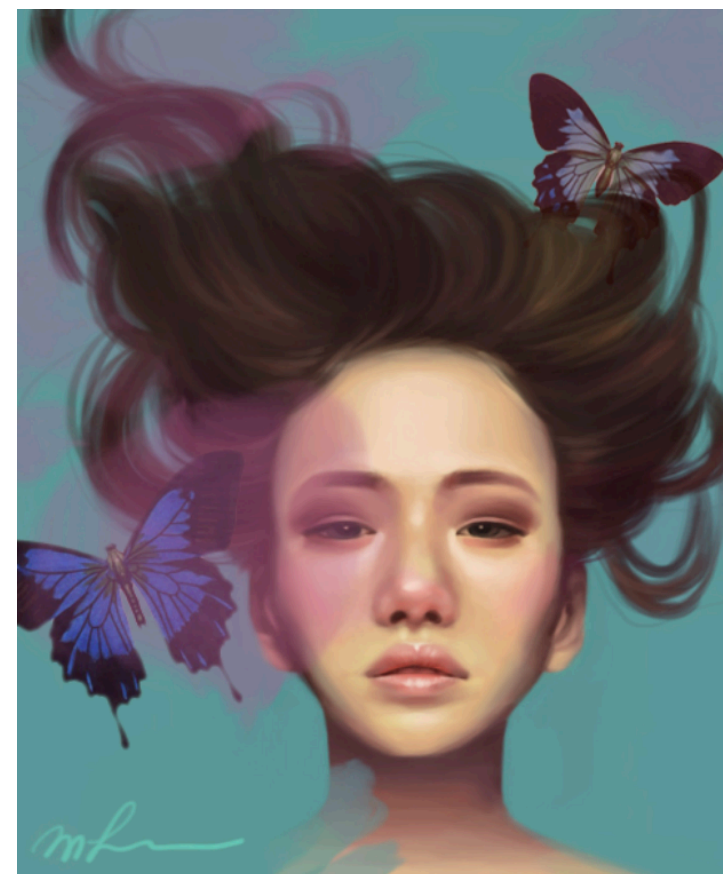
- Palette extraction for image editing

- Shapira et al. [2009]
- O'Donovan et al. [2011]
- Lin et al. [2013]
- Gerstner et al. [2013]
- Chang et al. [2015]
- Tan et al. [2016]



# Related Work

- Order-dependent translucent layers
  - Richardt et al. [2014]
  - Tan et al. [2015]
  - Tan et al. [2016]

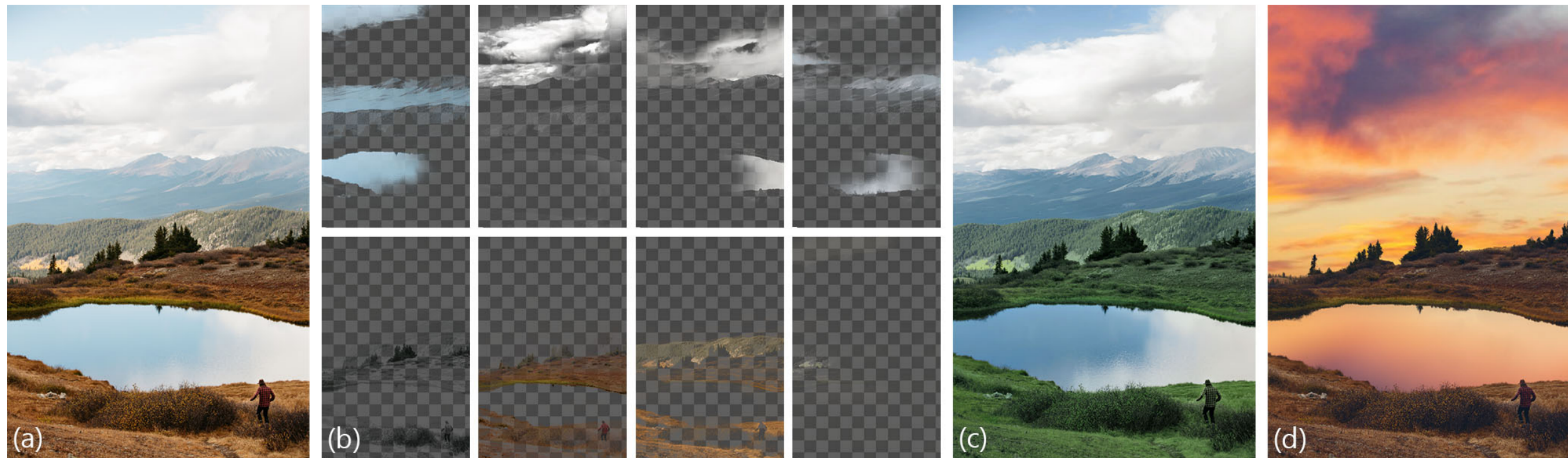


*Decomposing Images into Layers via RGB-space Geometry* [Tan et al. 2016]



# Related Work

- Order-independent additive-mixing layers
  - Lin et al. [2017]; Zhang et al. [2017], Aksoy et al. [2017].

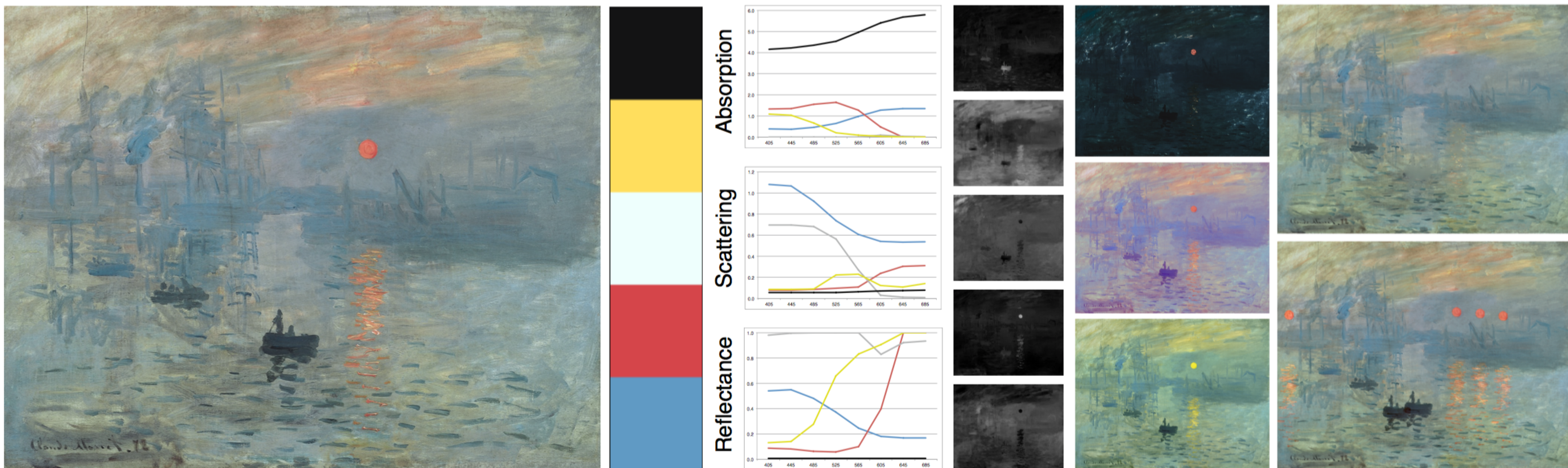


*Unmixing-Based Soft Color Segmentation for Image Manipulation [Aksoy et al. 2017]*



# Related Work

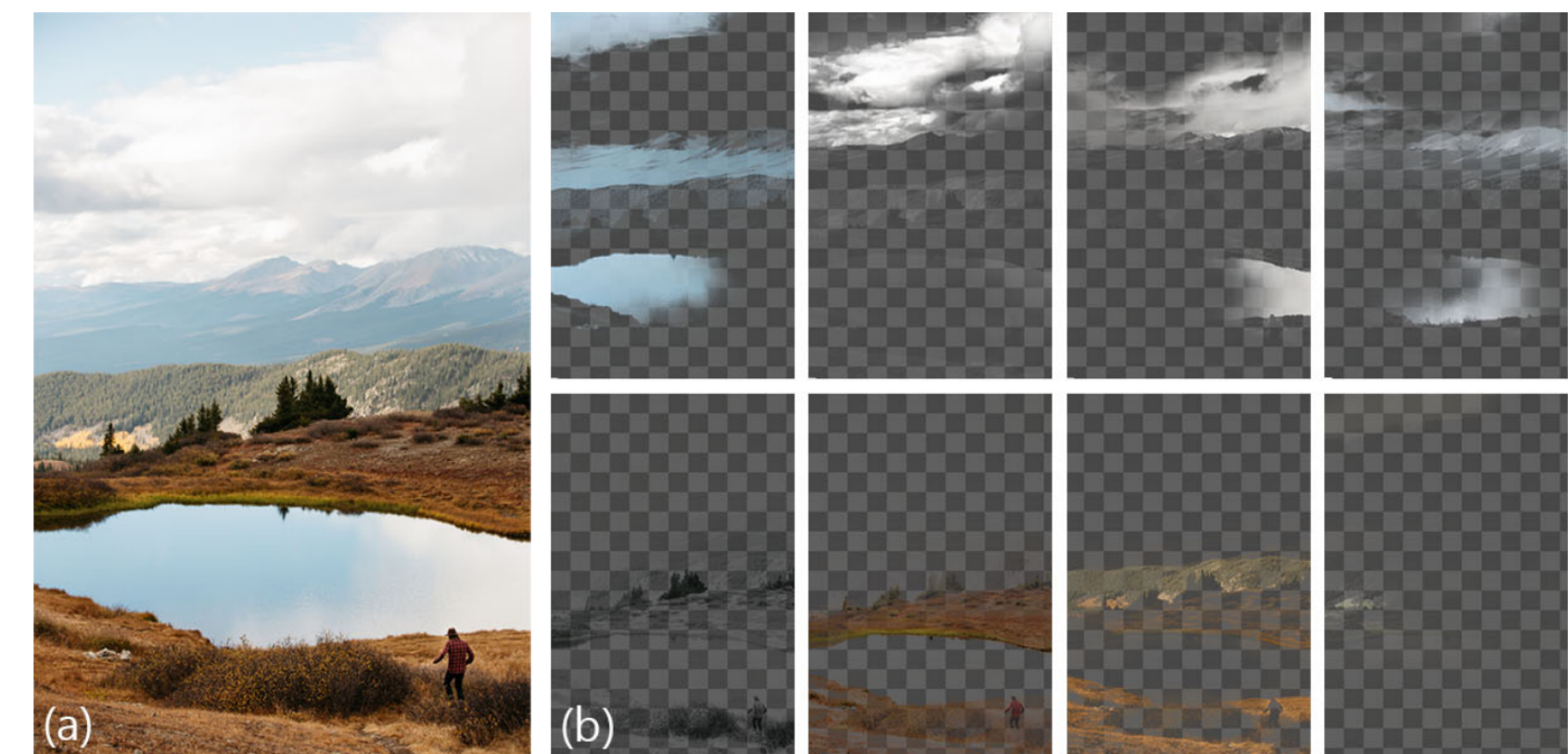
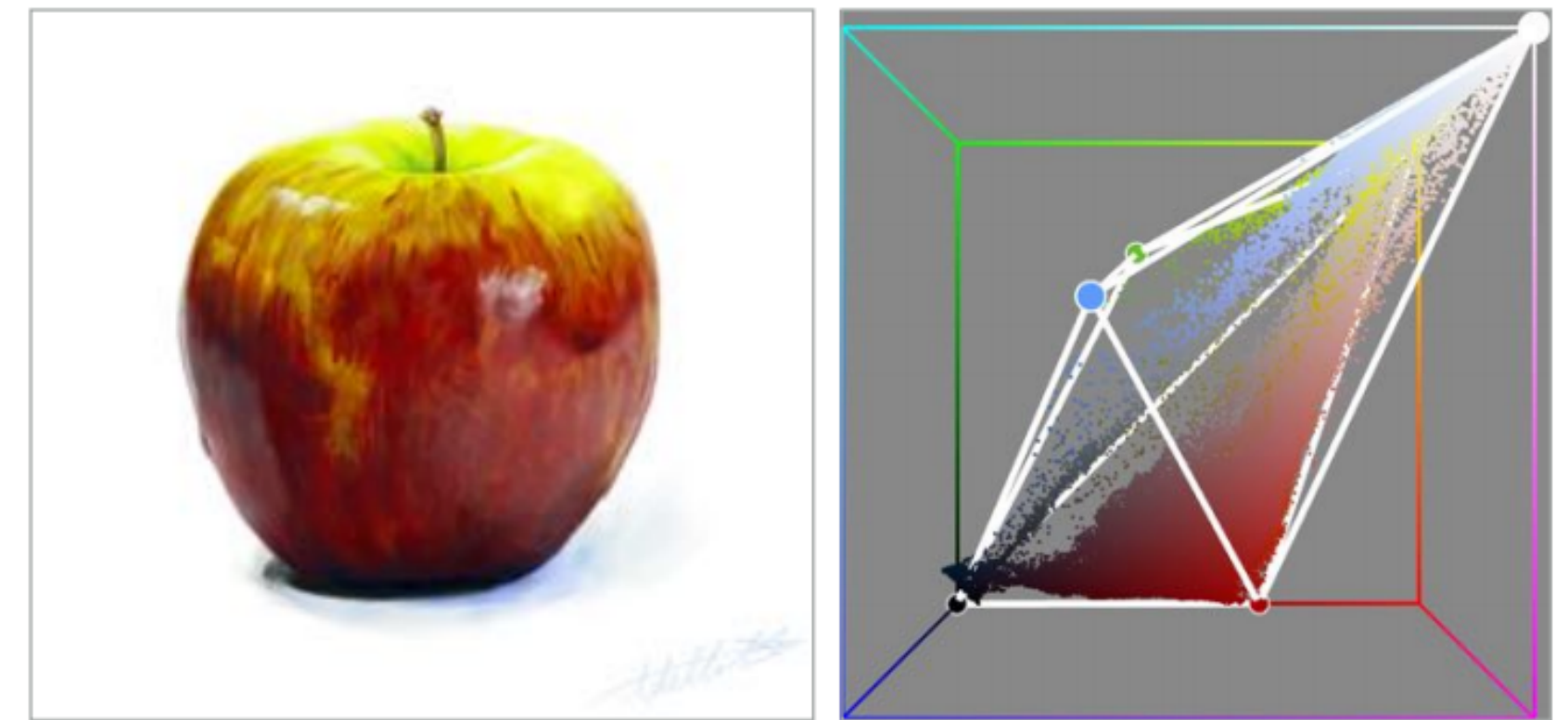
- Physically-based layers
  - Abed et al. [2014]; Tan et al. [2015]; Aharoni-Mack et al. [2017]; Tan et al. [2018].



*Pigmento: Pigment-Based Image Analysis and Editing* [Tan et al. 2018]

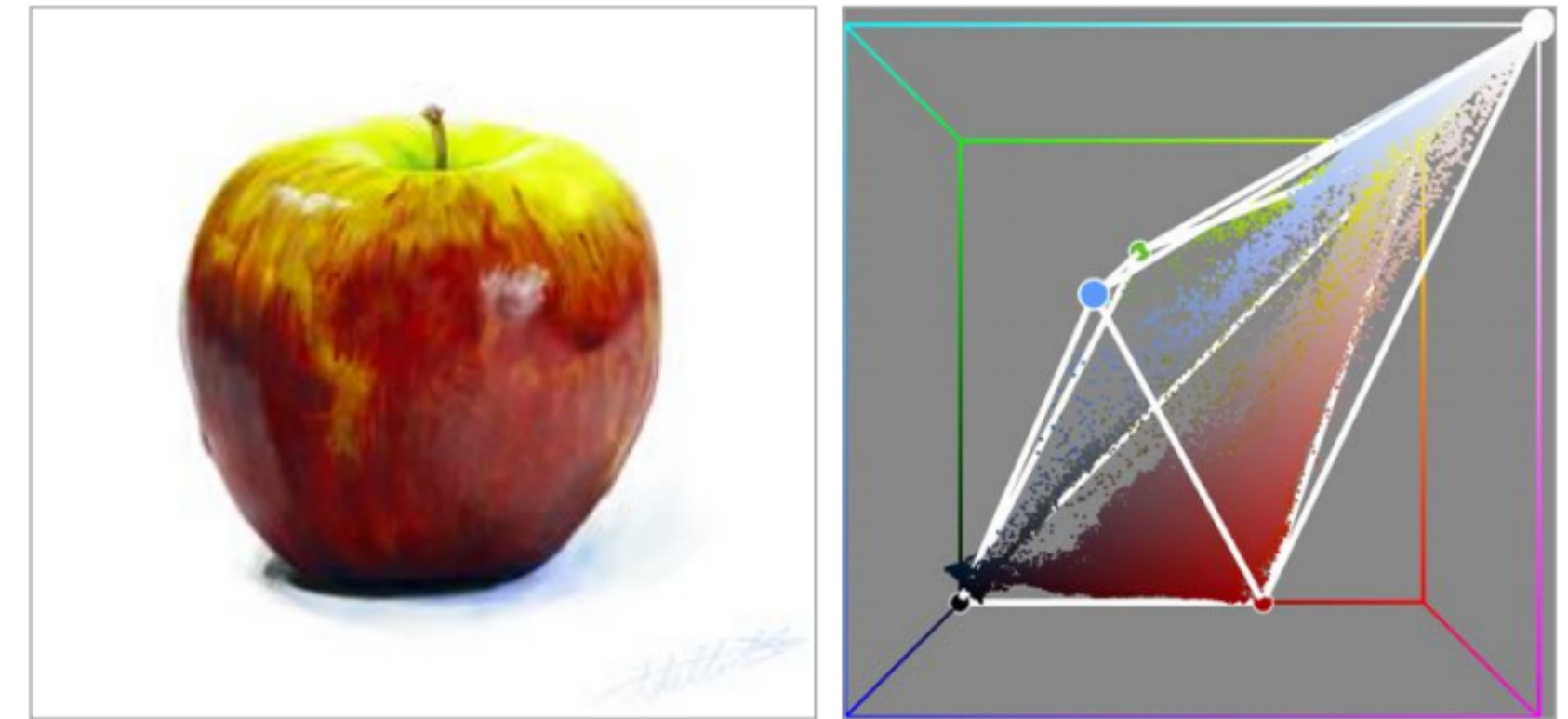


# Our approach



# Our approach

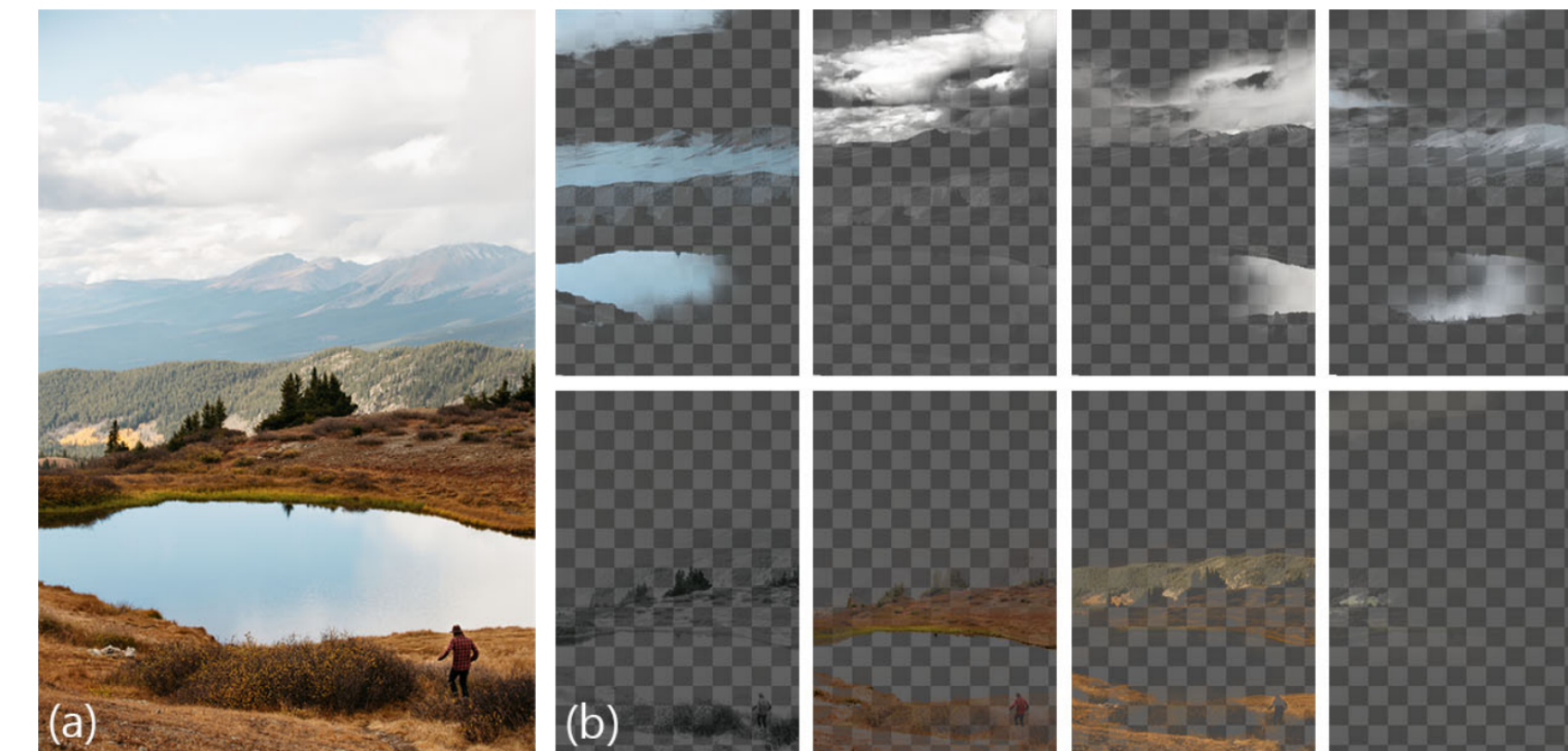
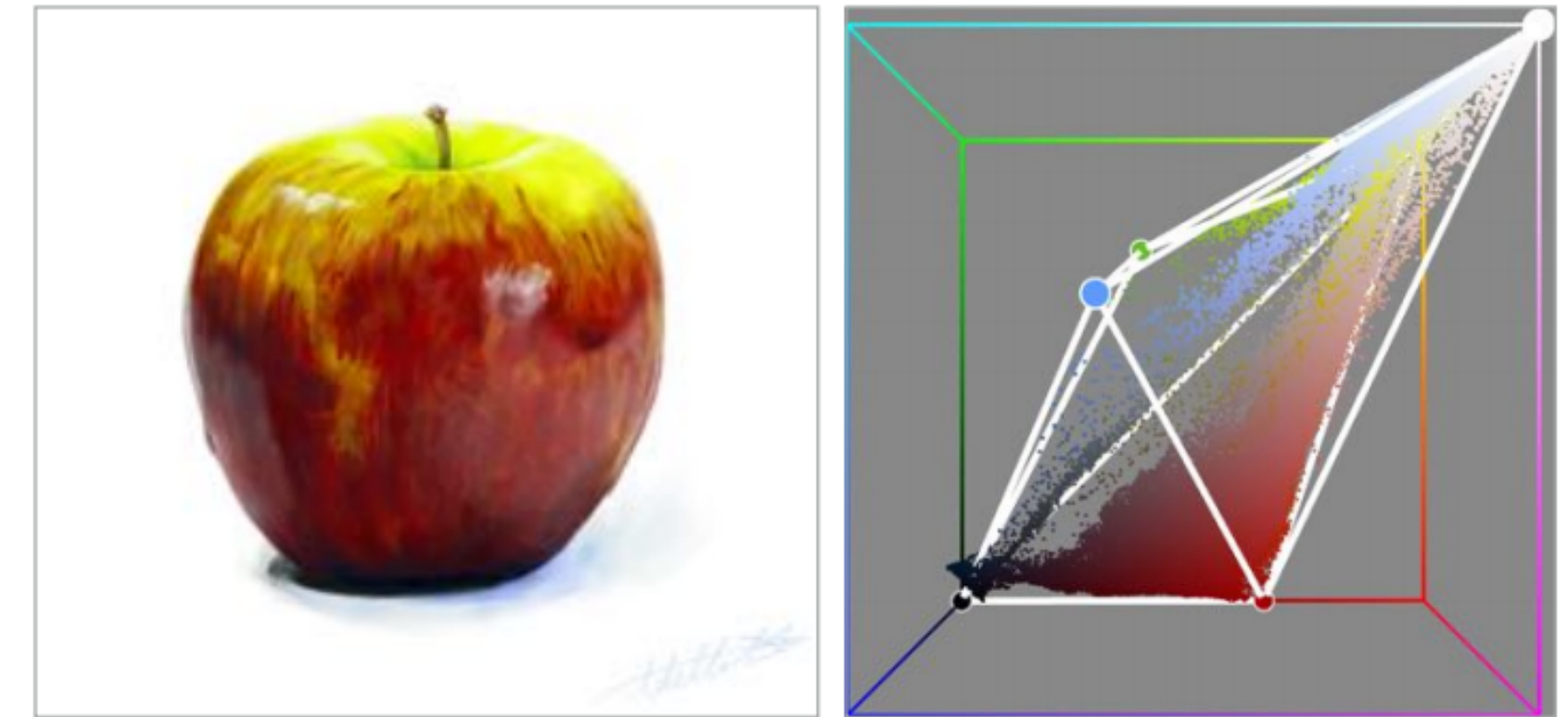
- Geometry-based convex palettes





# Our approach

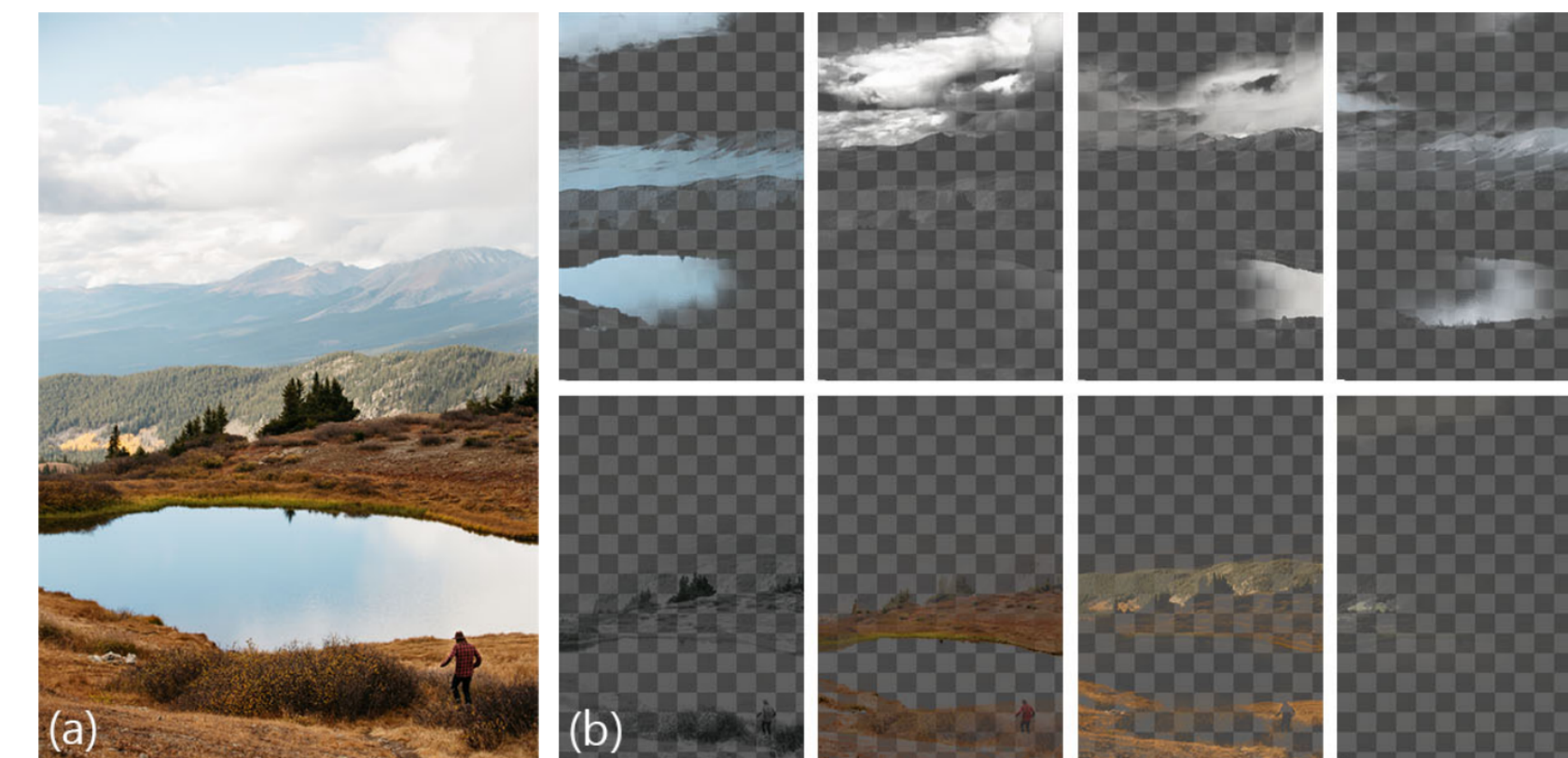
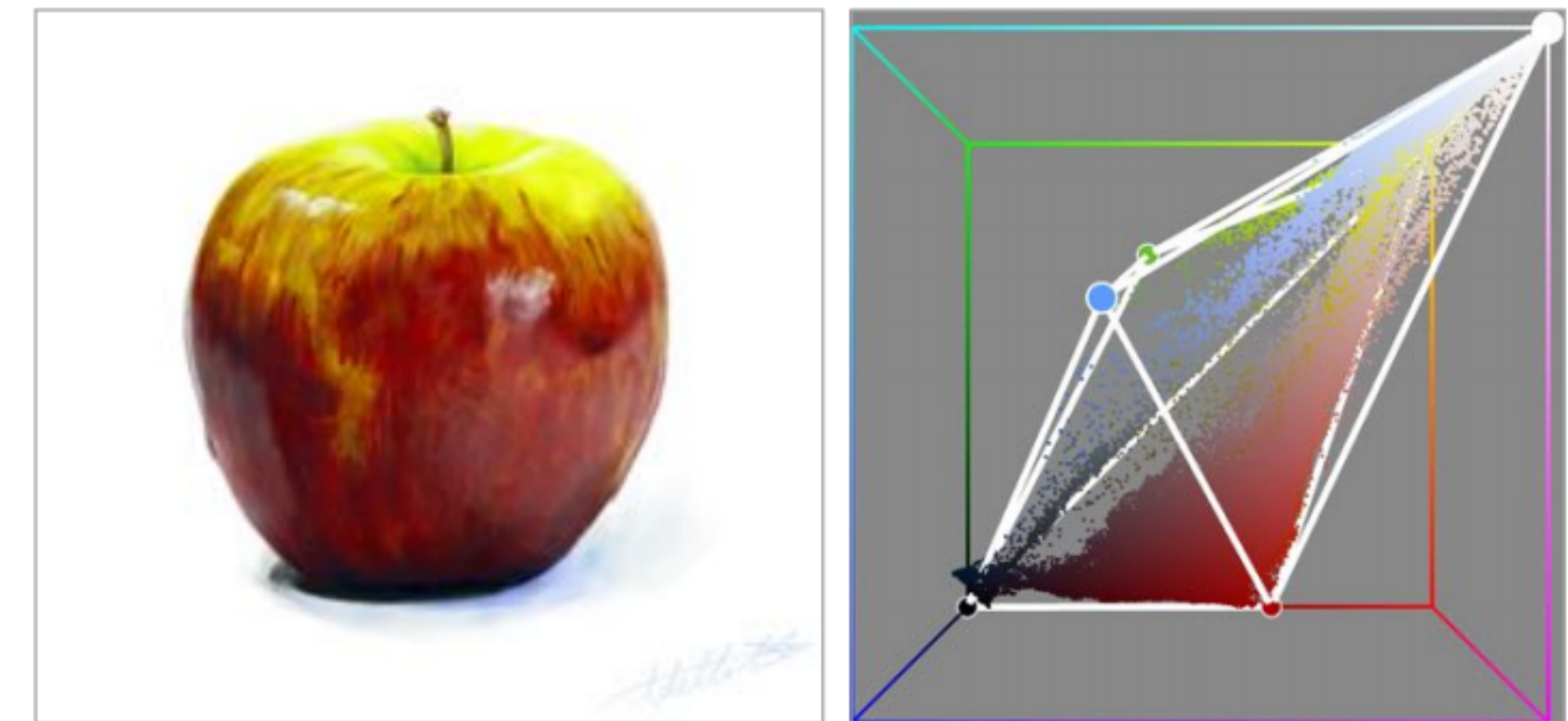
- Geometry-based convex palettes
  - Simpler





# Our approach

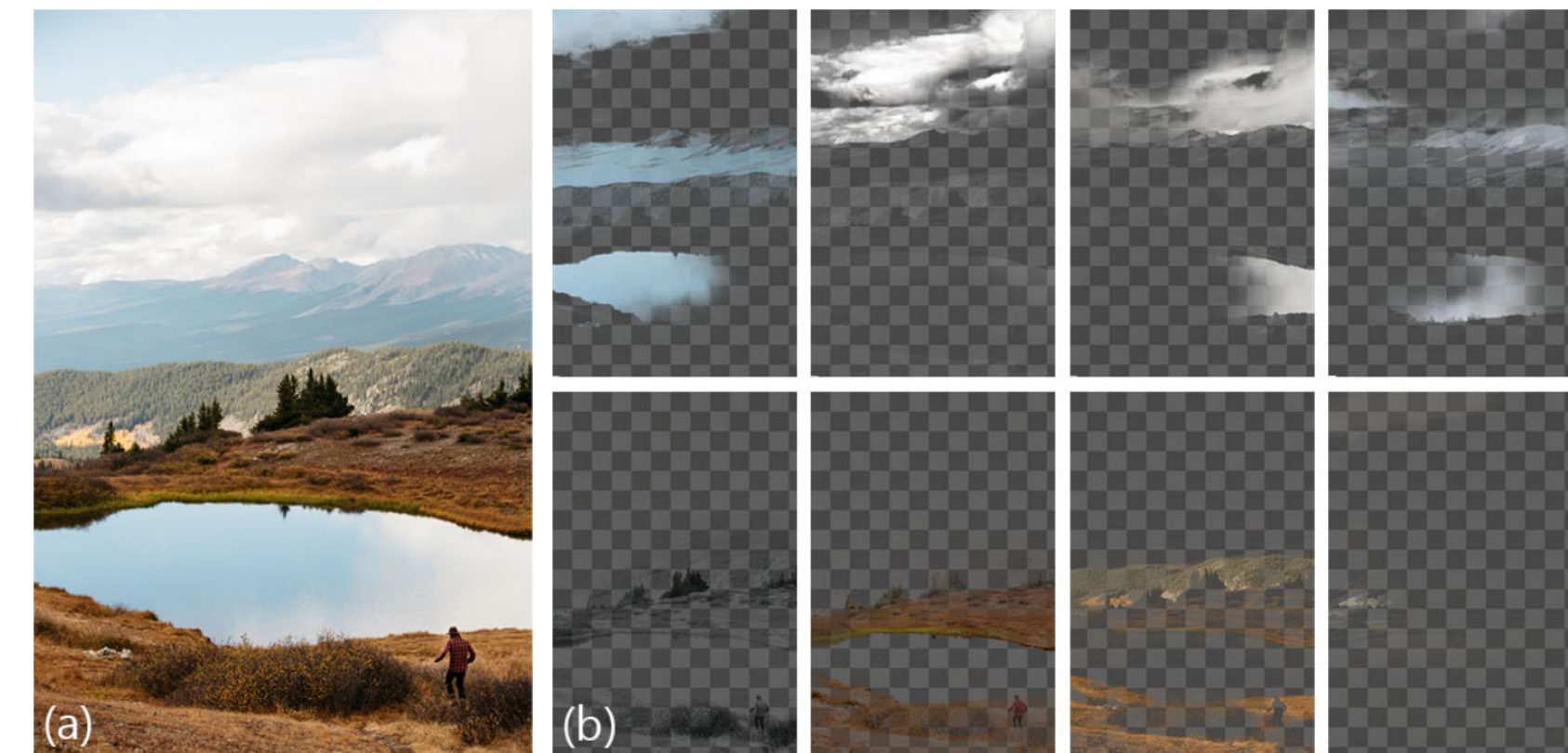
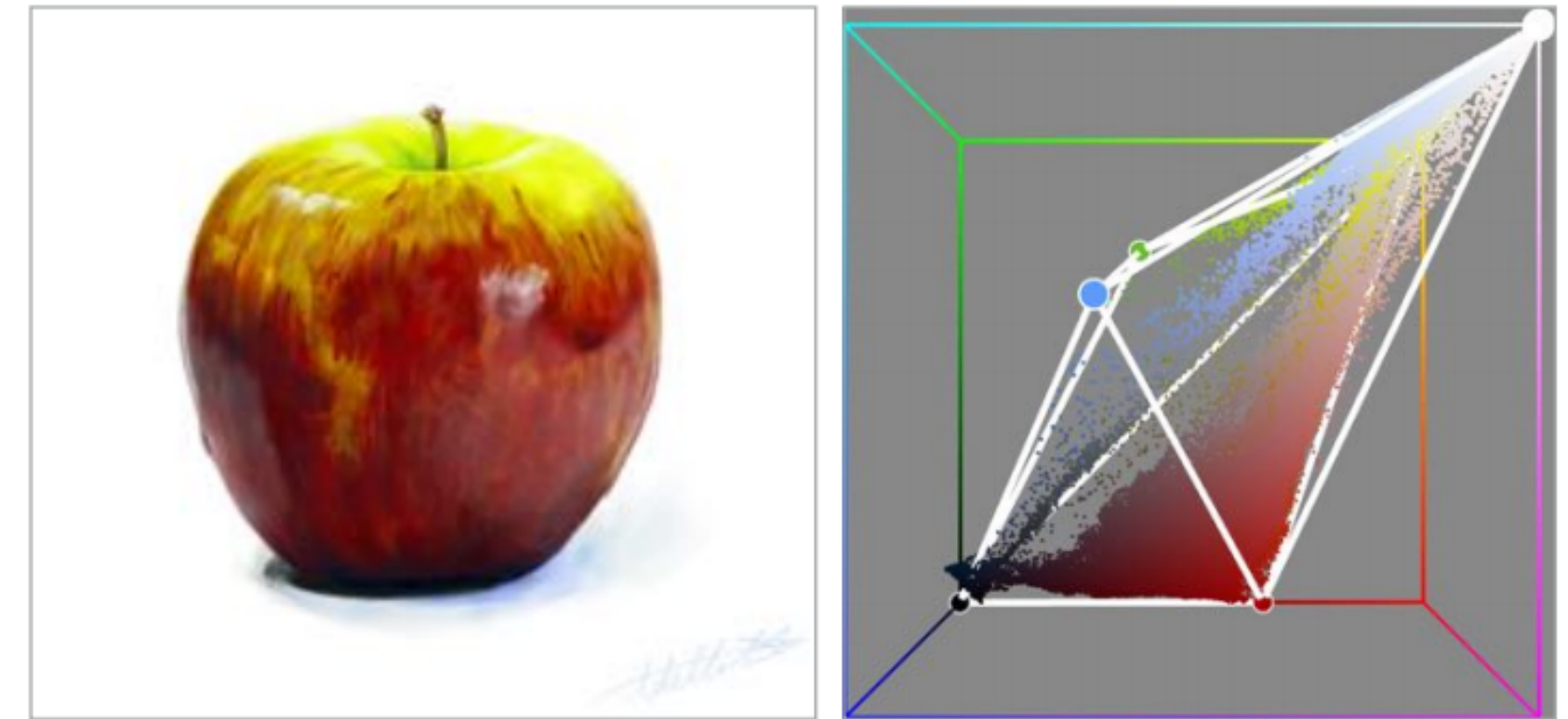
- Geometry-based convex palettes
  - Simpler
  - More general





# Our approach

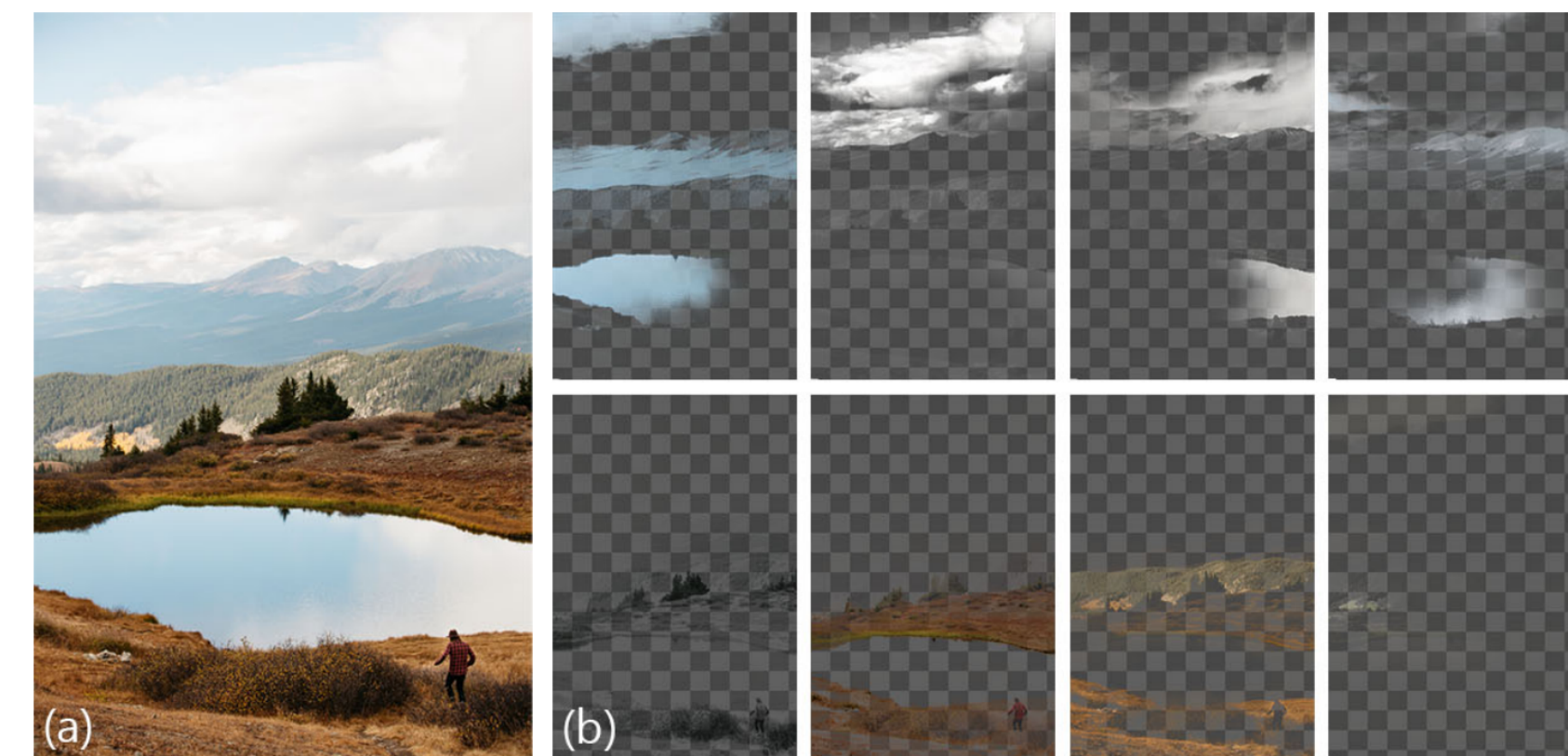
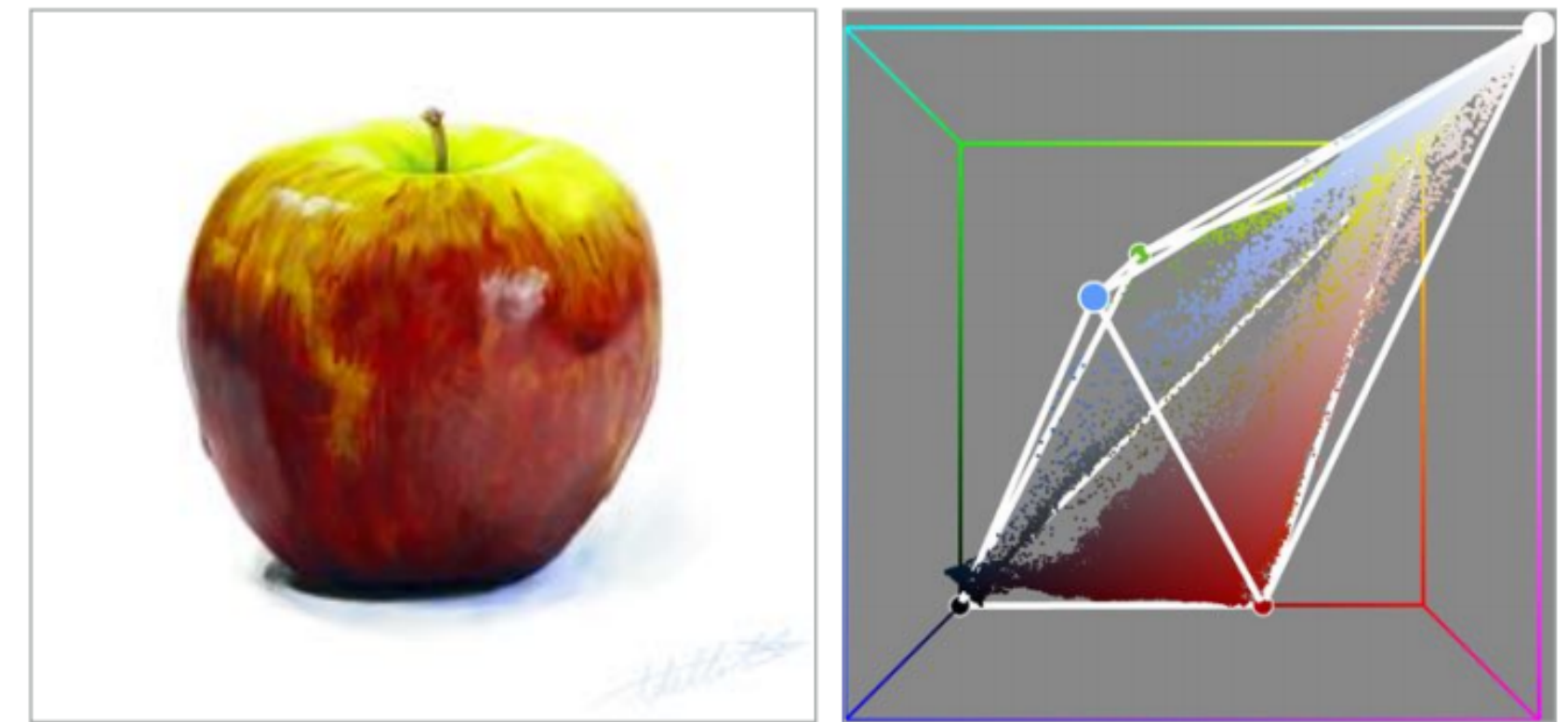
- Geometry-based convex palettes
  - Simpler
  - More general





# Our approach

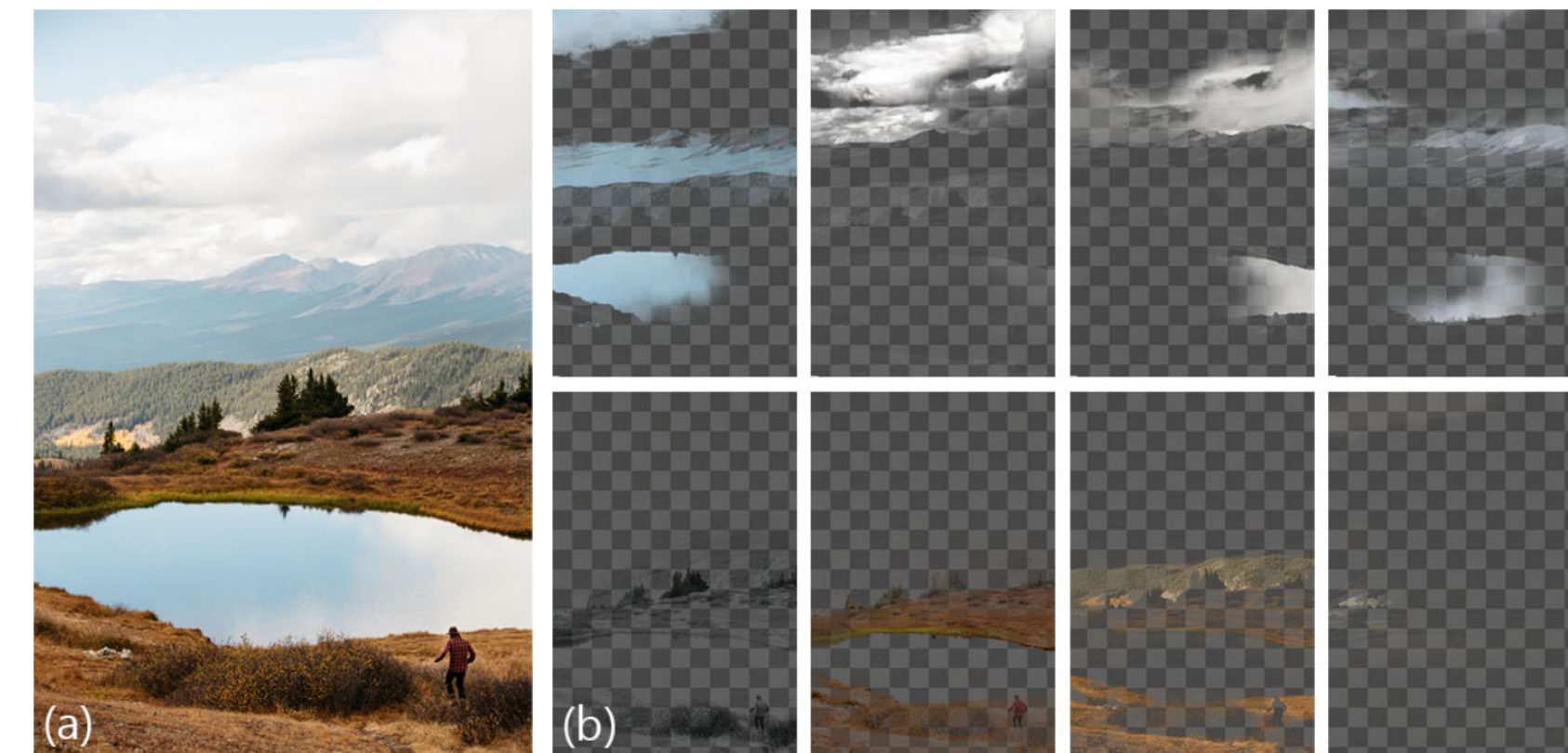
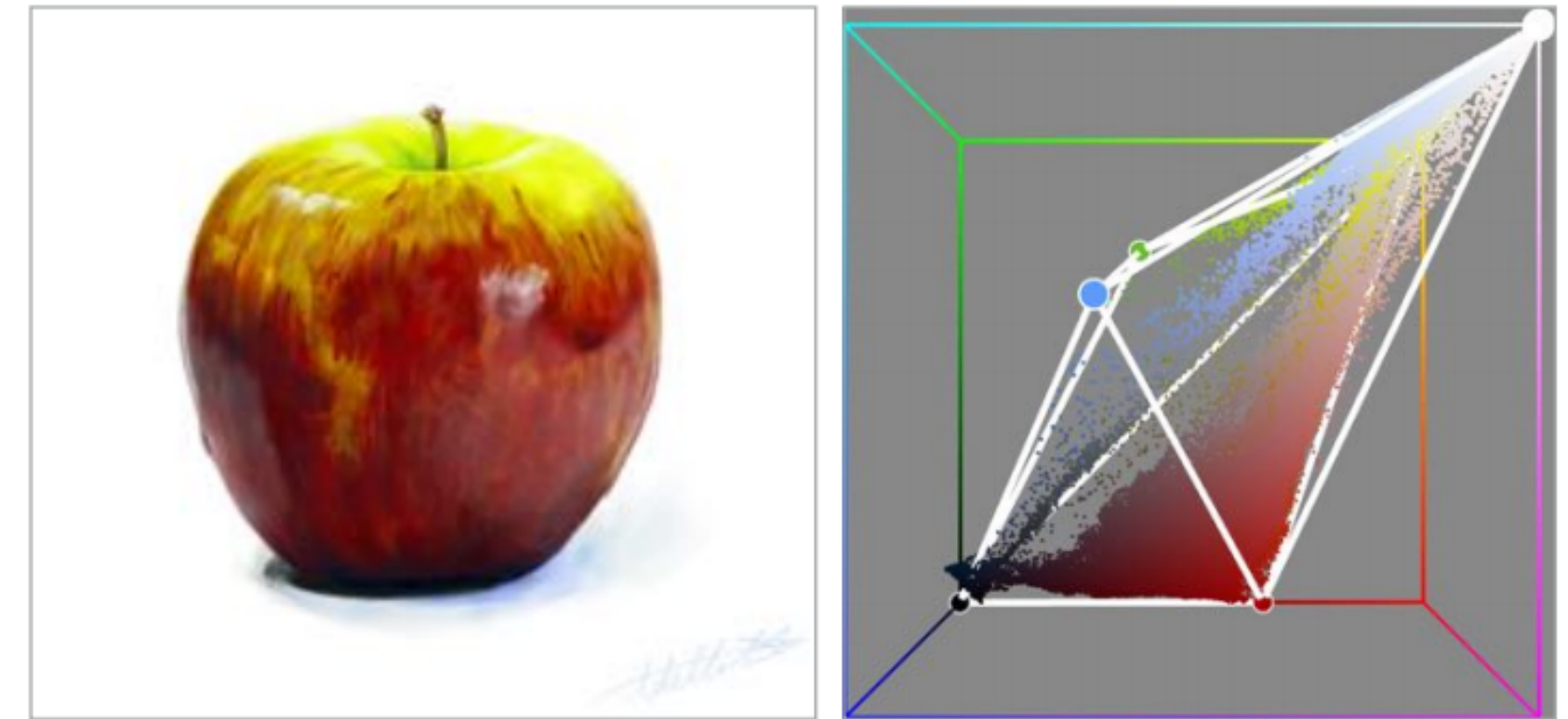
- Geometry-based convex palettes
  - Simpler
  - More general
  
- Additive-mixing layers





# Our approach

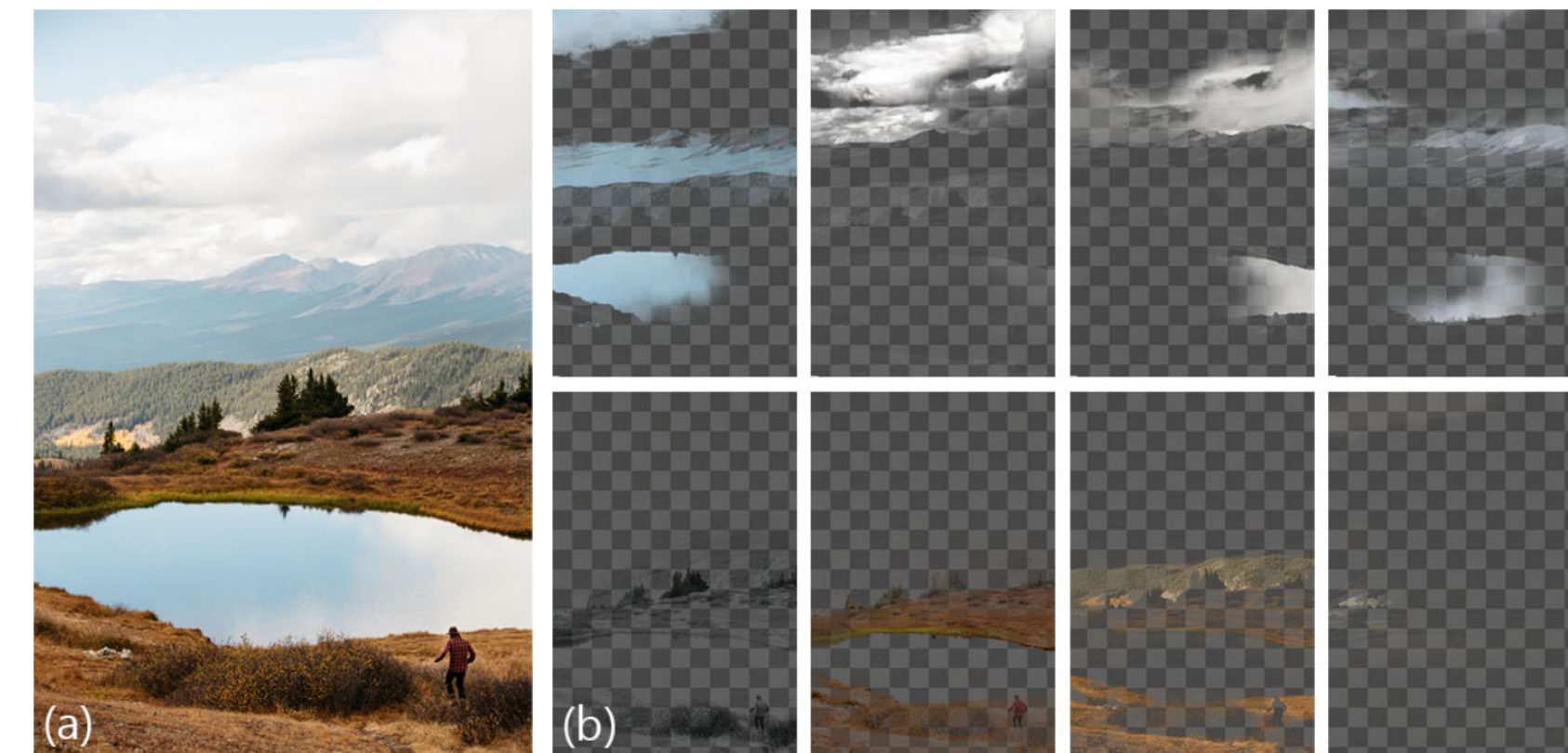
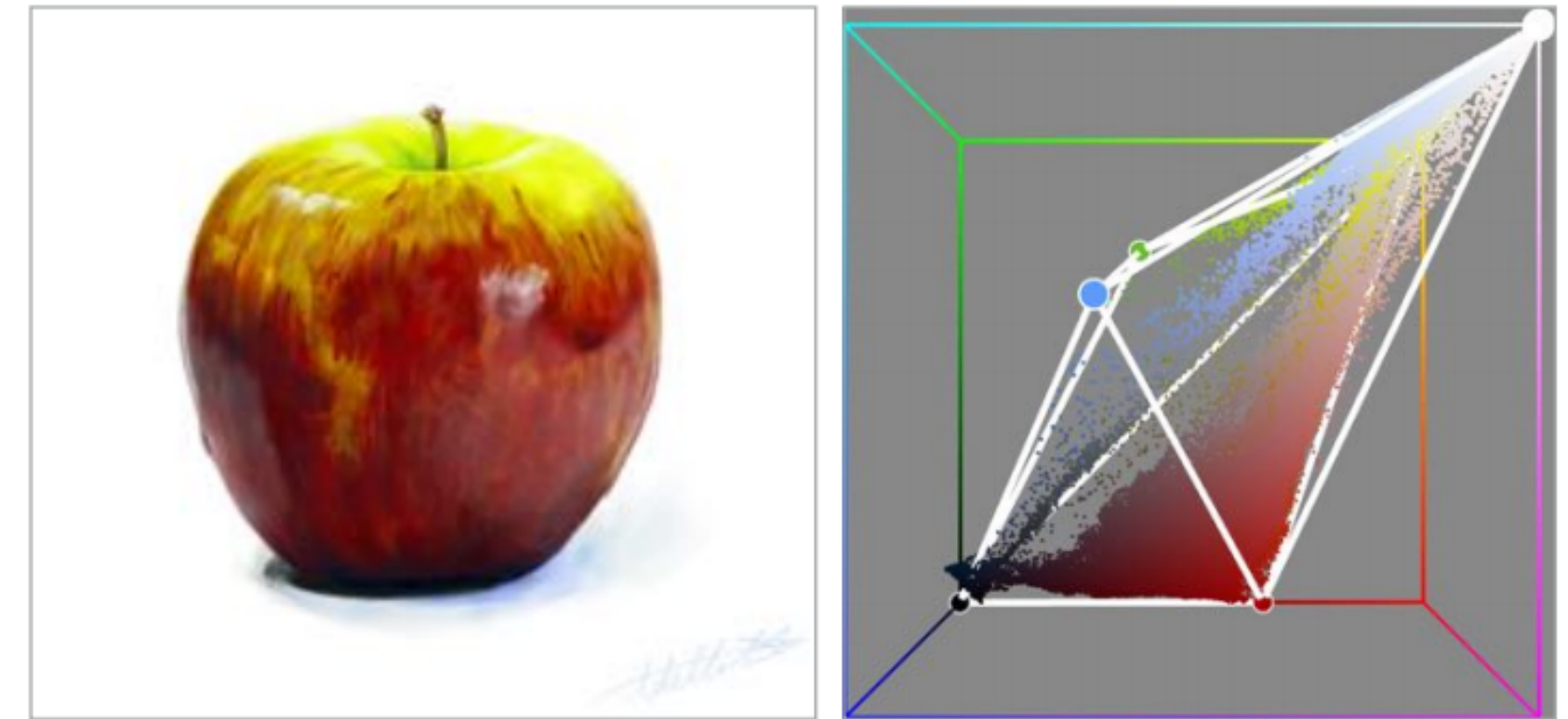
- Geometry-based convex palettes
  - Simpler
  - More general
- Additive-mixing layers
  - Single colors





# Our approach

- Geometry-based convex palettes
  - Simpler
  - More general
- Additive-mixing layers
  - Single colors
  - More general



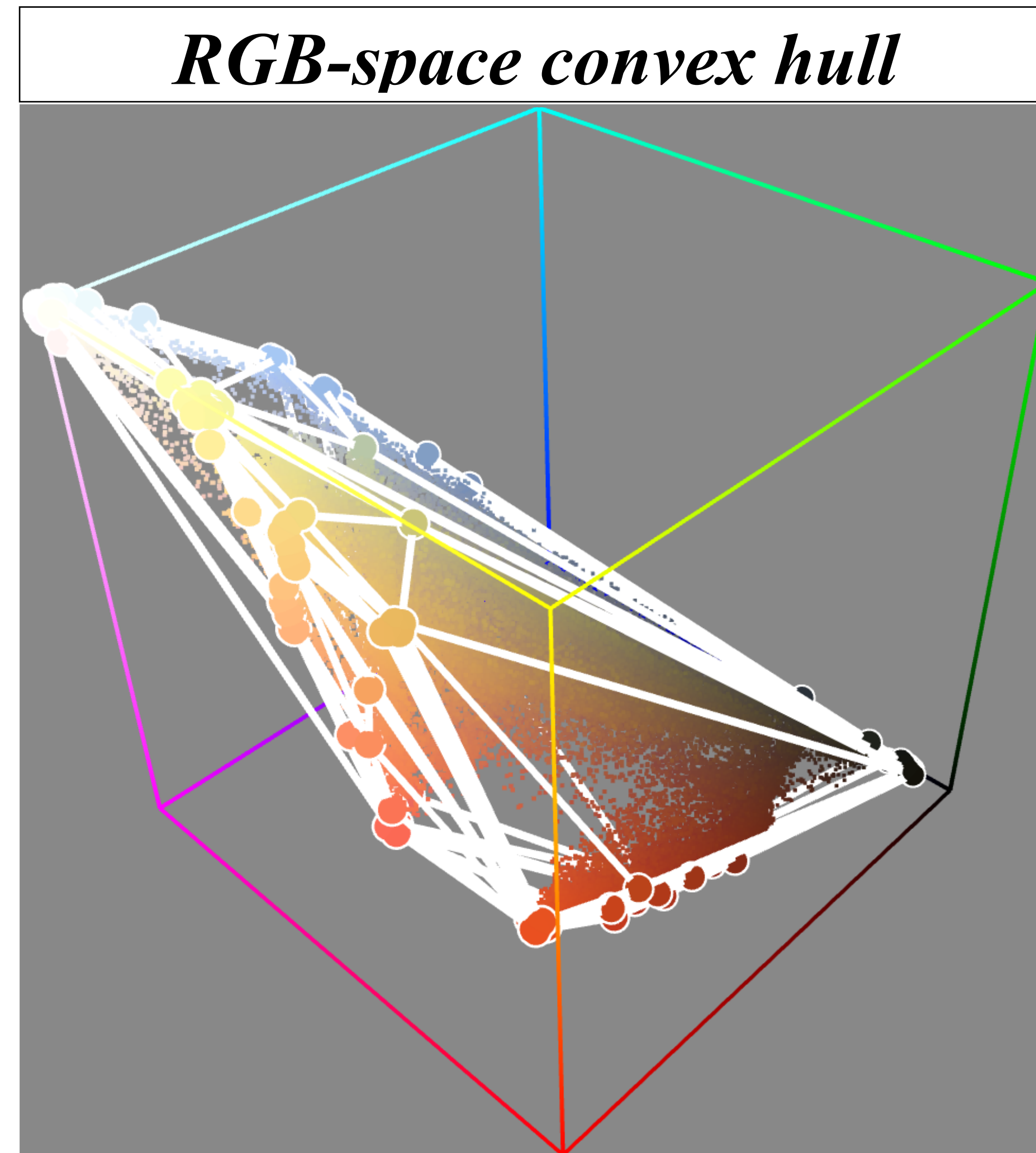


# Palette extraction



# Convex hulls in RGB

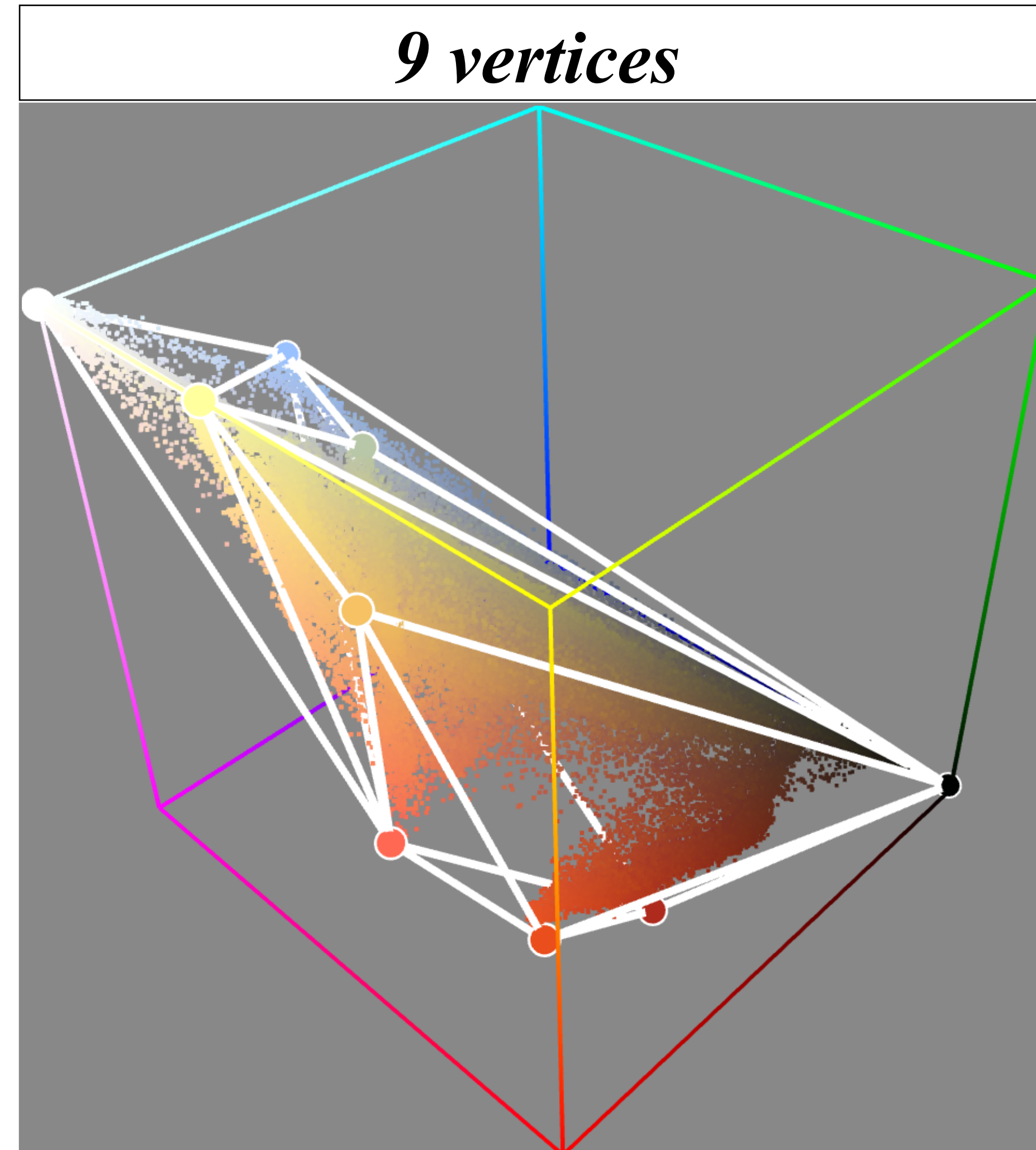
- Image colors show a convex structure in RGB [Tan et al. 2016]





# Palette Size

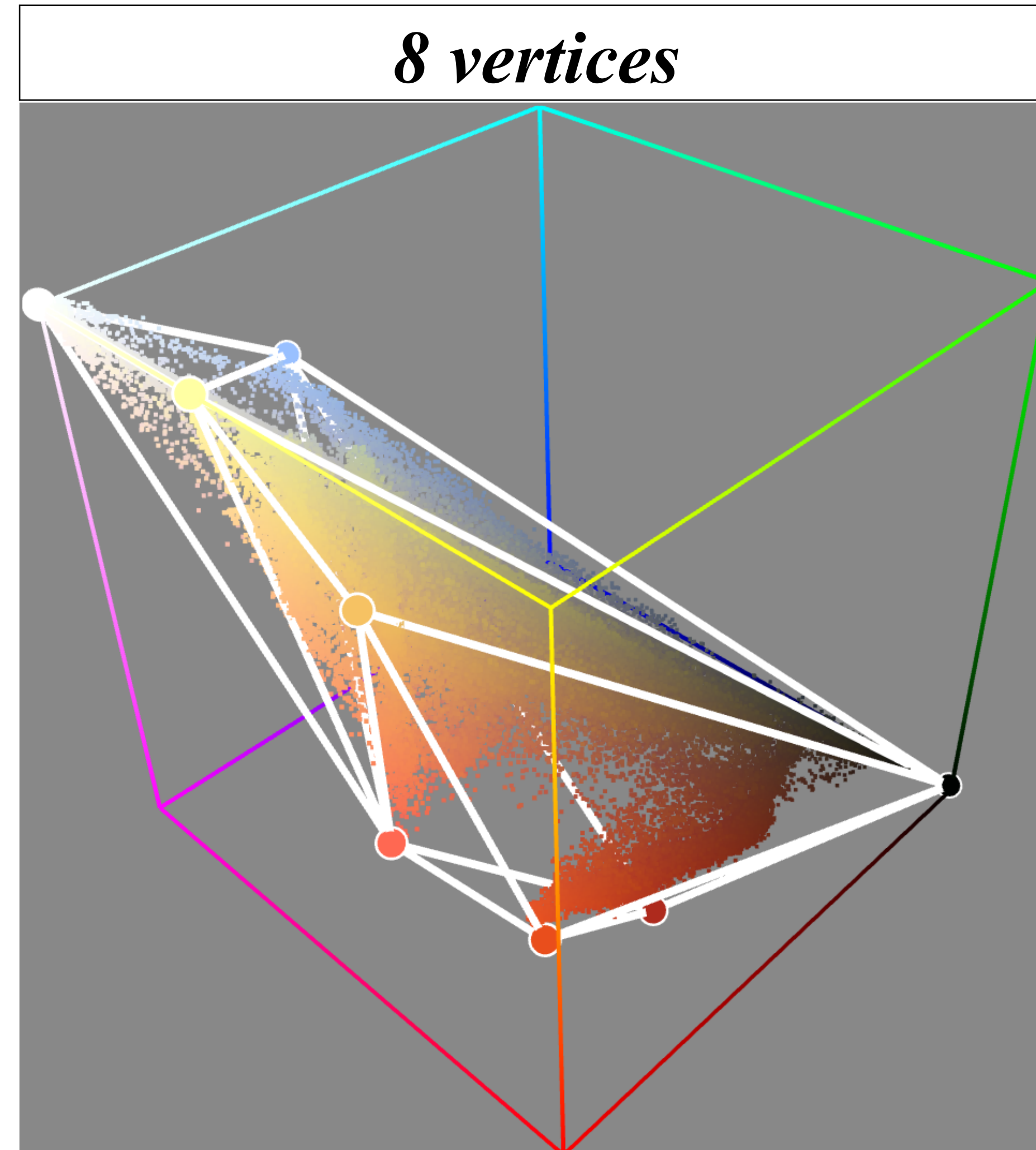
- The convex hull can be simplified to any complexity level.





# Palette Size

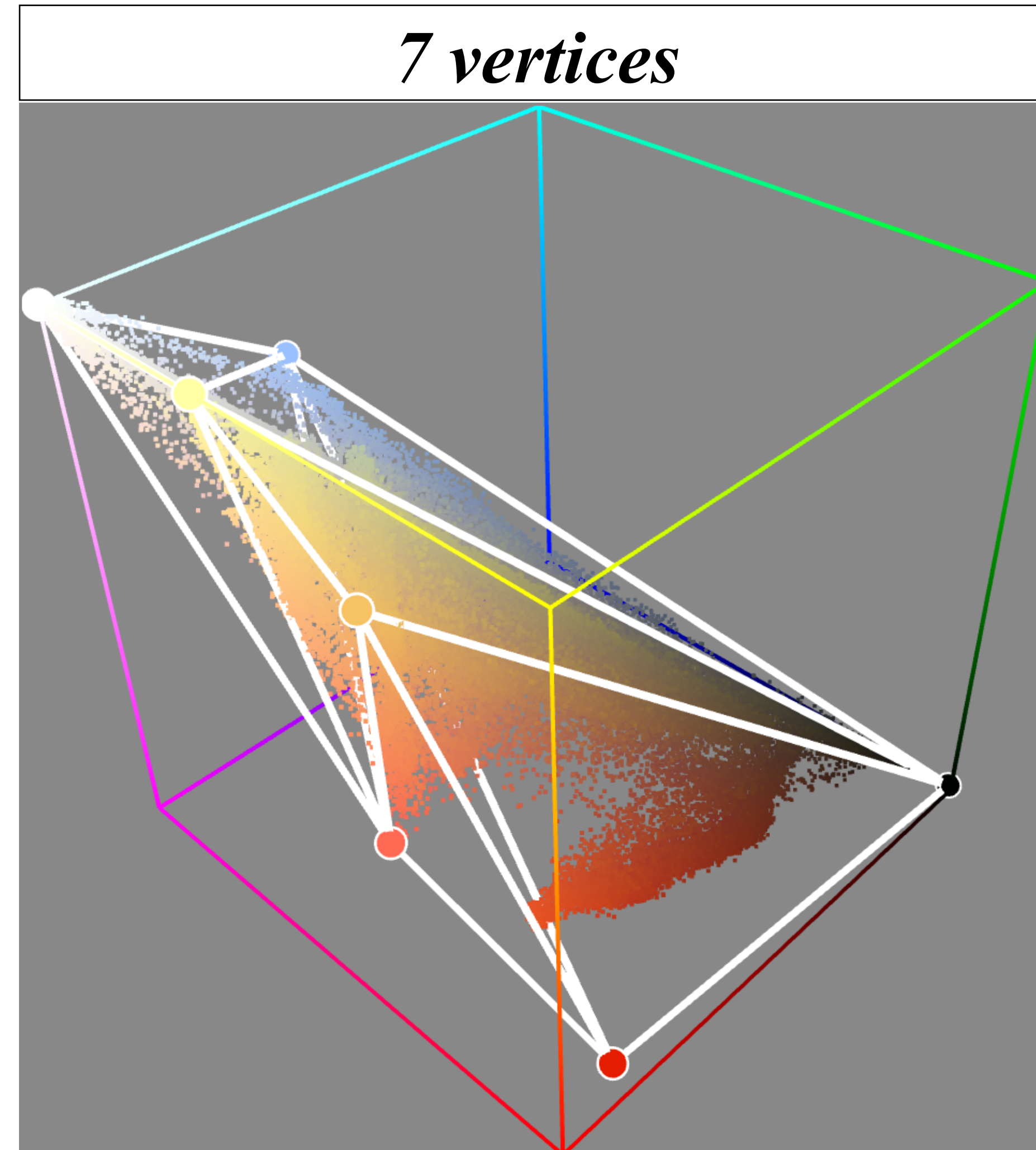
- The convex hull can be simplified to any complexity level.





# Palette Size

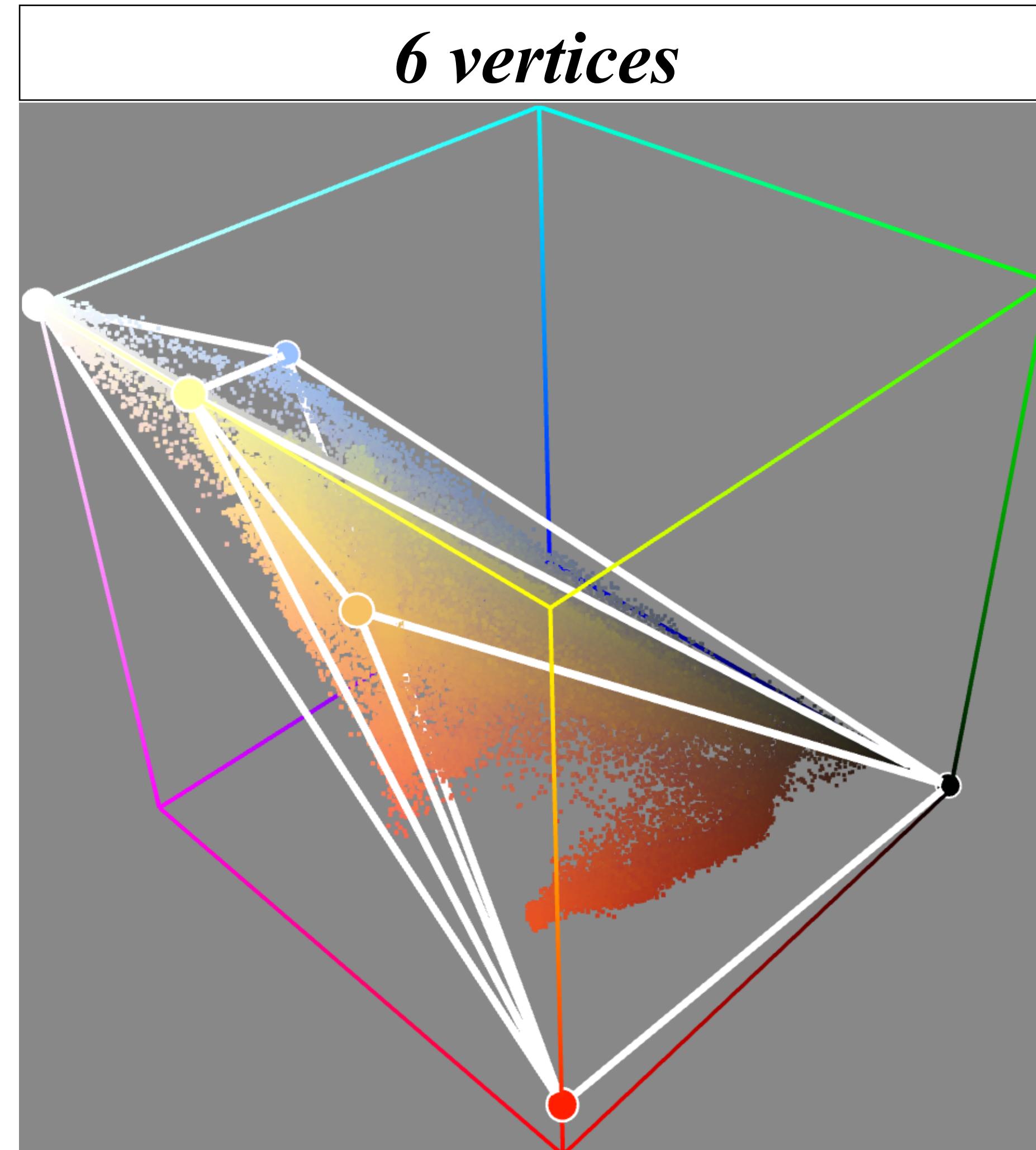
- The convex hull can be simplified to any complexity level.





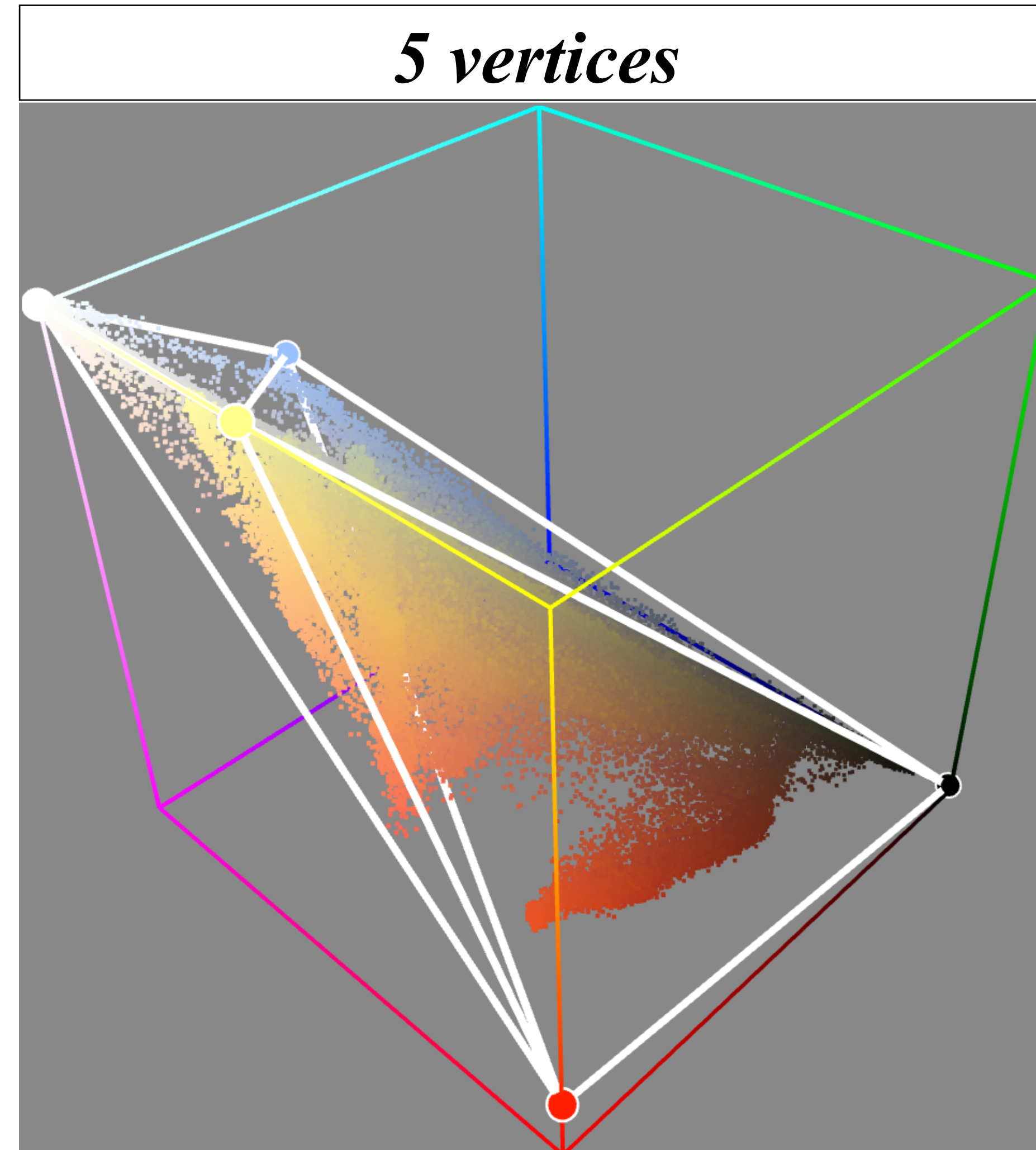
# Palette Size

- The convex hull can be simplified to any complexity level.



# Palette Size

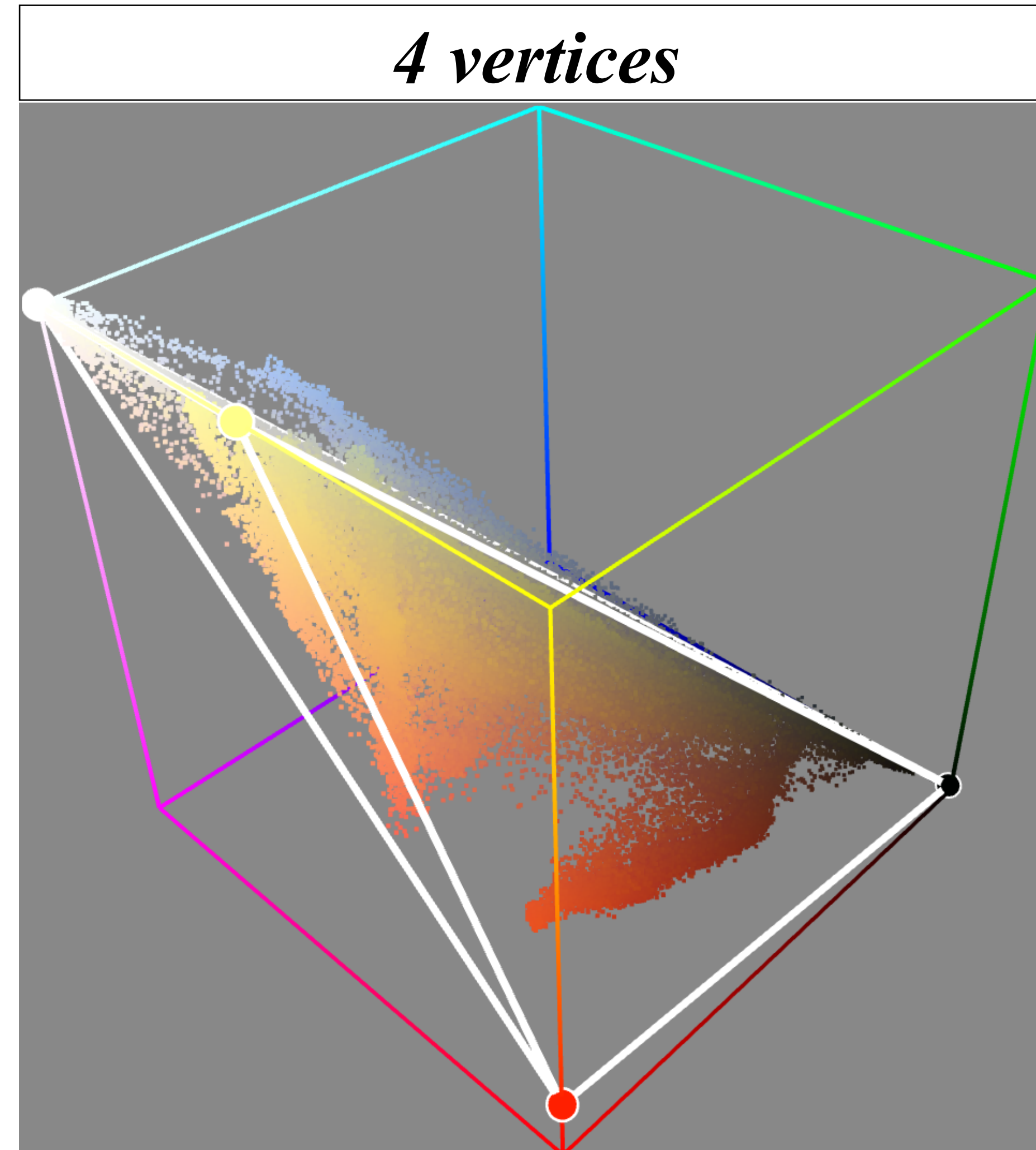
- The convex hull can be simplified to any complexity level.





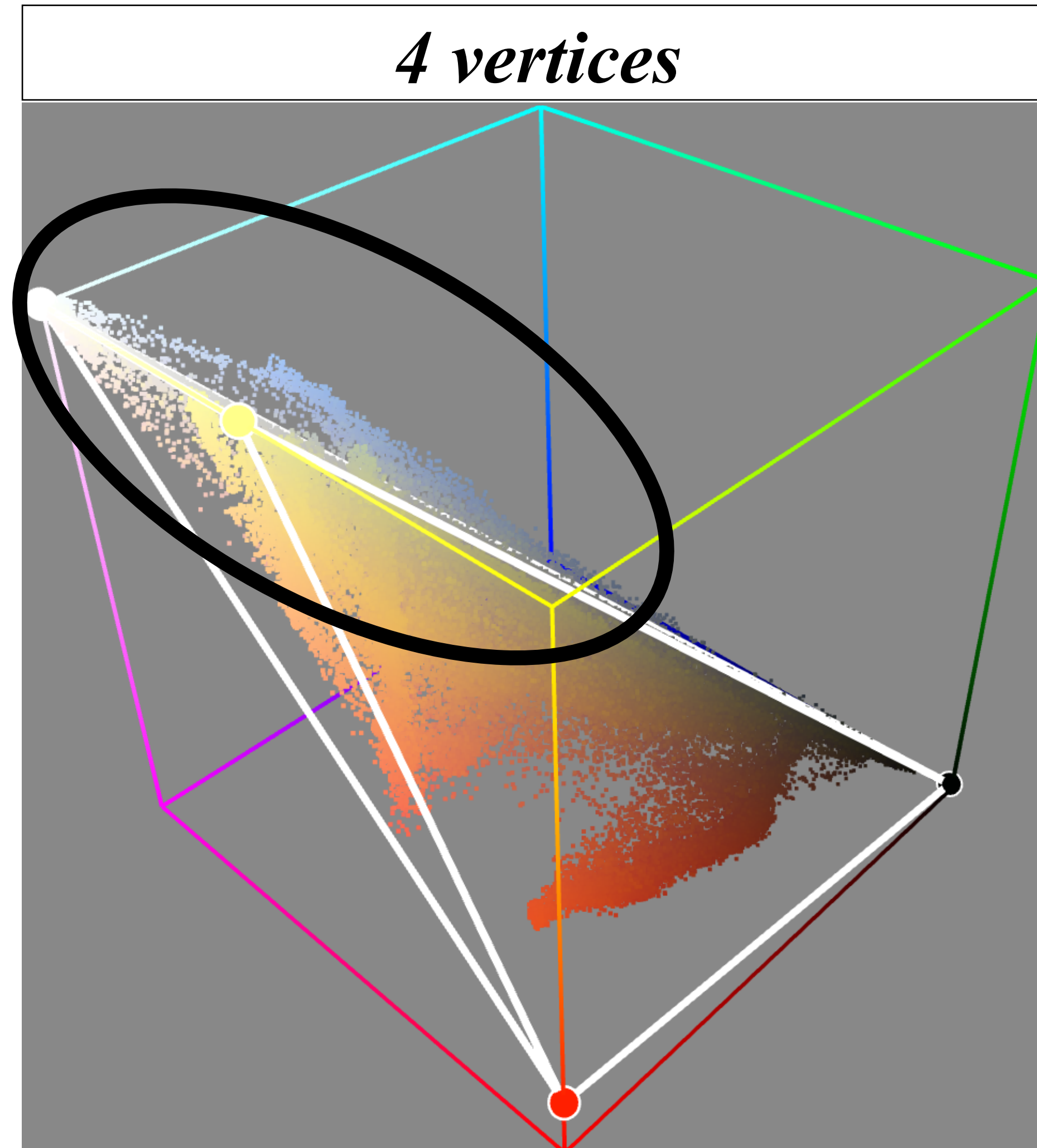
# Palette Size

- The convex hull can be simplified to any complexity level.



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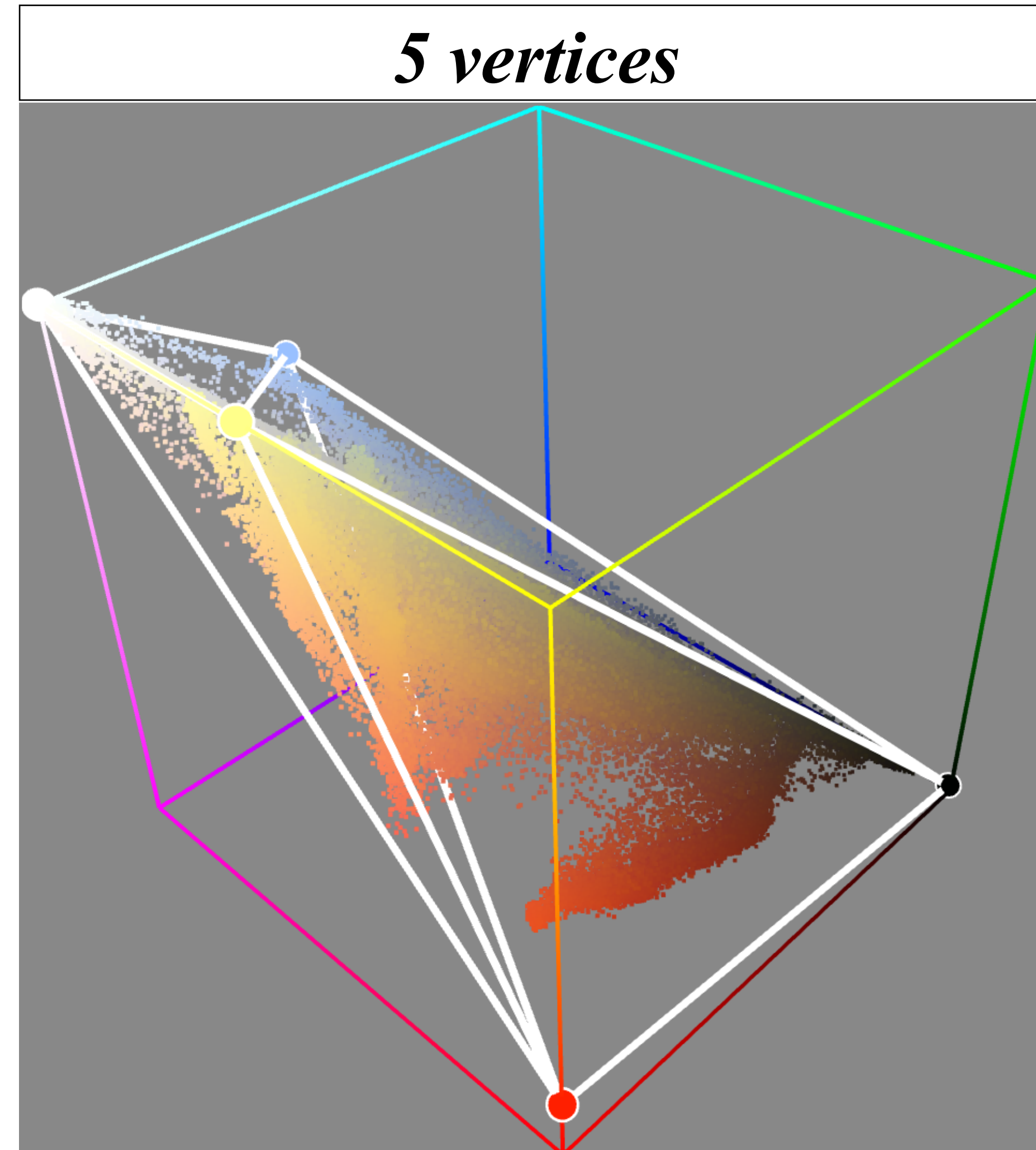
- The convex hull can be simplified to any complexity level.





# Palette Size

- Our automatic error-bound simplification



# **Image Decomposition**

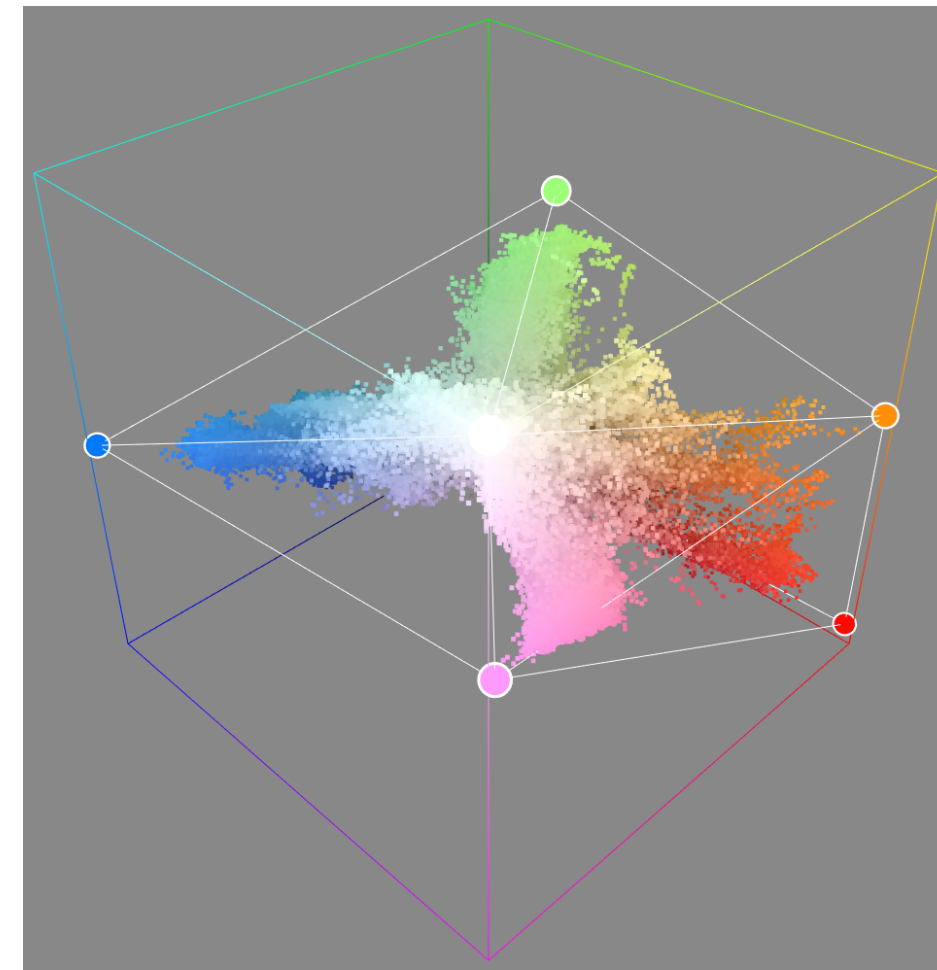


# Extracting mixing weights

image



RGB-space



Optimization



palette

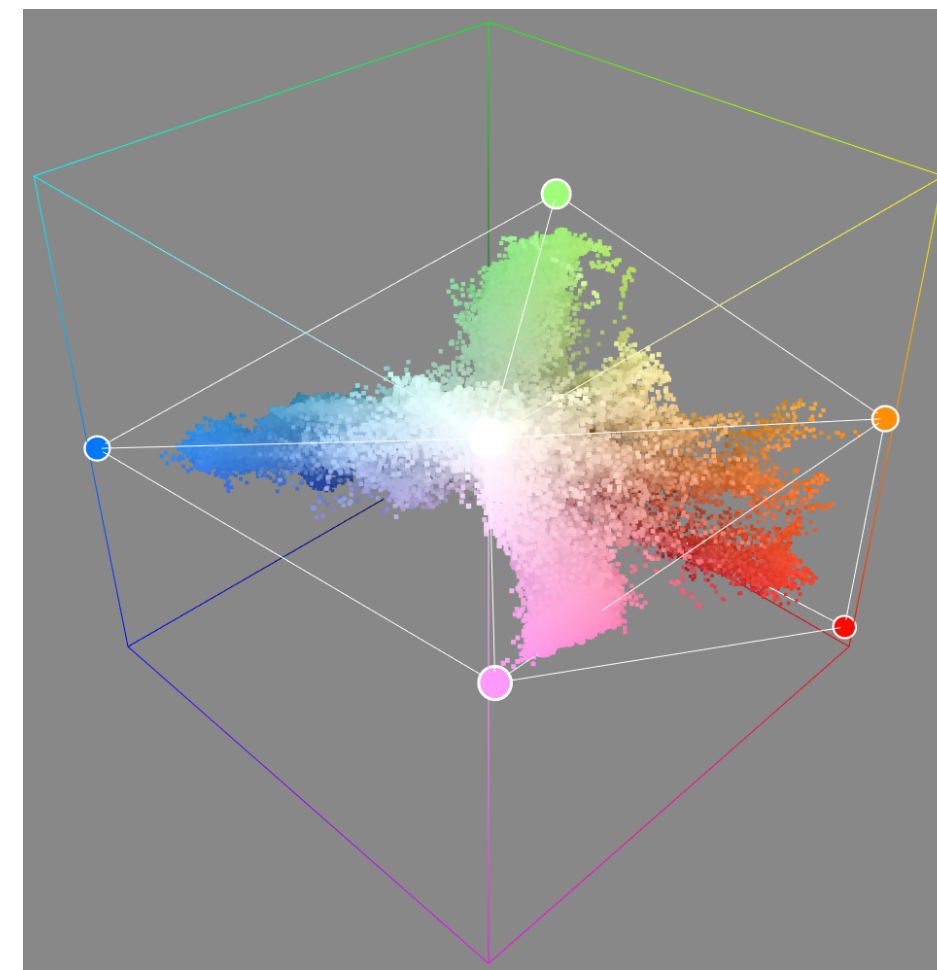
# Extracting mixing weights

image



palette

RGB-space



Optimization

- Slow for high resolutions



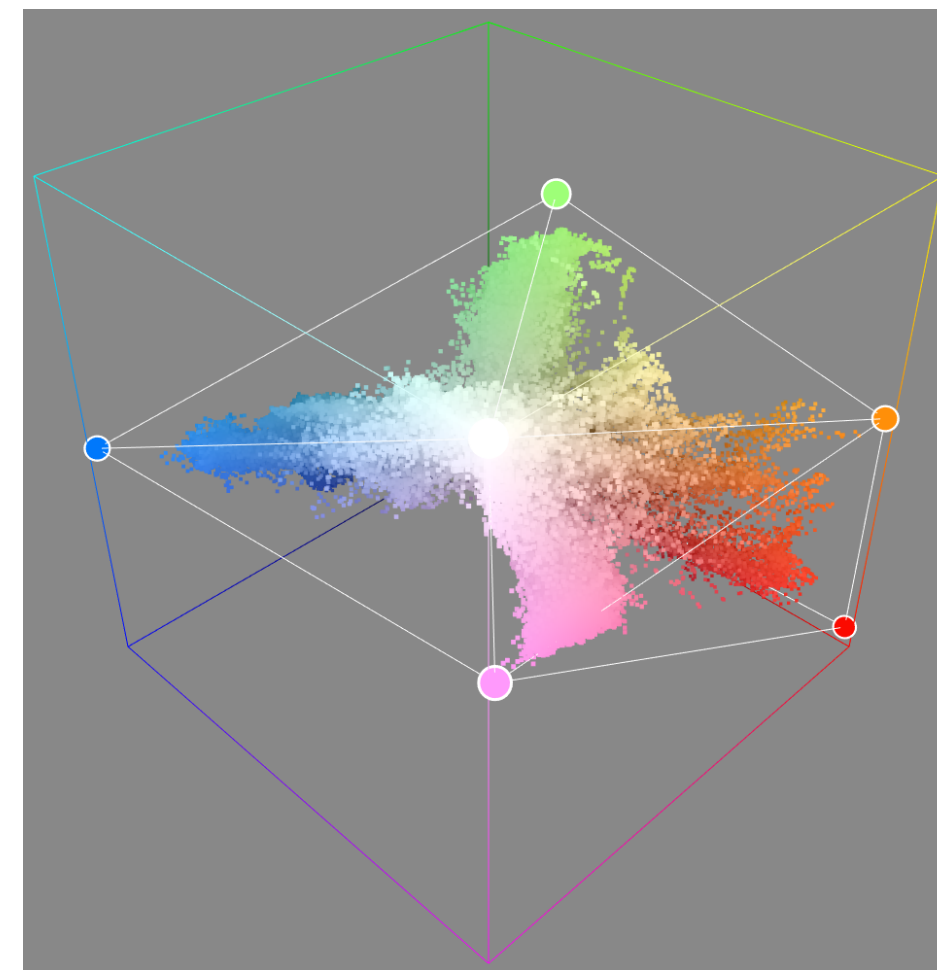
# Extracting mixing weights

image



palette

RGB-space



Optimization

- Slow for high resolutions
- Many parameters to tune

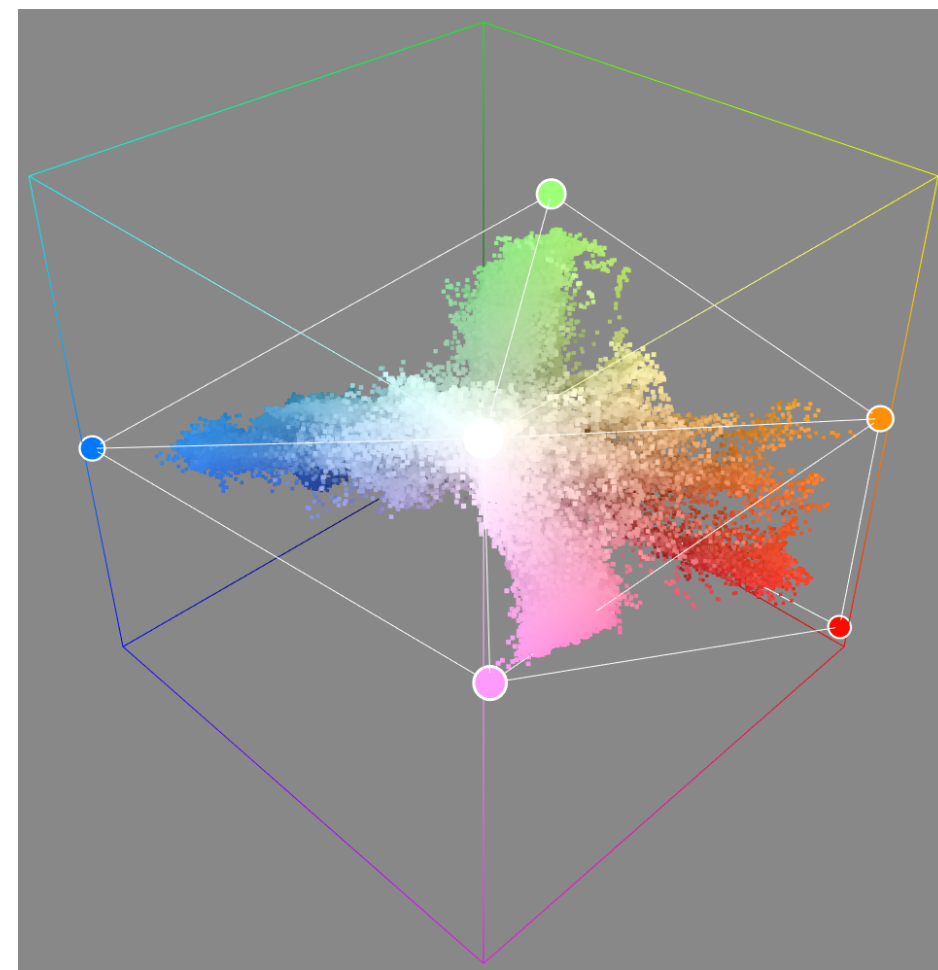
# Extracting mixing weights

image



palette

RGB-space



Optimization

- Slow for high resolutions
- Many parameters to tune
- Per-image parameters



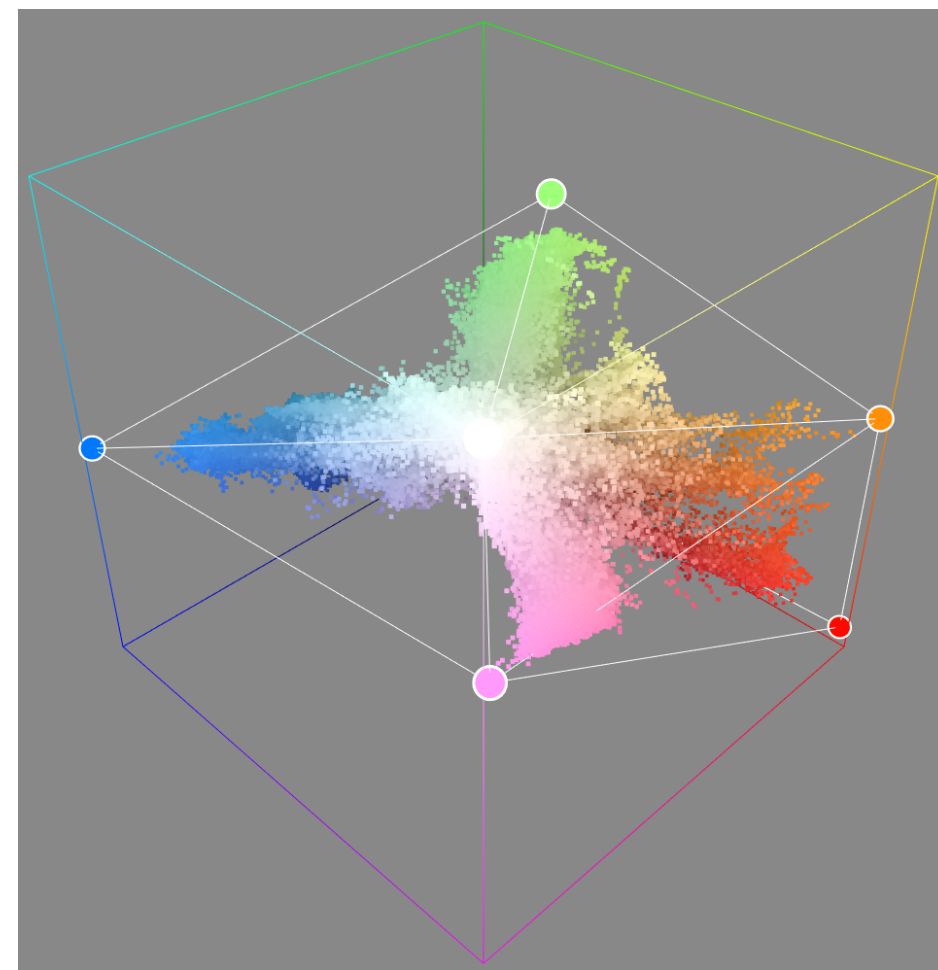
# Extracting mixing weights

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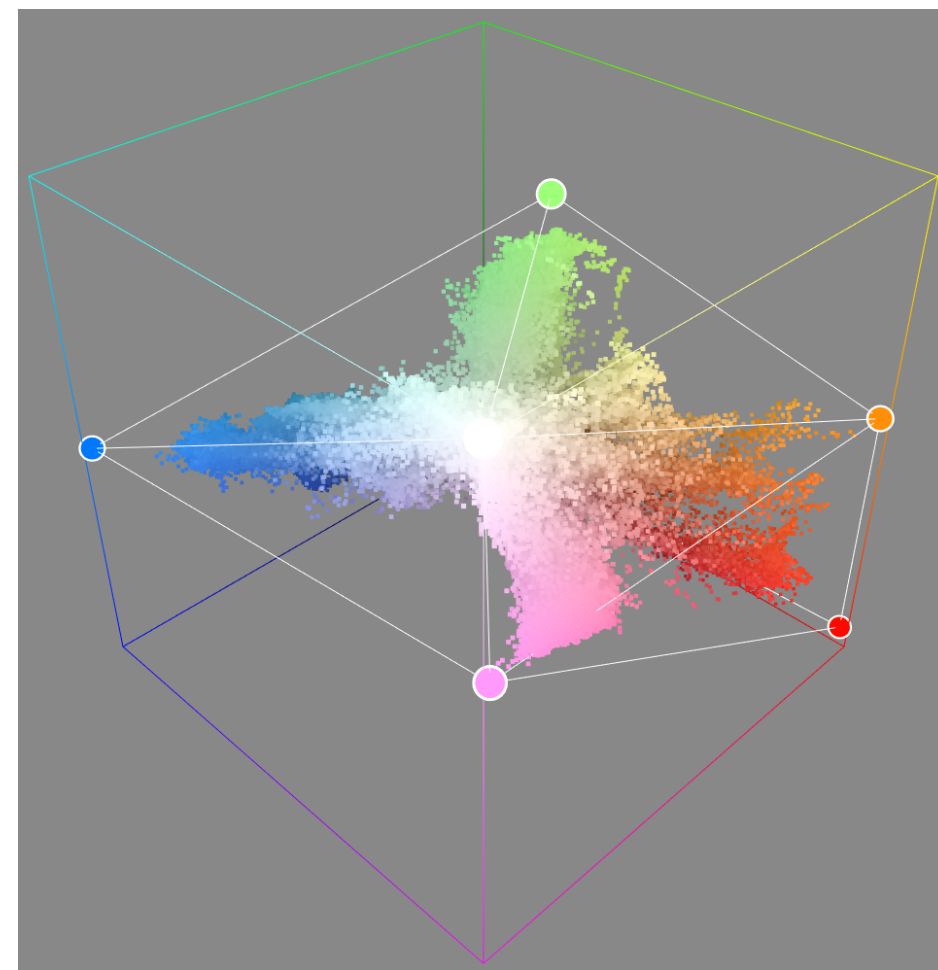
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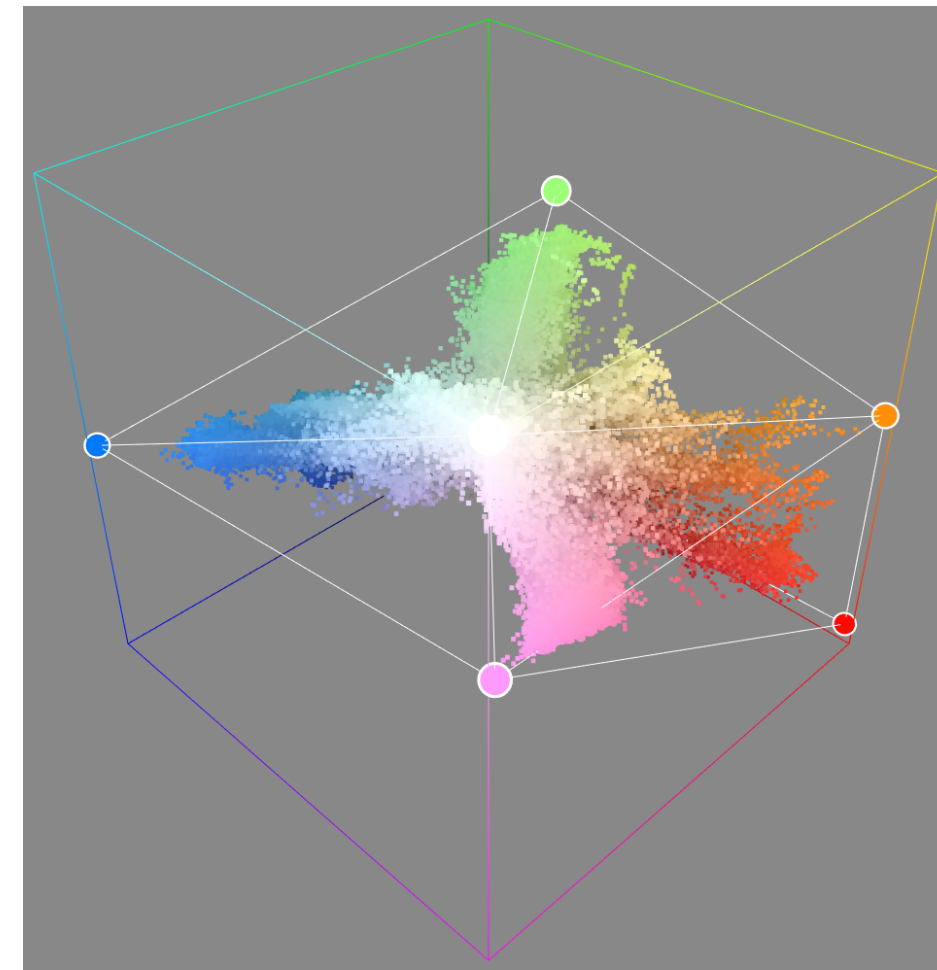


# Extracting mixing weights

image



RGB-space



~~Optimization~~



palette

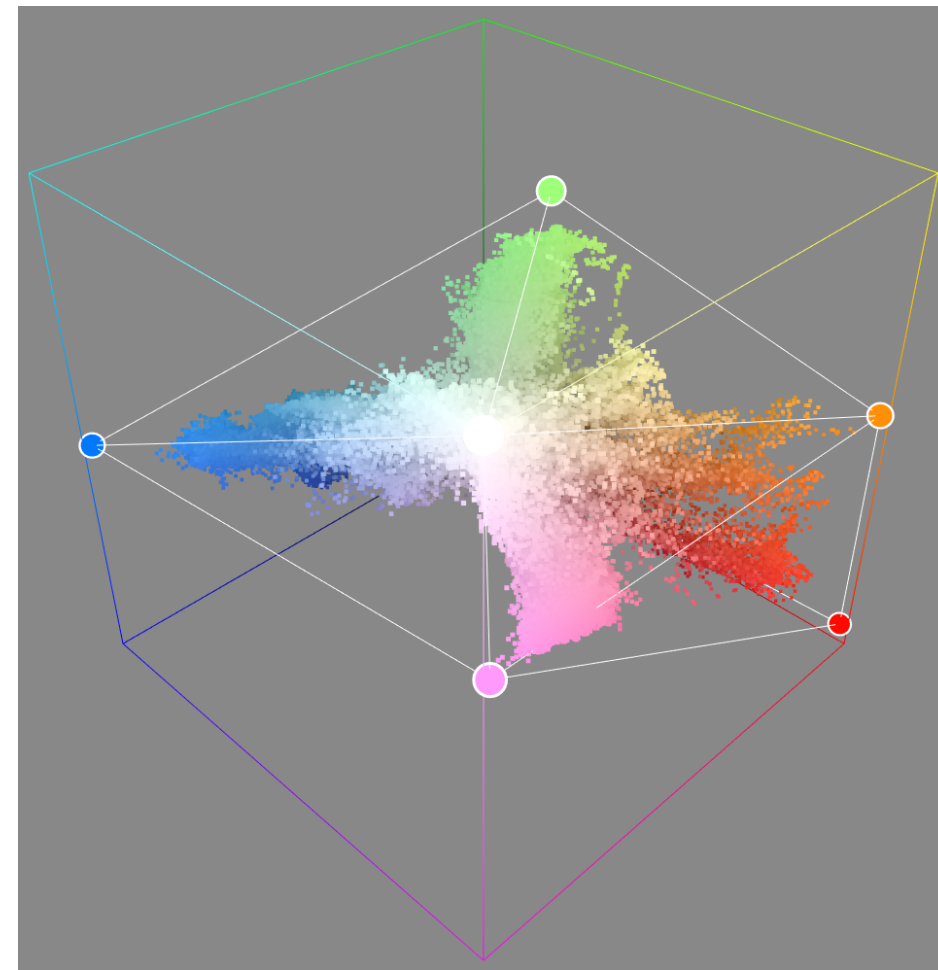
# Extracting mixing weights

image



palette

RGB-space



~~Optimization~~

**Generalized Barycentric  
Coordinates**



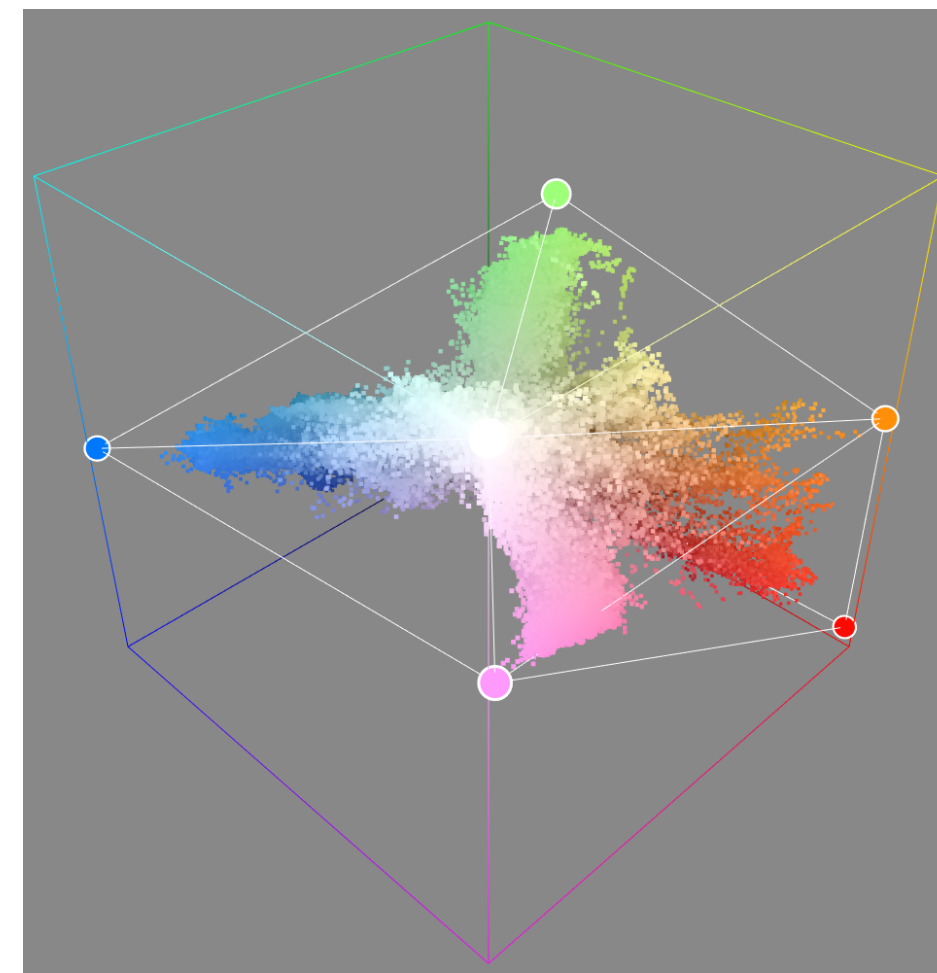
# Extracting mixing weights

image



palette

RGB-space



- Fast

~~Optimization~~

**Generalized Barycentric  
Coordinates**

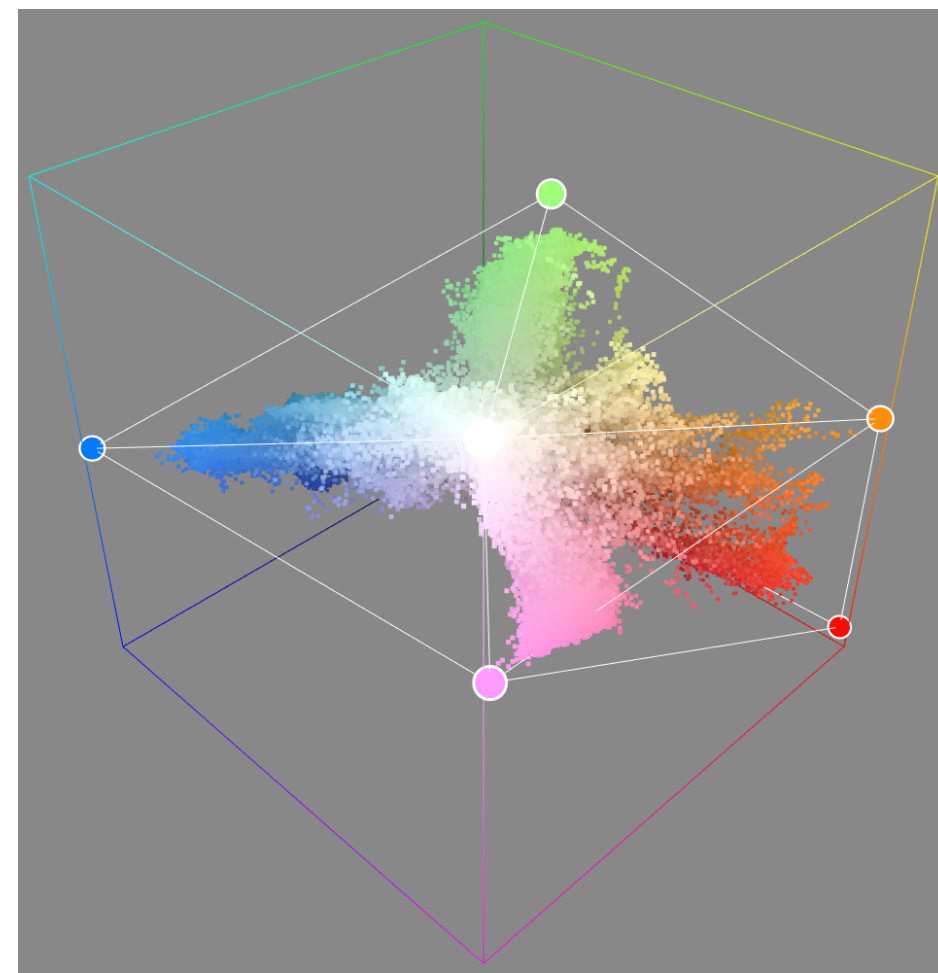
# Extracting mixing weights

image



palette

RGB-space



~~Optimization~~

**Generalized Barycentric  
Coordinates**

- Fast
- No parameters to tune



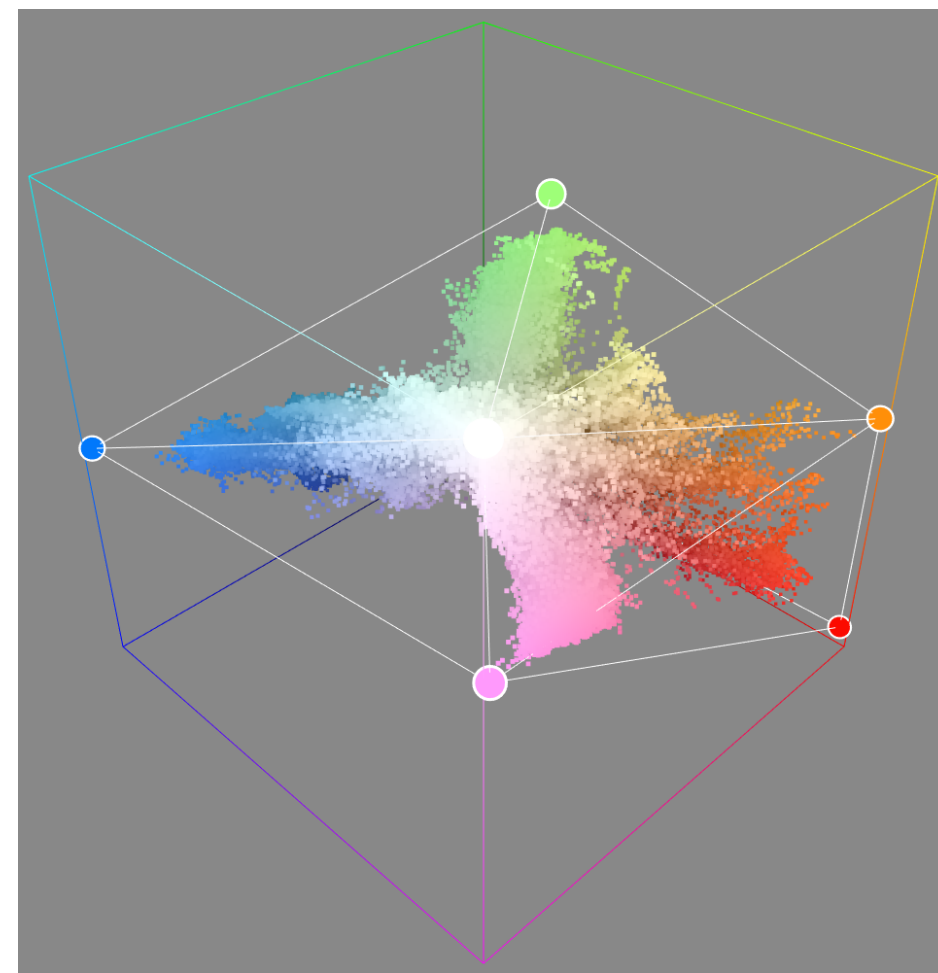
# Extracting mixing weights

image



palette

RGB-space



~~Optimization~~

**Generalized Barycentric  
Coordinates**

- Fast
- No parameters to tune
- Does not guarantee spatial smoothness



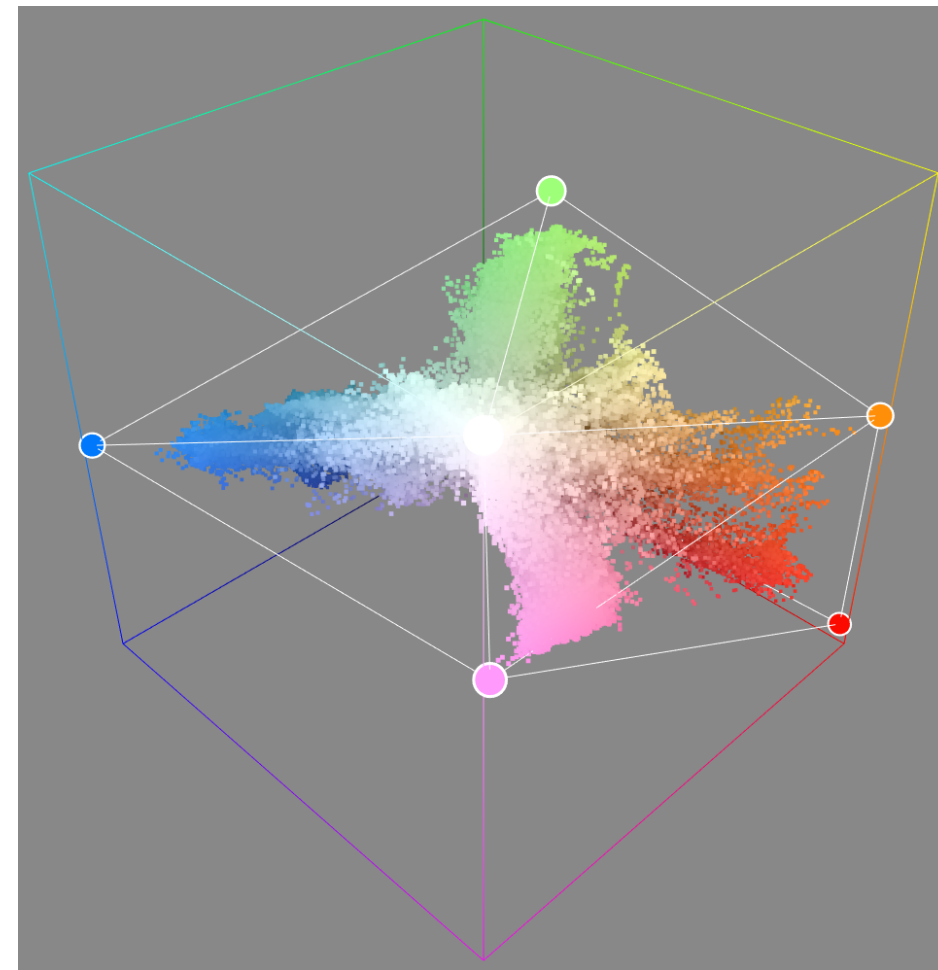
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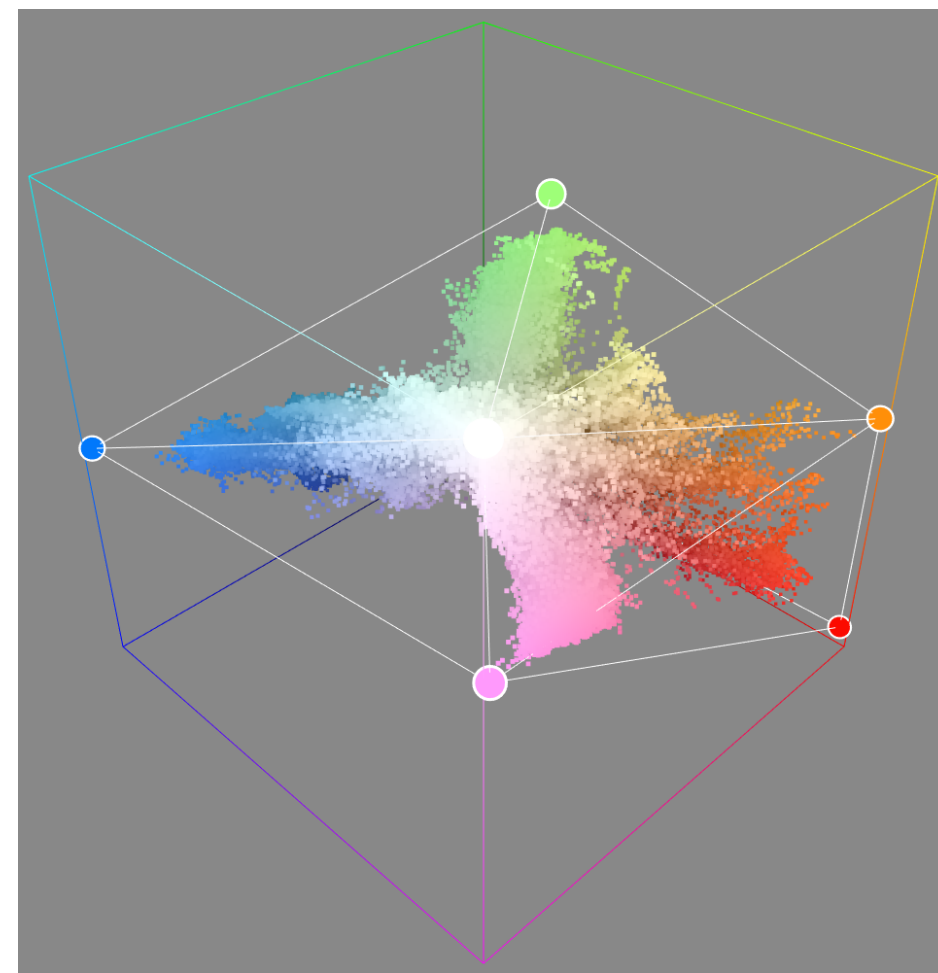
# Extracting mixing weights

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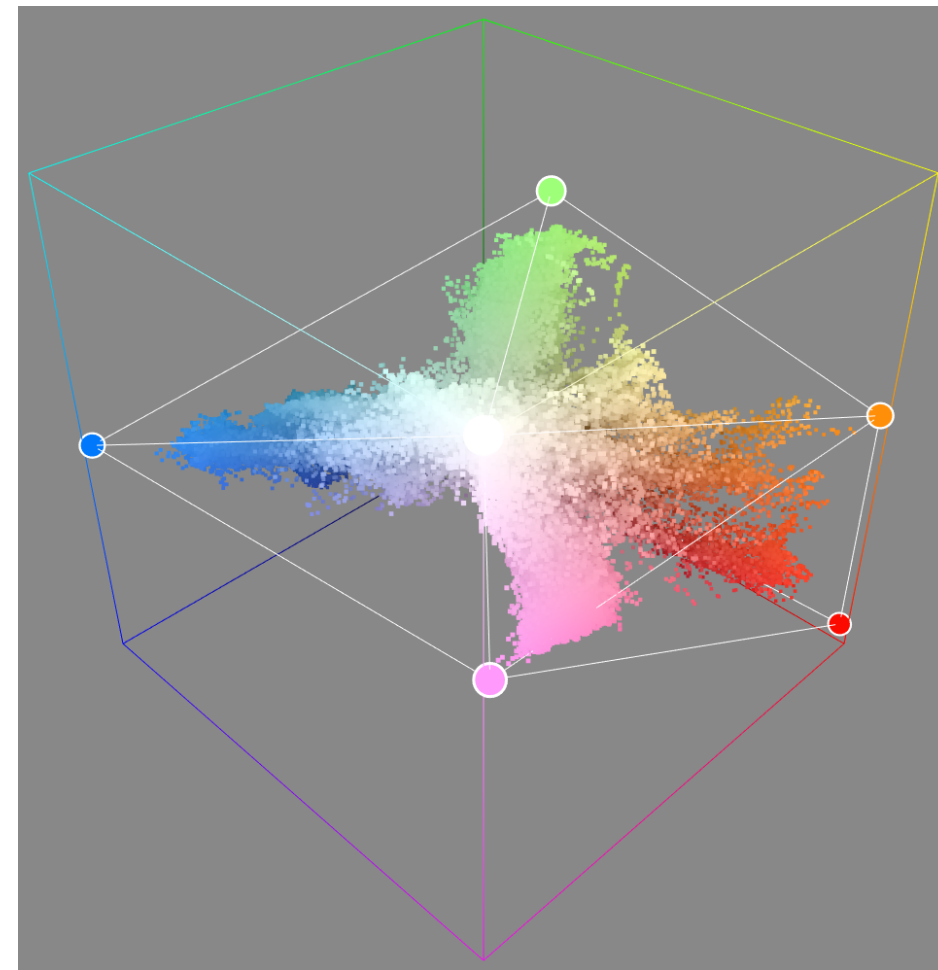
# Extracting mixing weights

image



palette

RGB-space



~~Optimization~~

~~Generalized Barycentric  
Coordinates~~



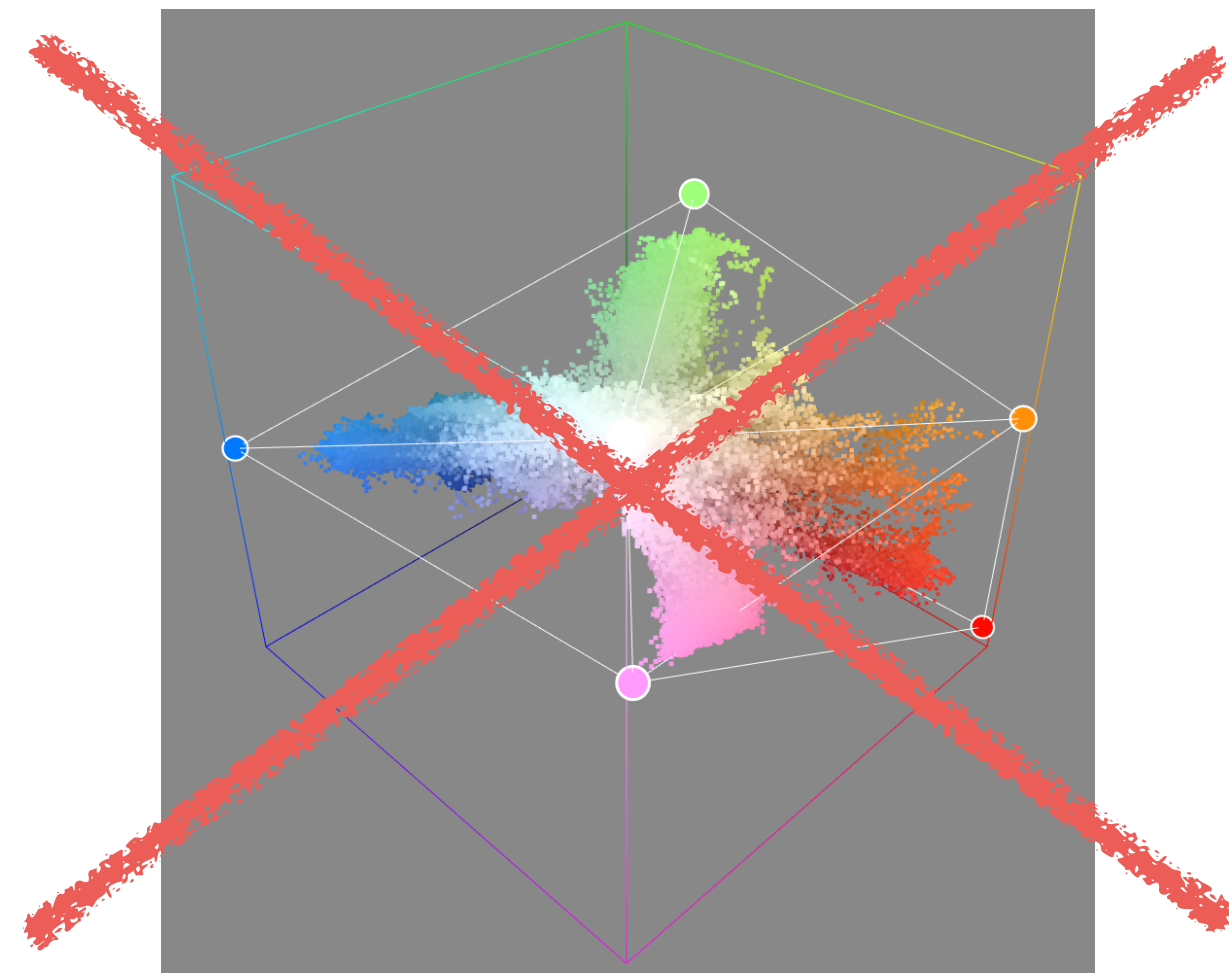
# Extracting mixing weights

image



palette

RGB-space

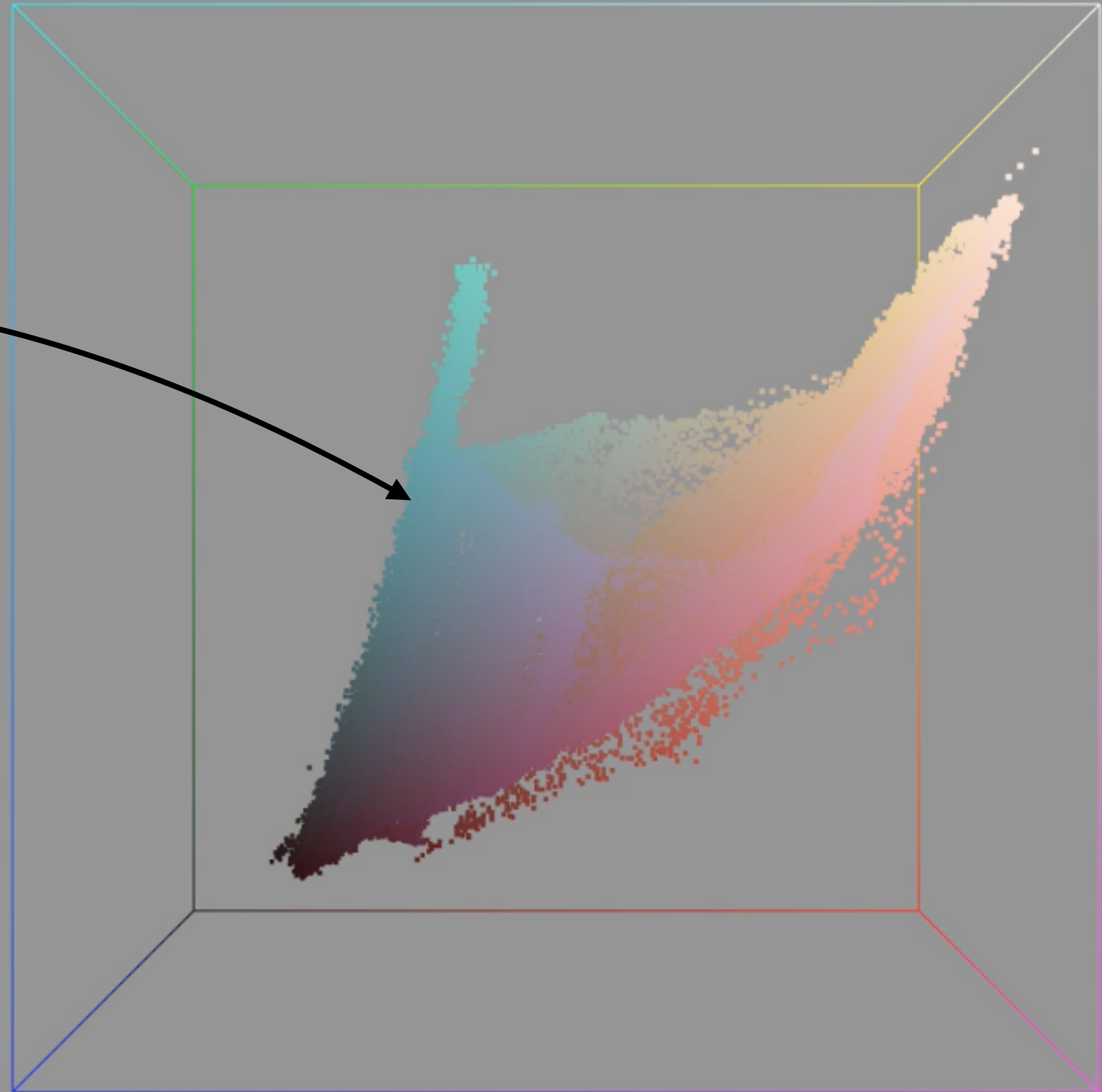
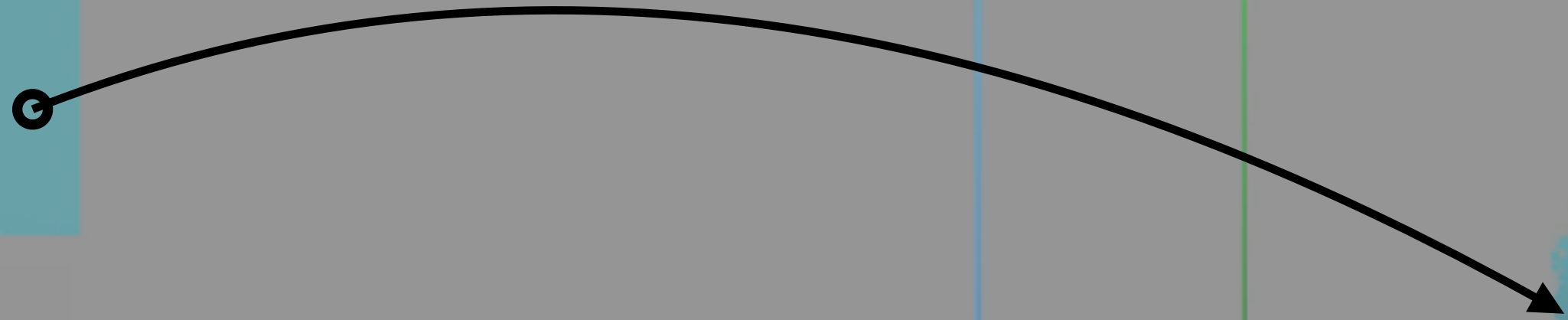


~~Optimization~~

~~Generalized Barycentric  
Coordinates~~



(R,G,B)

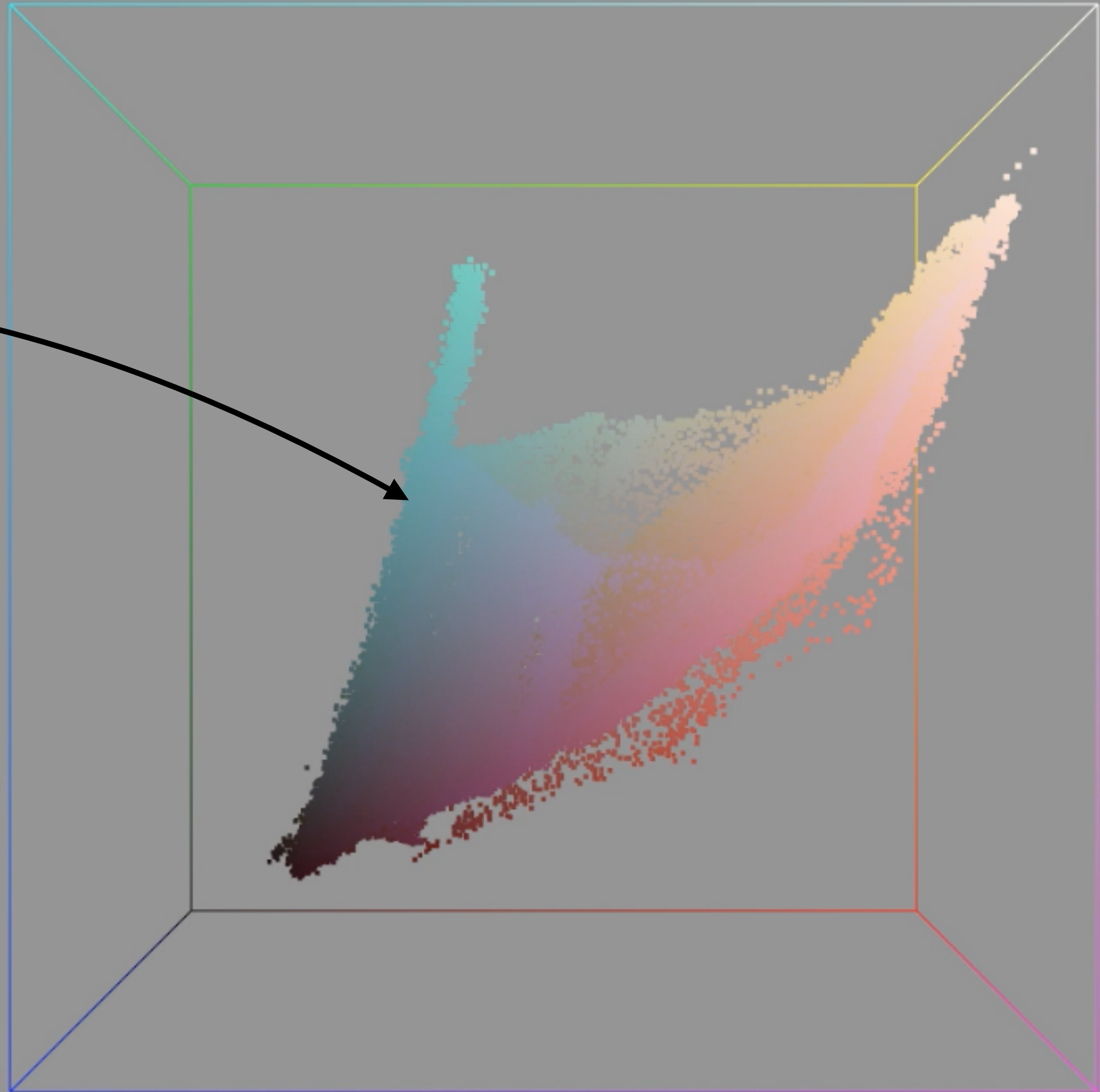
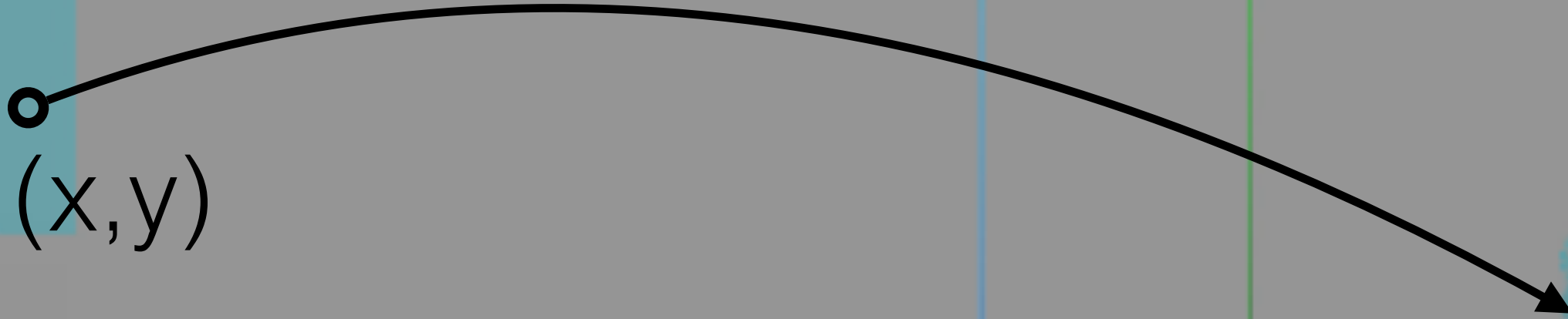






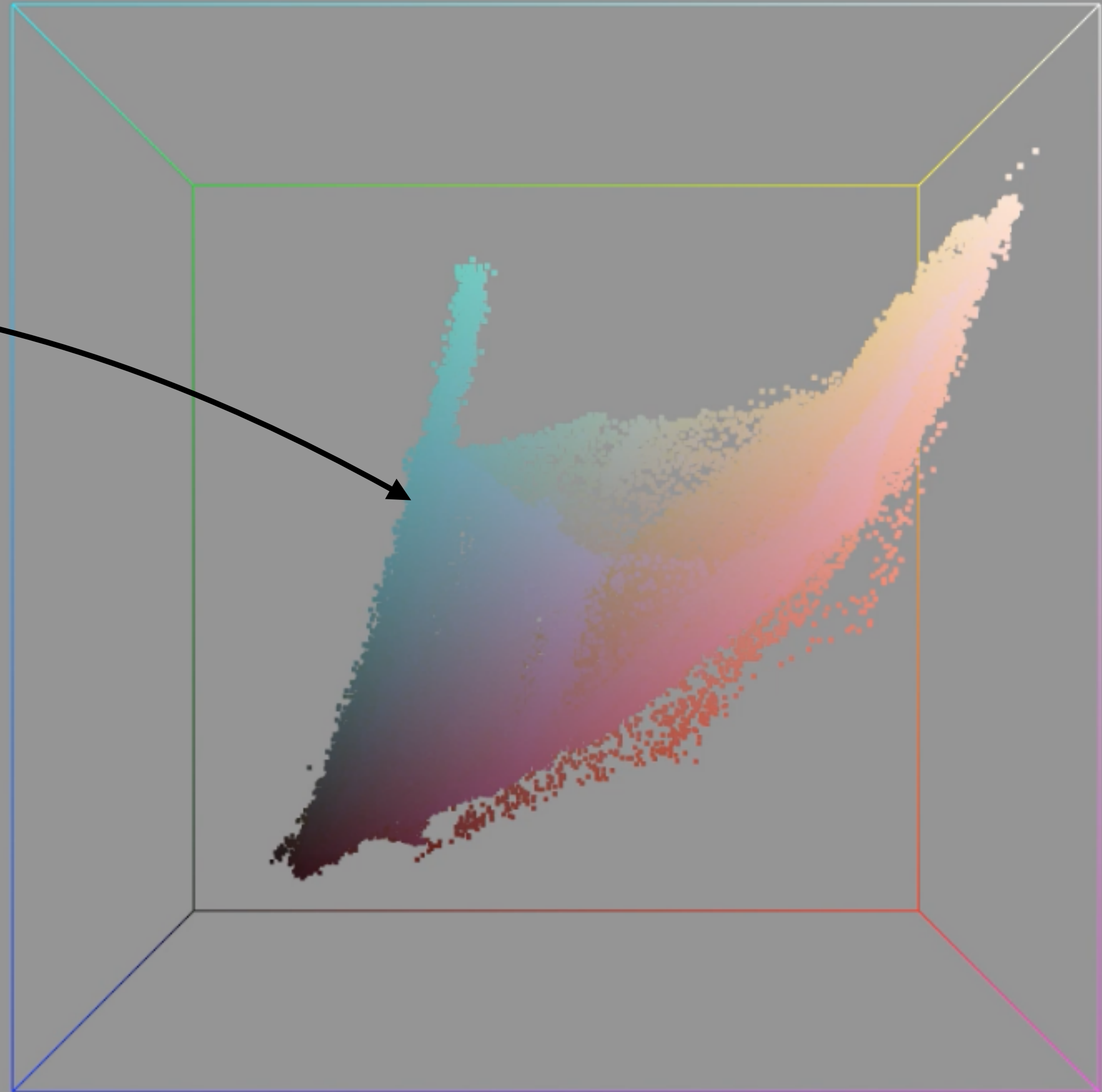
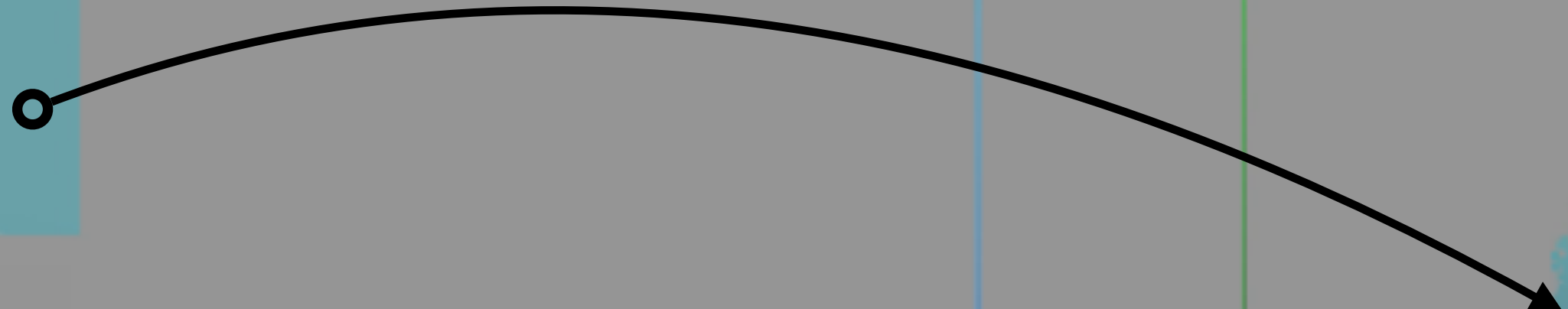
$(x,y)$

$(R,G,B)$





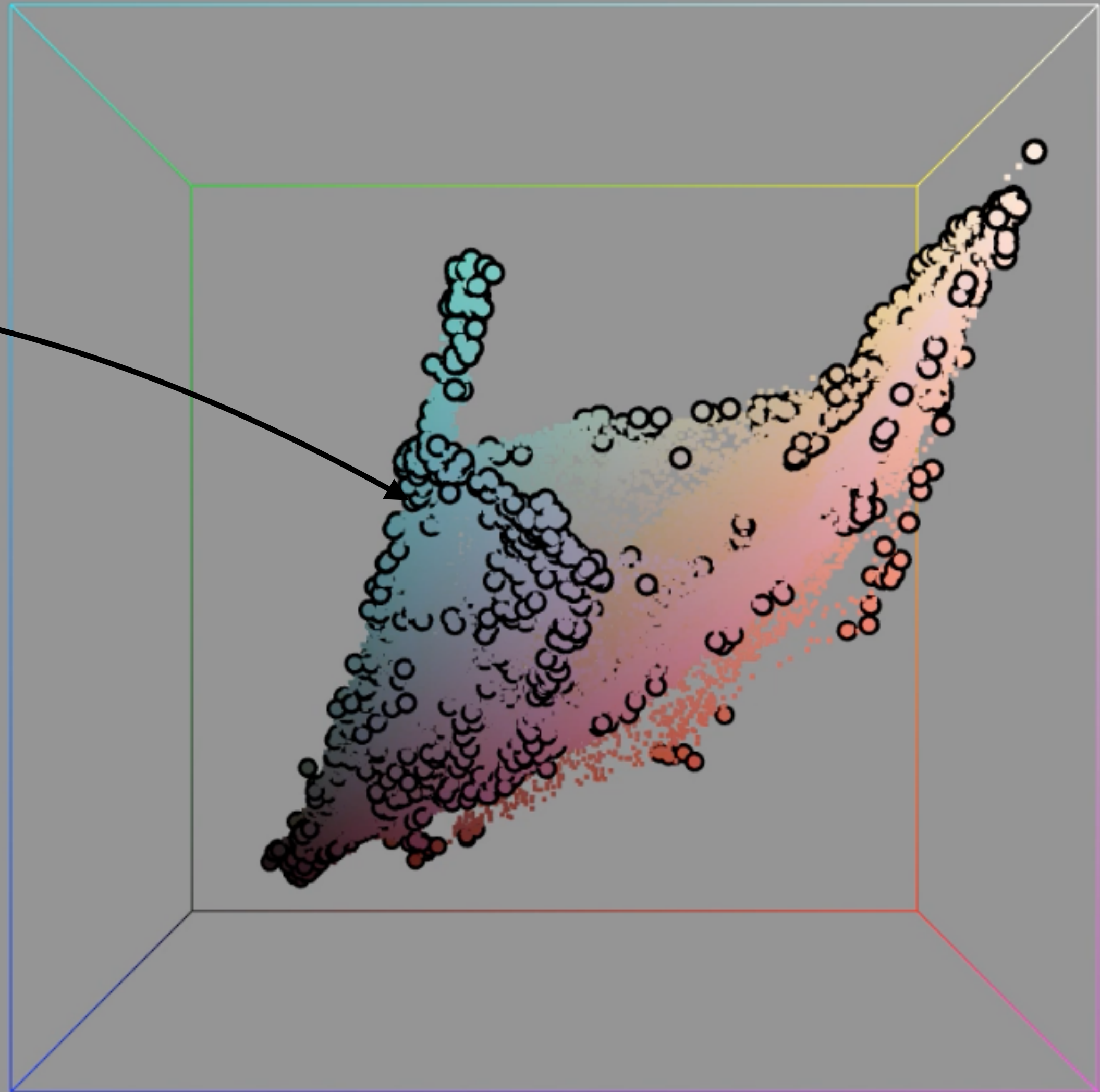
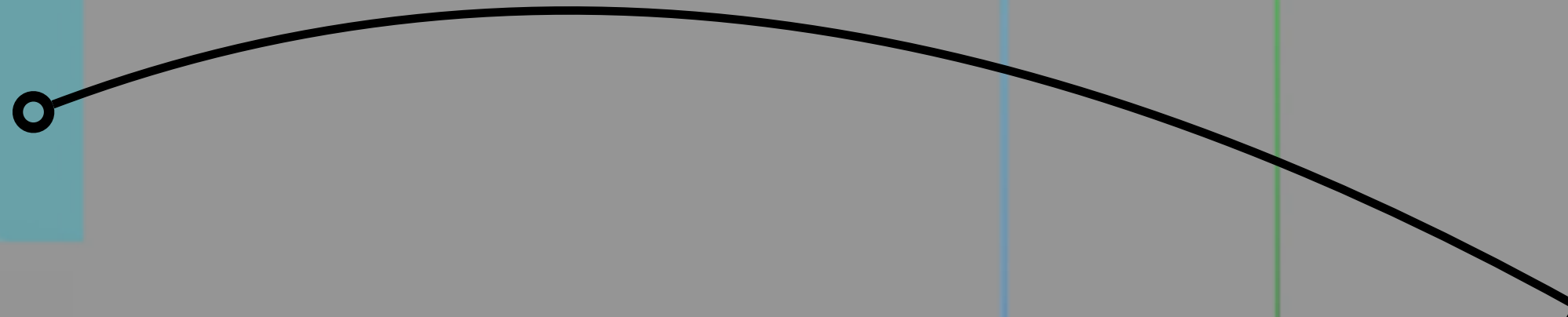
(R,G,B, x, y)

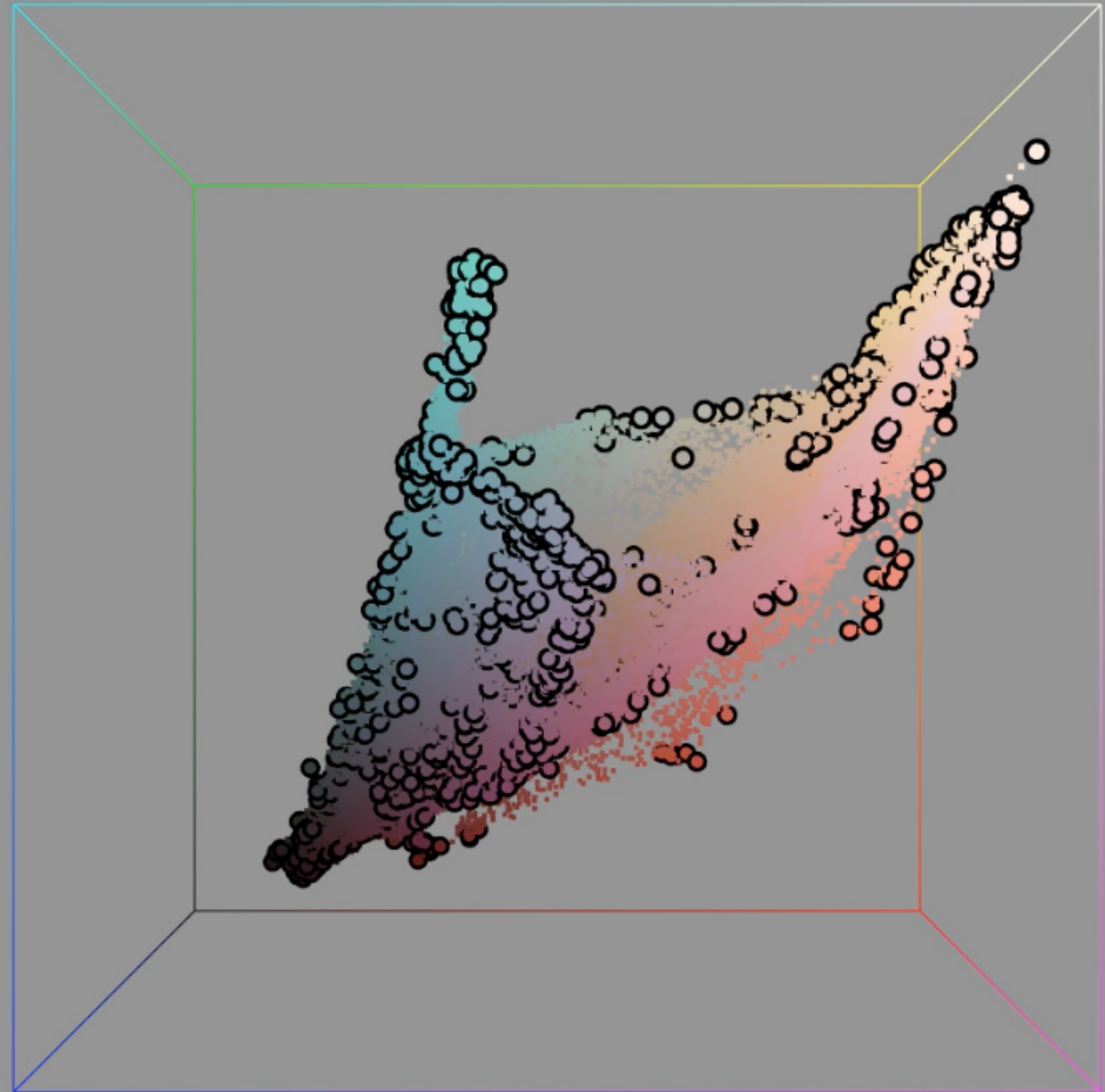




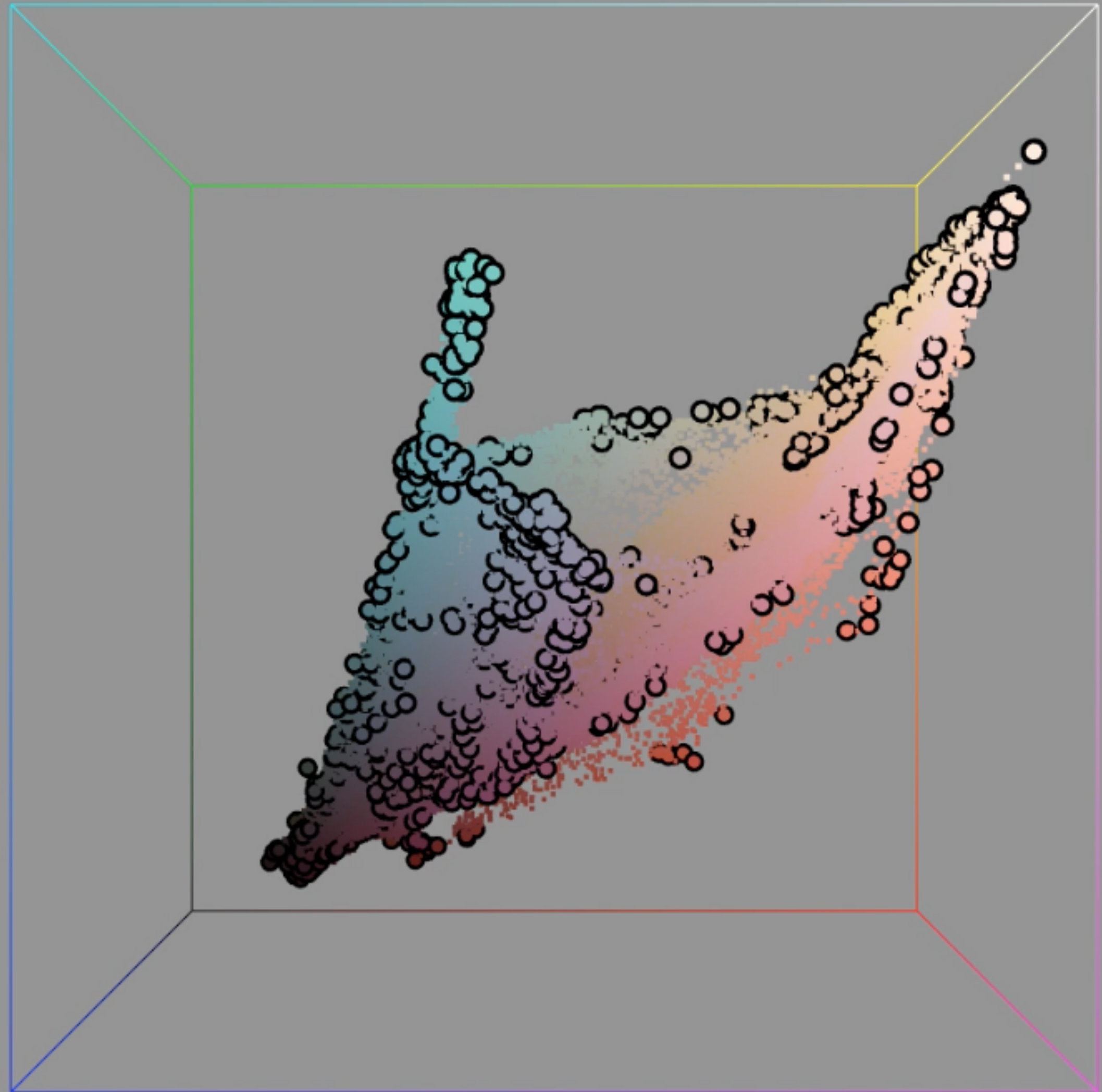
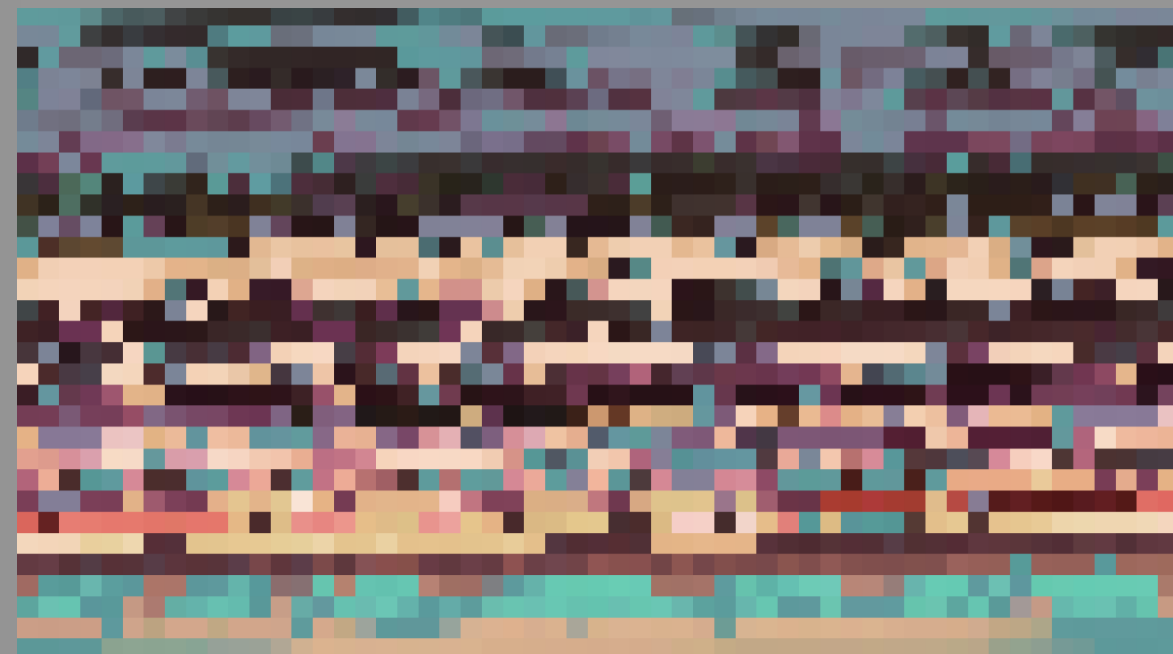


(R,G,B, x, y)





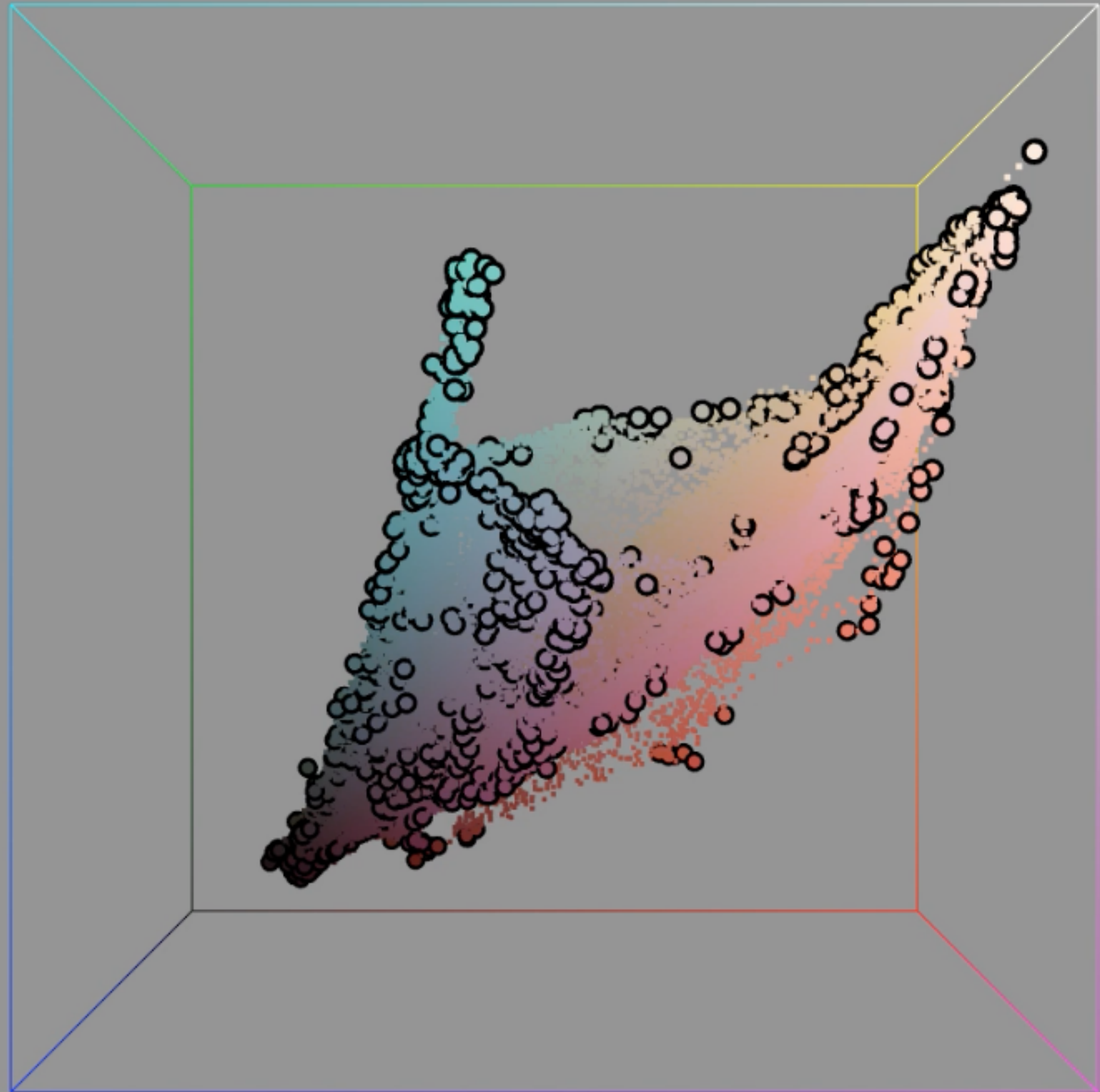








RGBXY palette  
(projected to RGB)



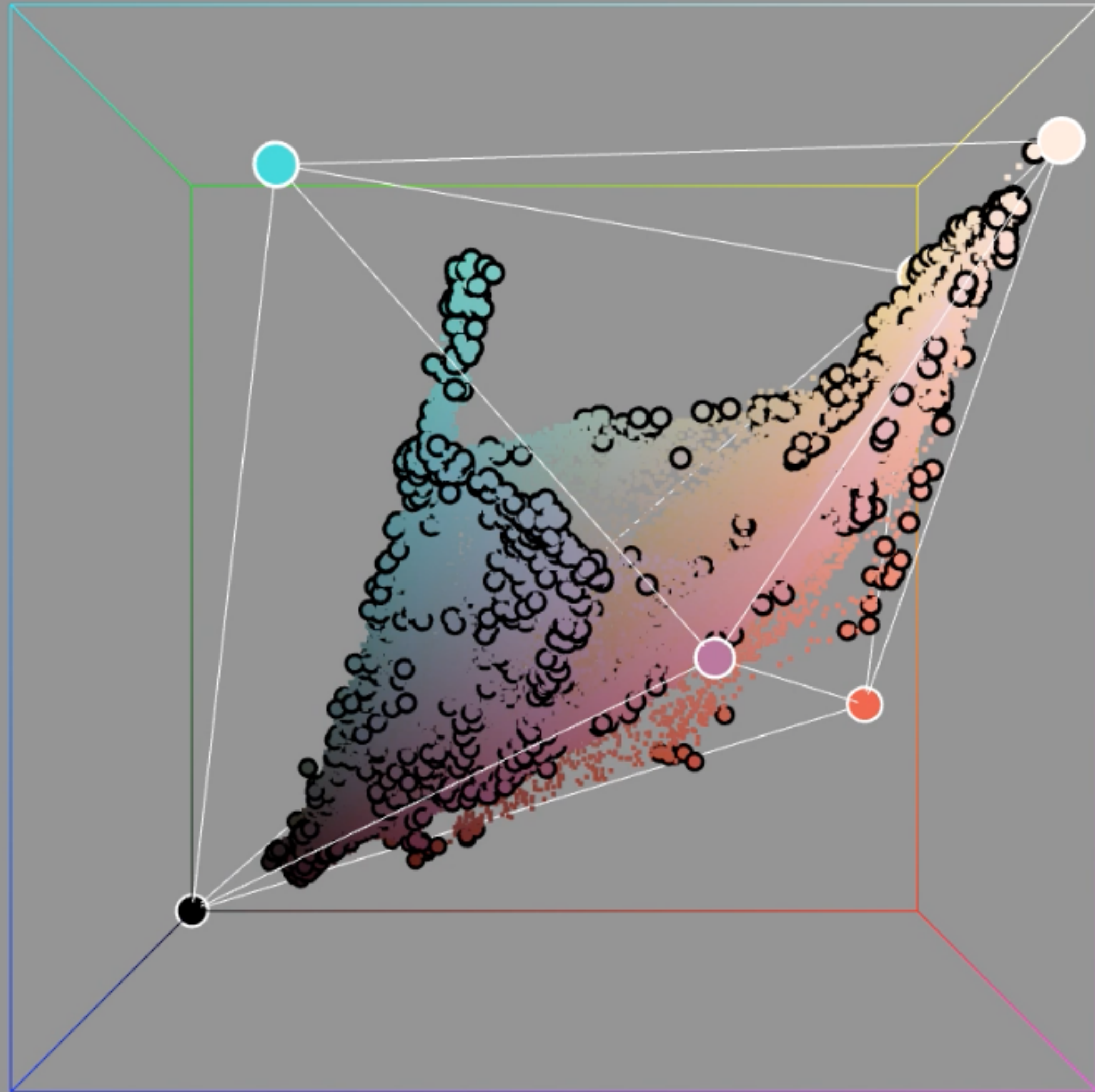




RGBXY palette  
(projected to RGB)



RGB palette



# Two-level decomposition





# Two-level decomposition

RGB palette



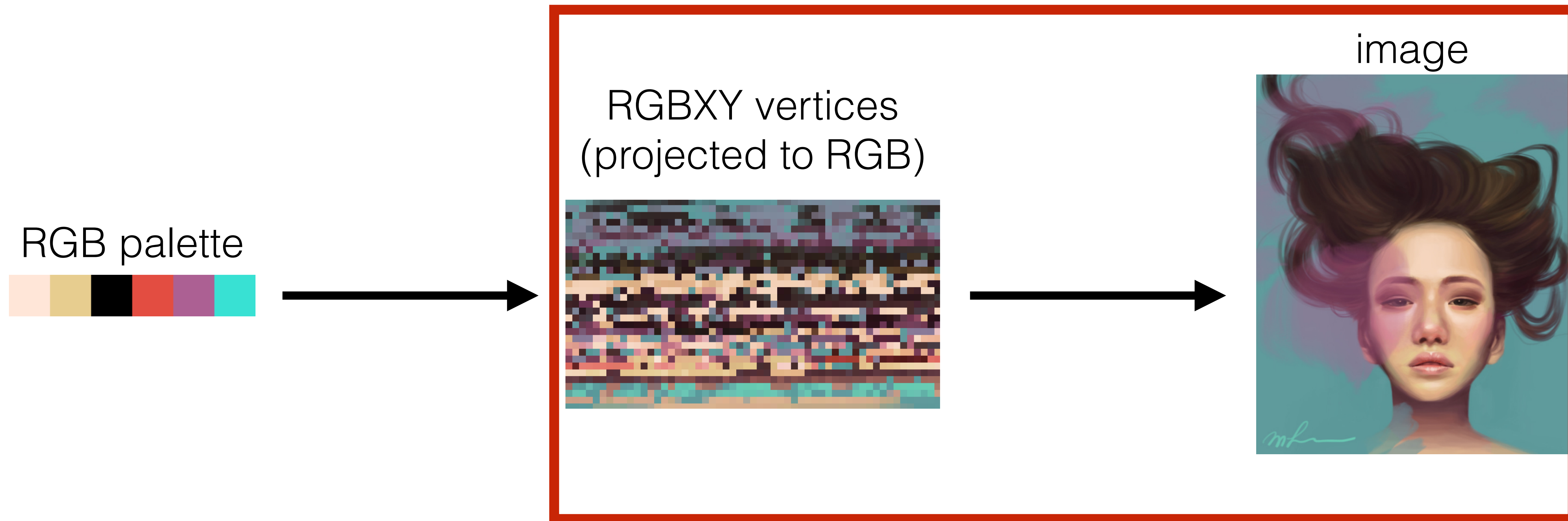
RGBXY vertices  
(projected to RGB)



image

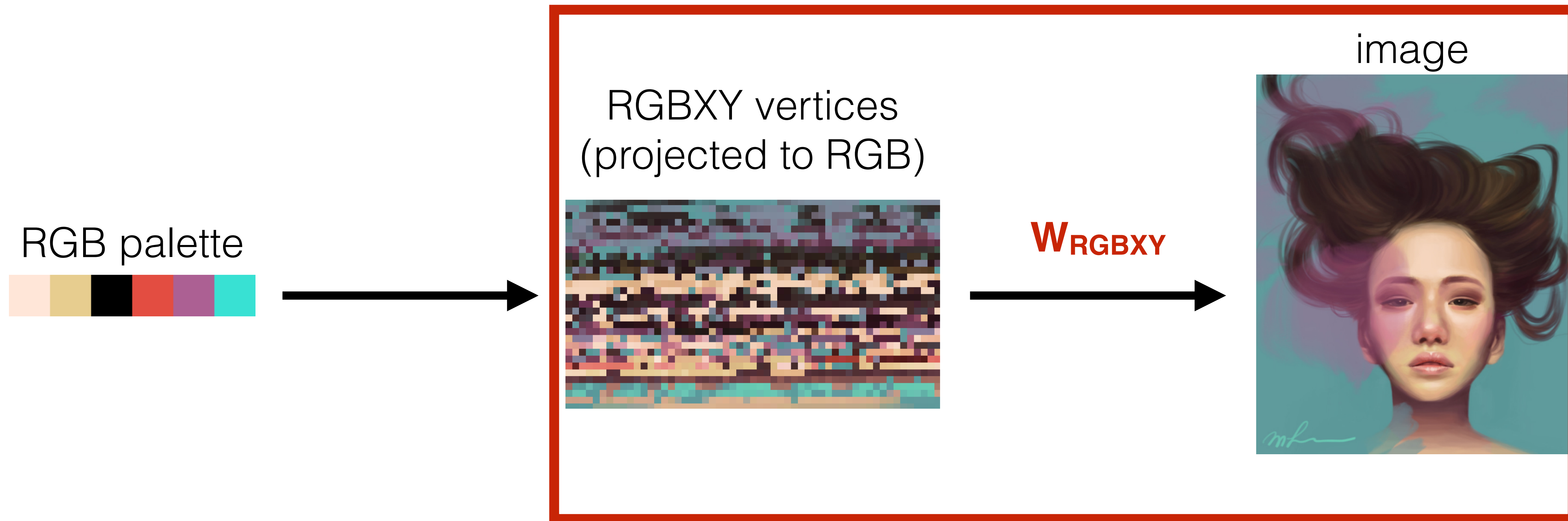


# Two-level decomposition

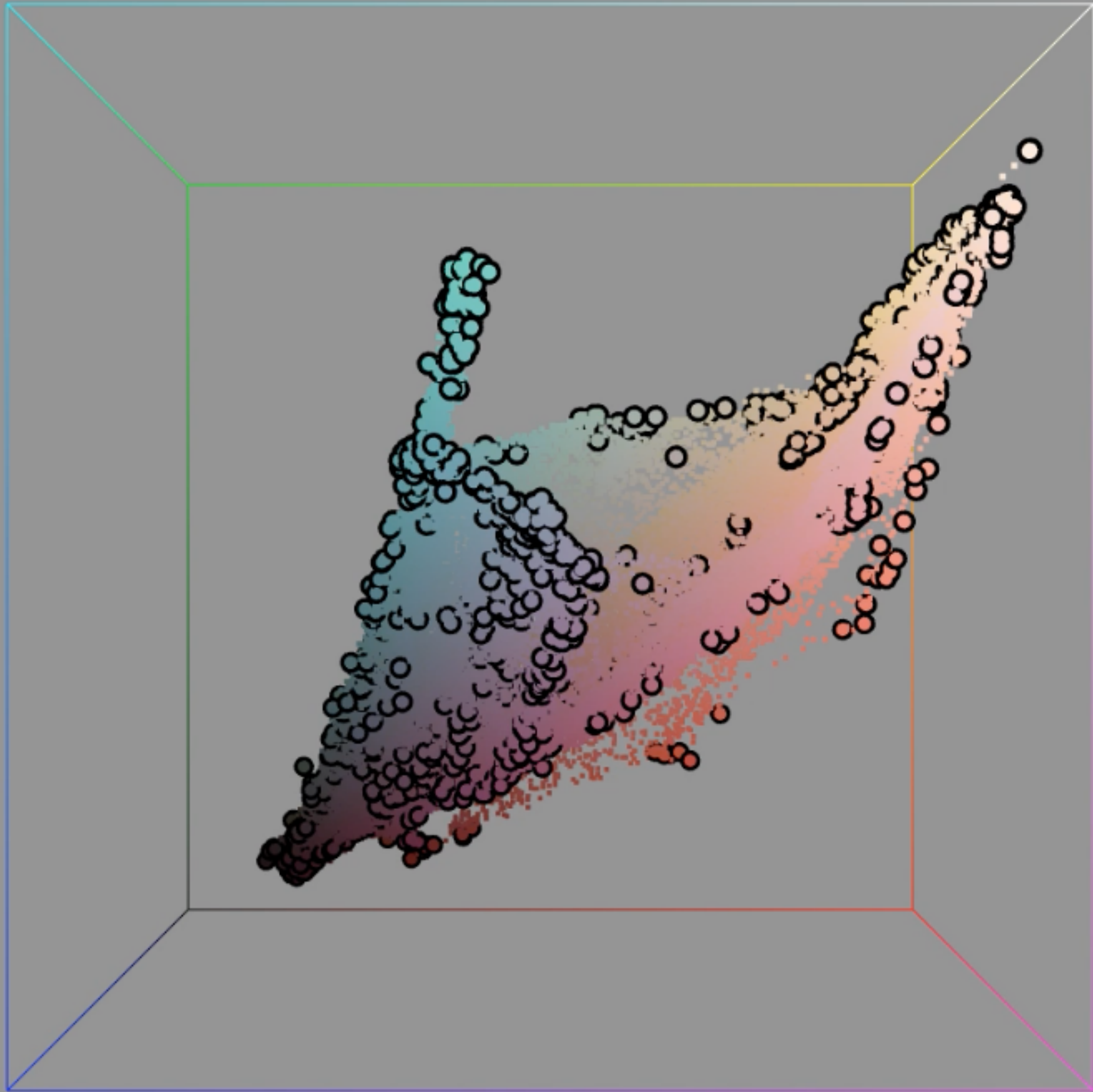




# Two-level decomposition



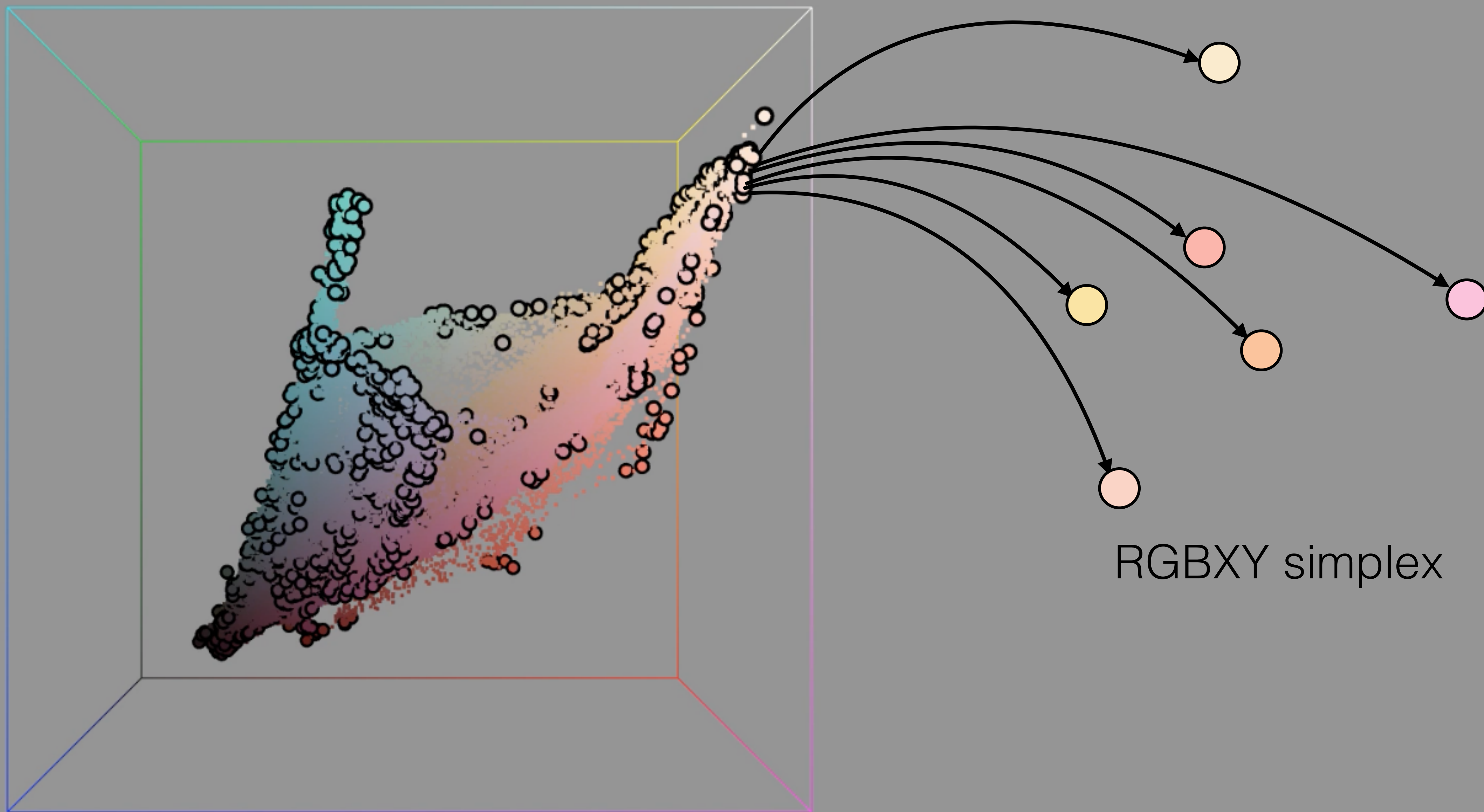
# Delaunay Tessellation in RGBXY space



Extract barycentric mixing weights  $\mathbf{W}_{\text{RGBXY}}$



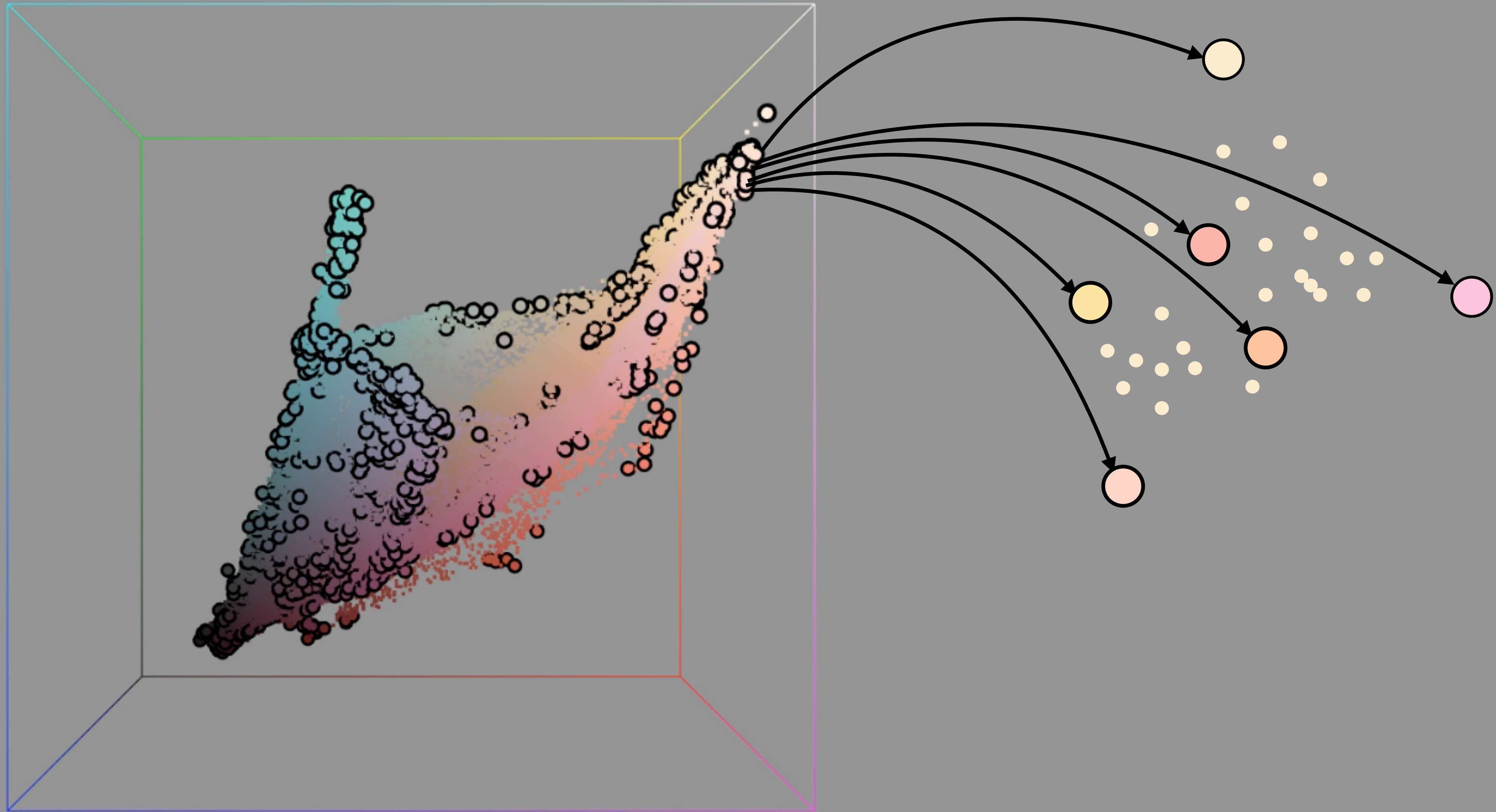
# Delaunay Tessellation in RGBXY space



RGBXY simplex

Extract barycentric mixing weights  $\mathbf{W}_{\text{RGBXY}}$

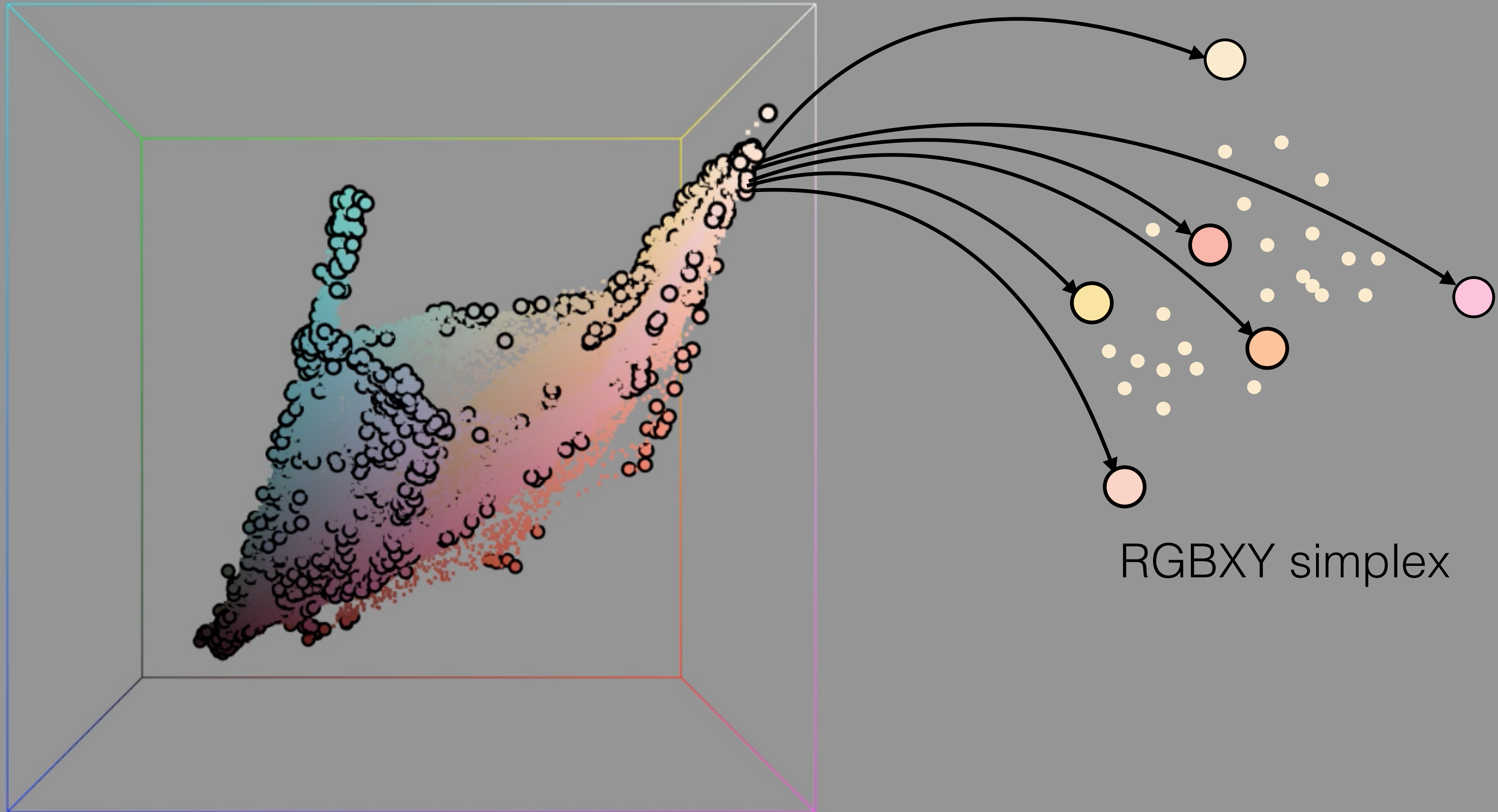
# Delaunay Tessellation in RGBXY space



Extract barycentric mixing weights  $\mathbf{W}_{\text{RGBXY}}$

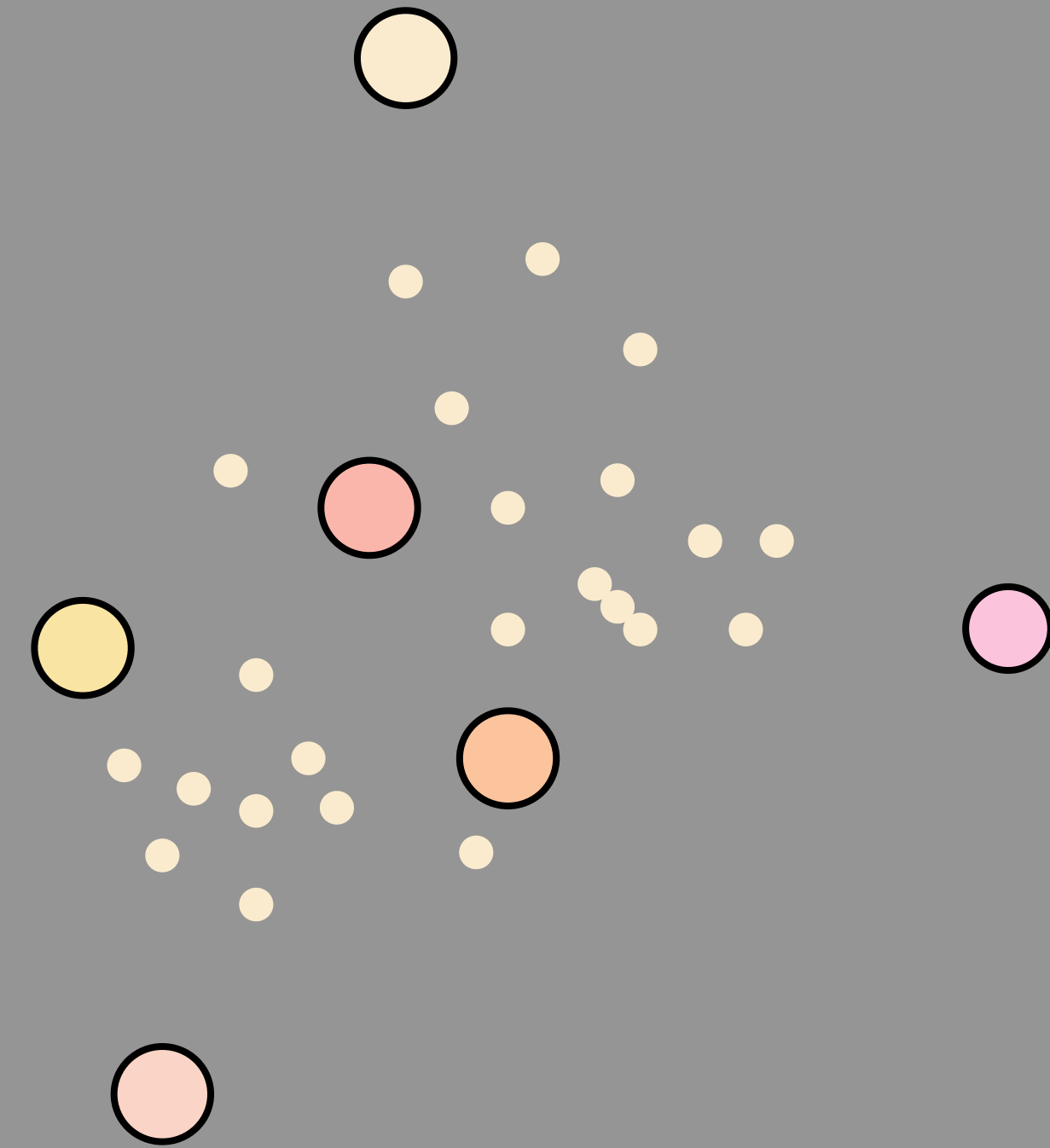
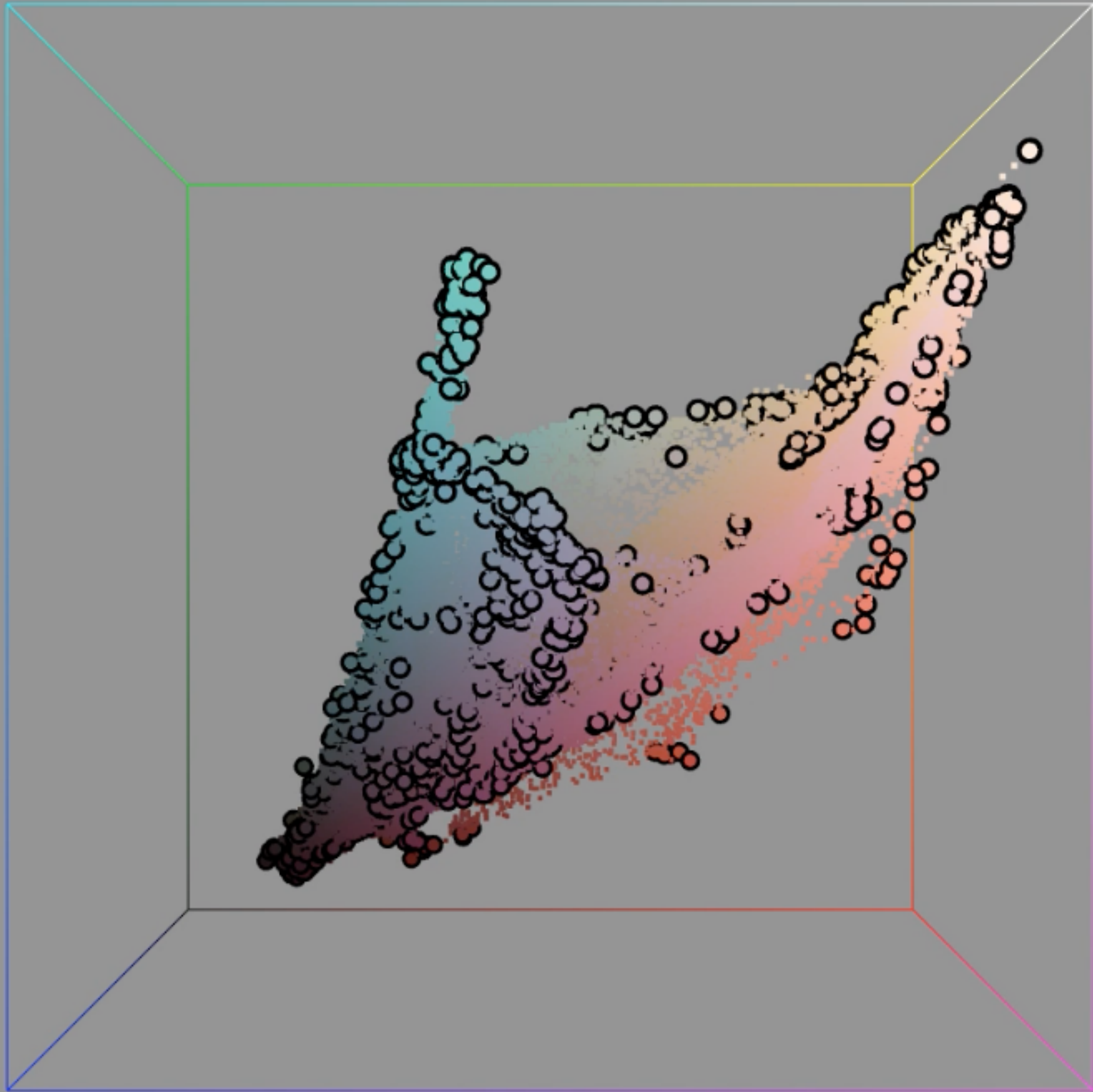


# Delaunay Tessellation in RGBXY space



Extract barycentric mixing weights  $\mathbf{W}_{\text{RGBXY}}$

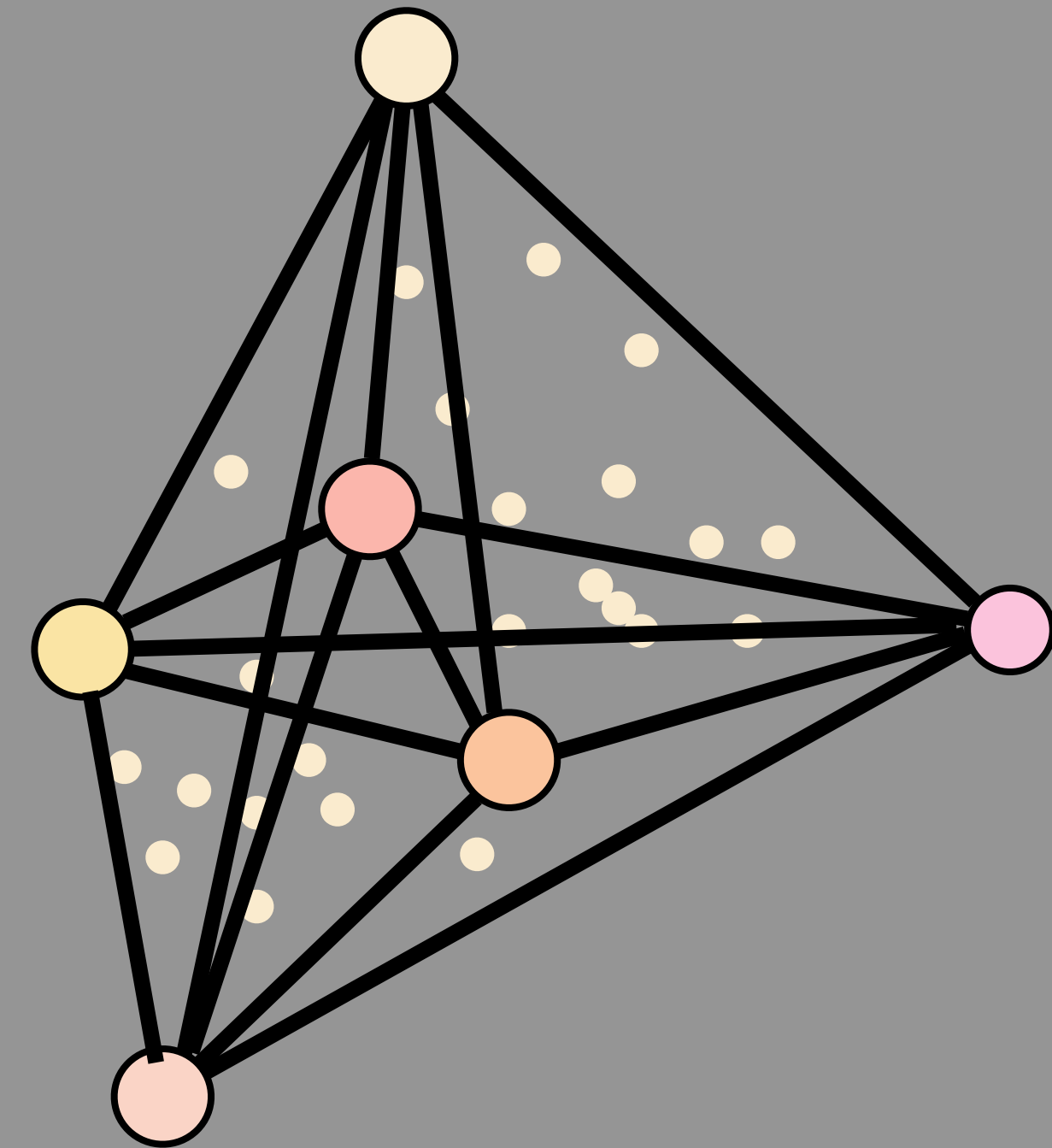
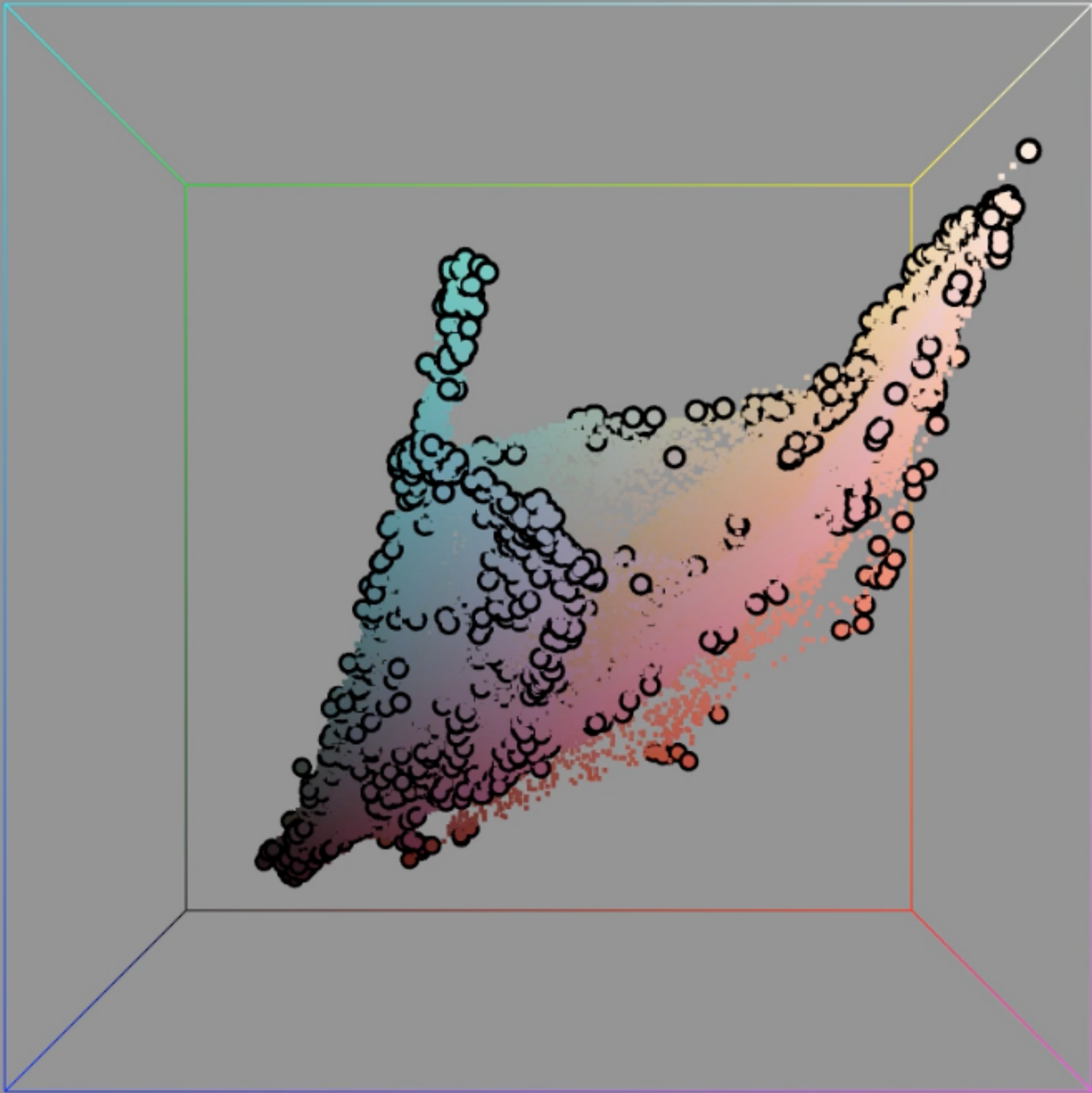
# Delaunay Tessellation in RGBXY space



Extract barycentric mixing weights  $\mathbf{W}_{\text{RGBXY}}$



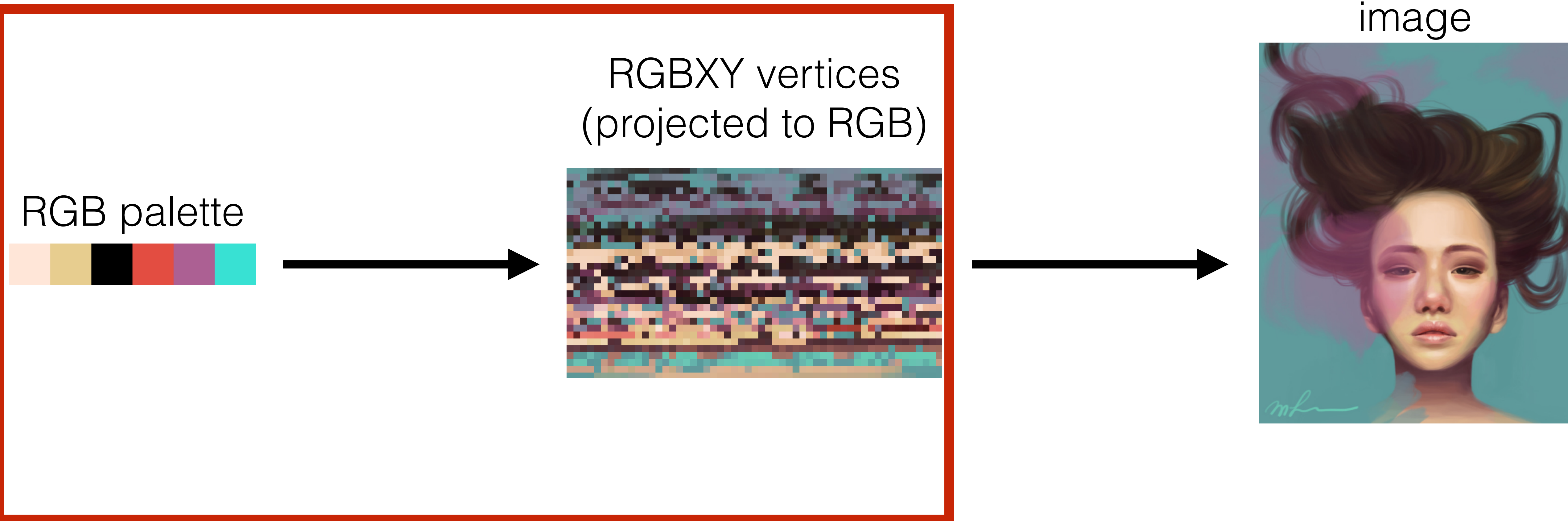
# Delaunay Tessellation in RGBXY space



RGBXY simplex

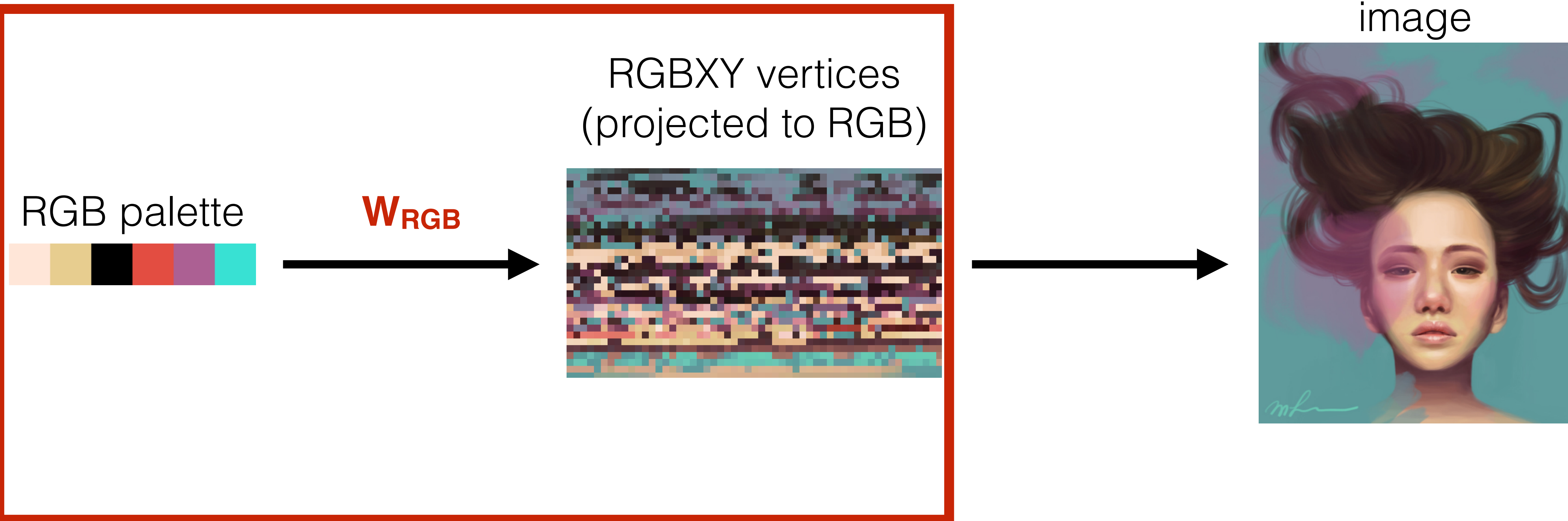
Extract barycentric mixing weights  $\mathbf{W}_{\text{RGBXY}}$

# Two-level decomposition

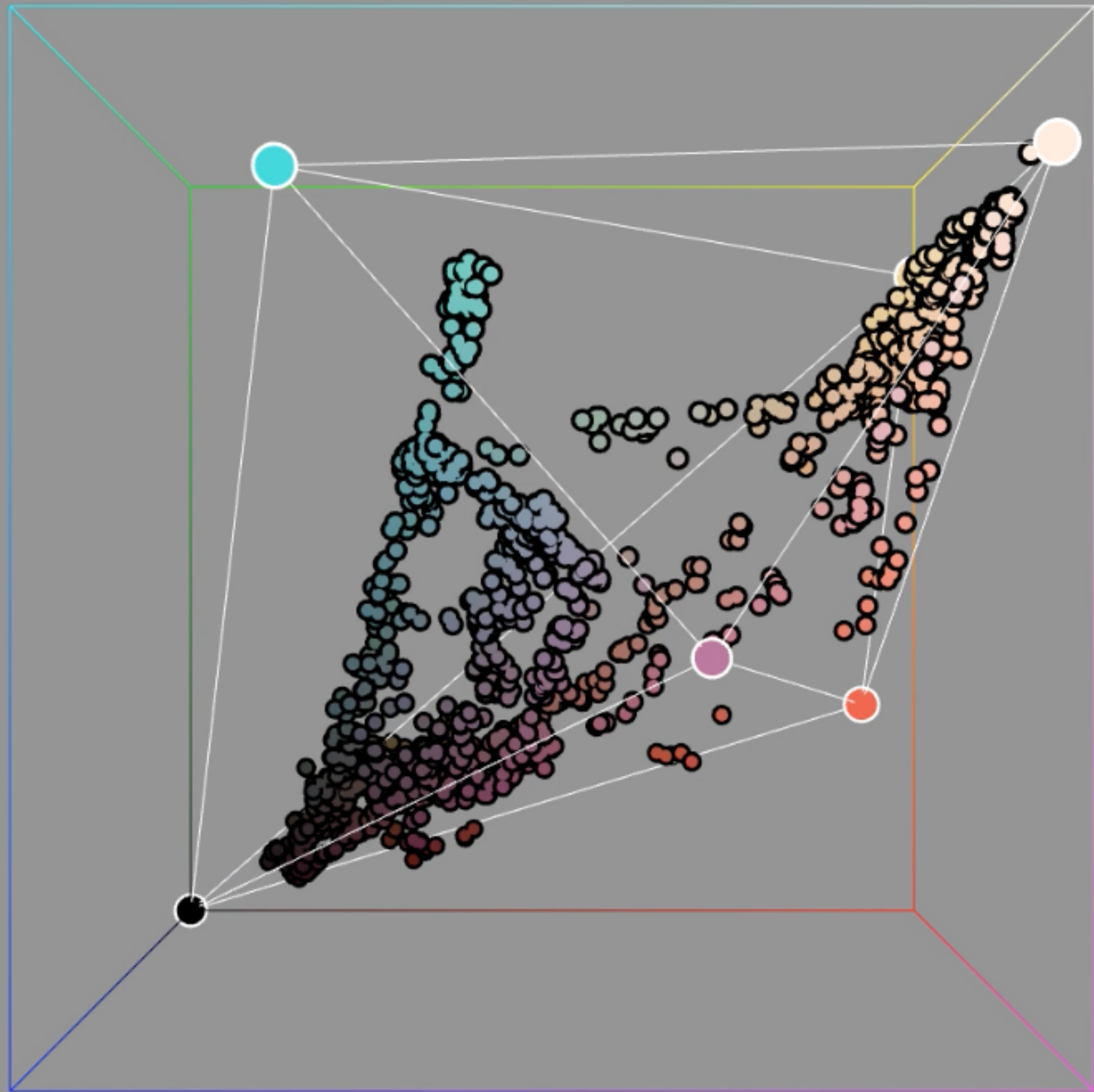




# Two-level decomposition



# Tessellation in RGB space

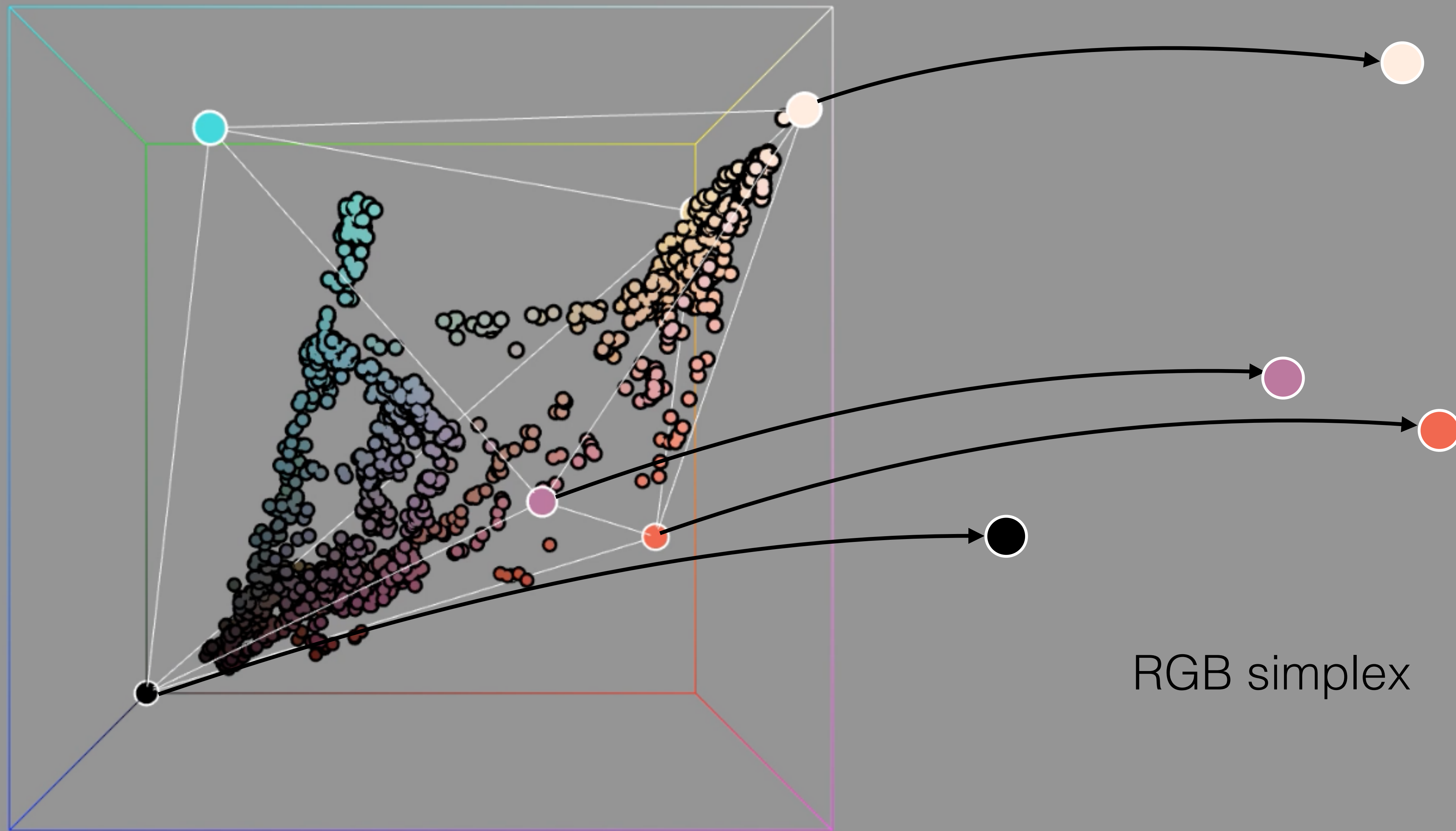


RGB simplex

Extract barycentric mixing weights  $\mathbf{W}_{\text{RGB}}$

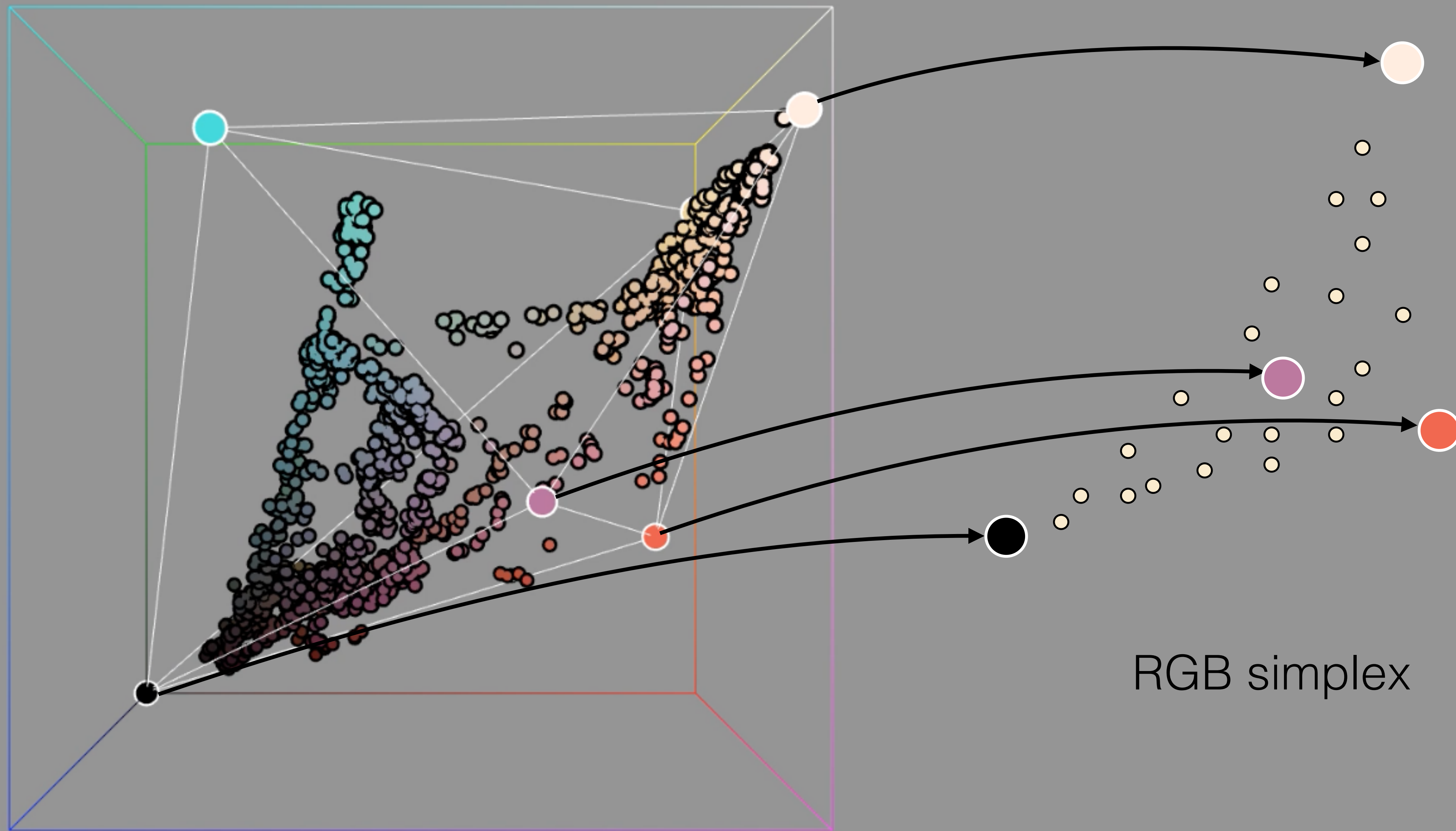


# Tessellation in RGB space



Extract barycentric mixing weights  $\mathbf{W}_{\text{RGB}}$

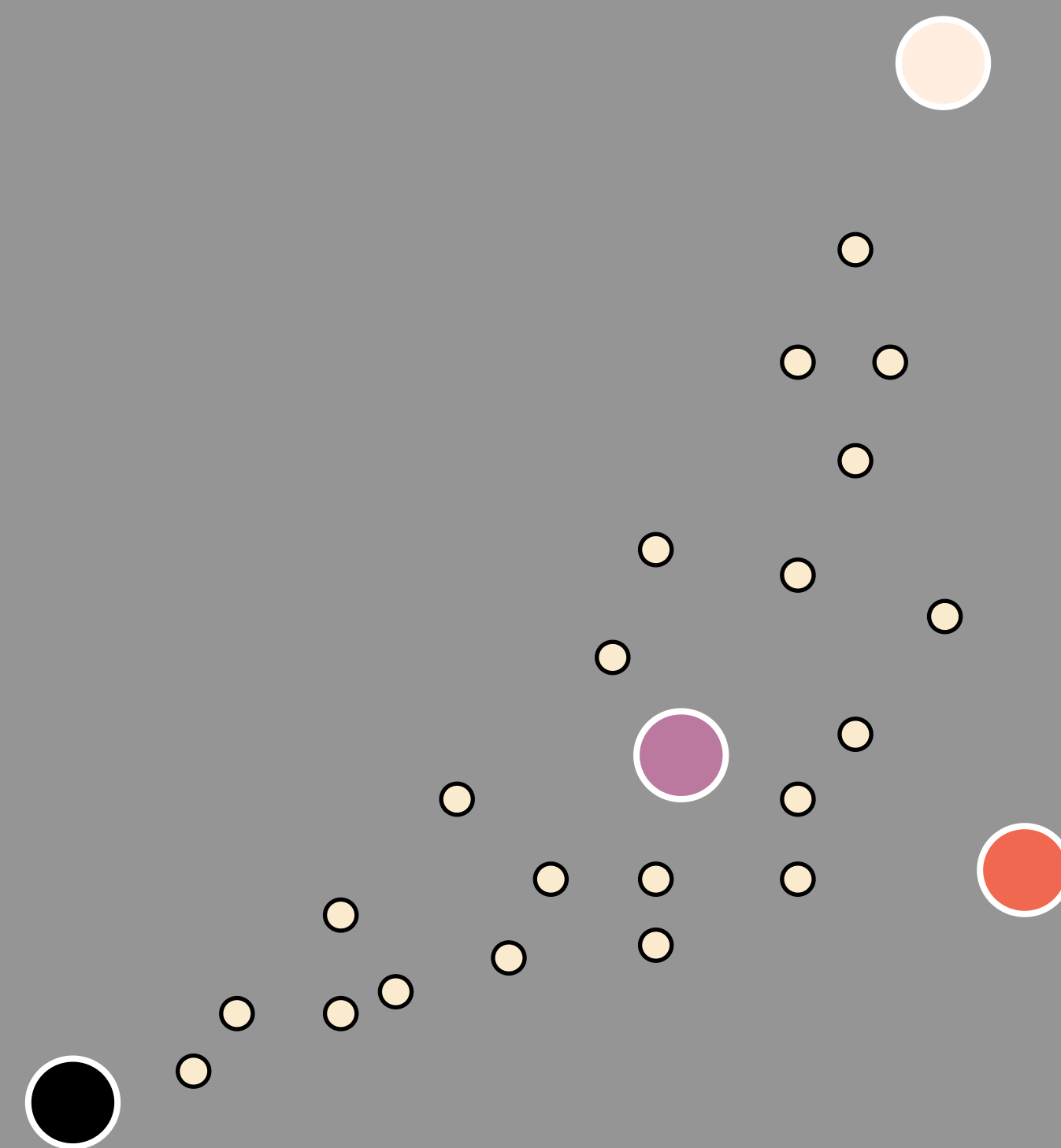
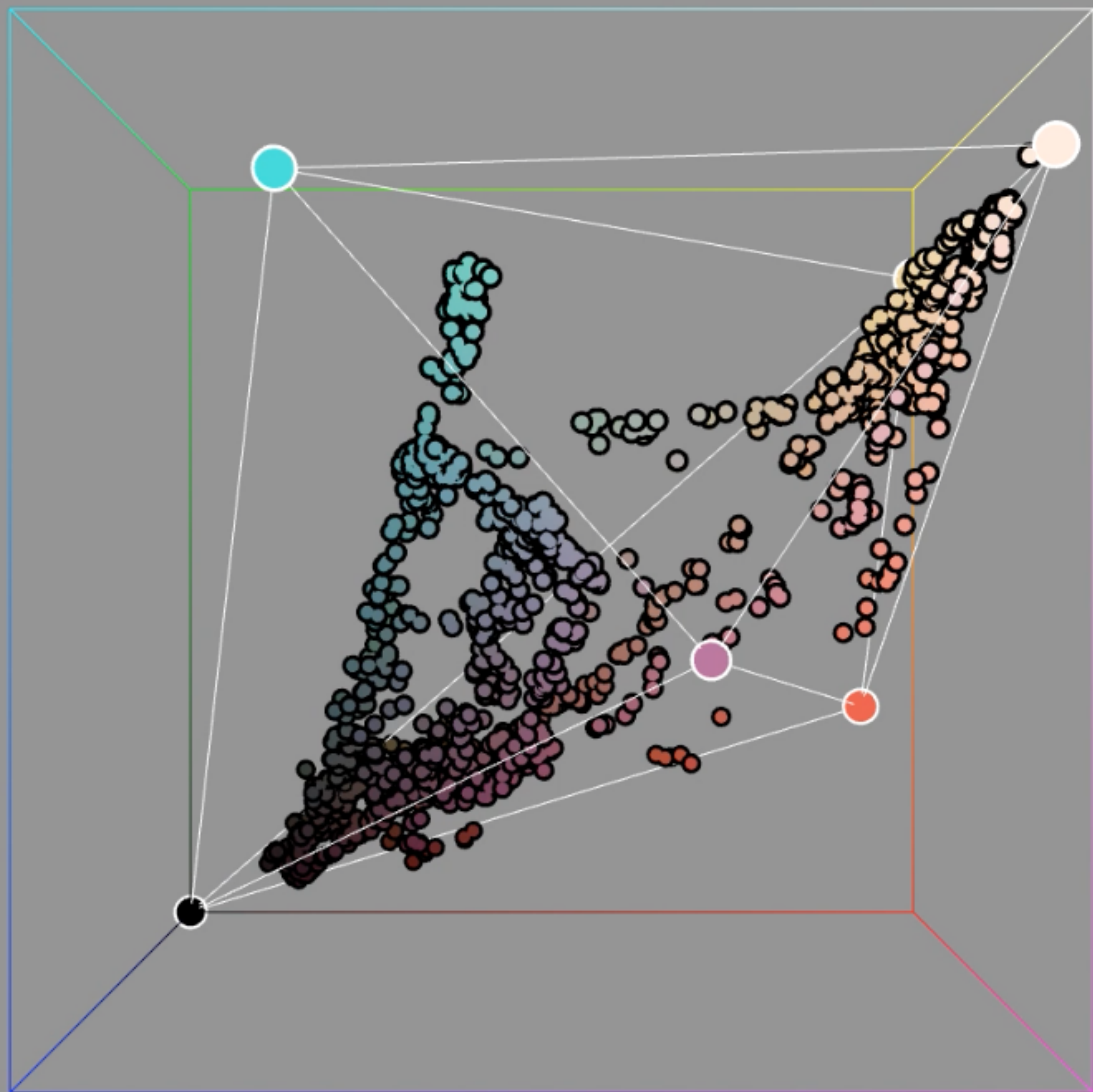
# Tessellation in RGB space



Extract barycentric mixing weights  $\mathbf{W}_{\text{RGB}}$



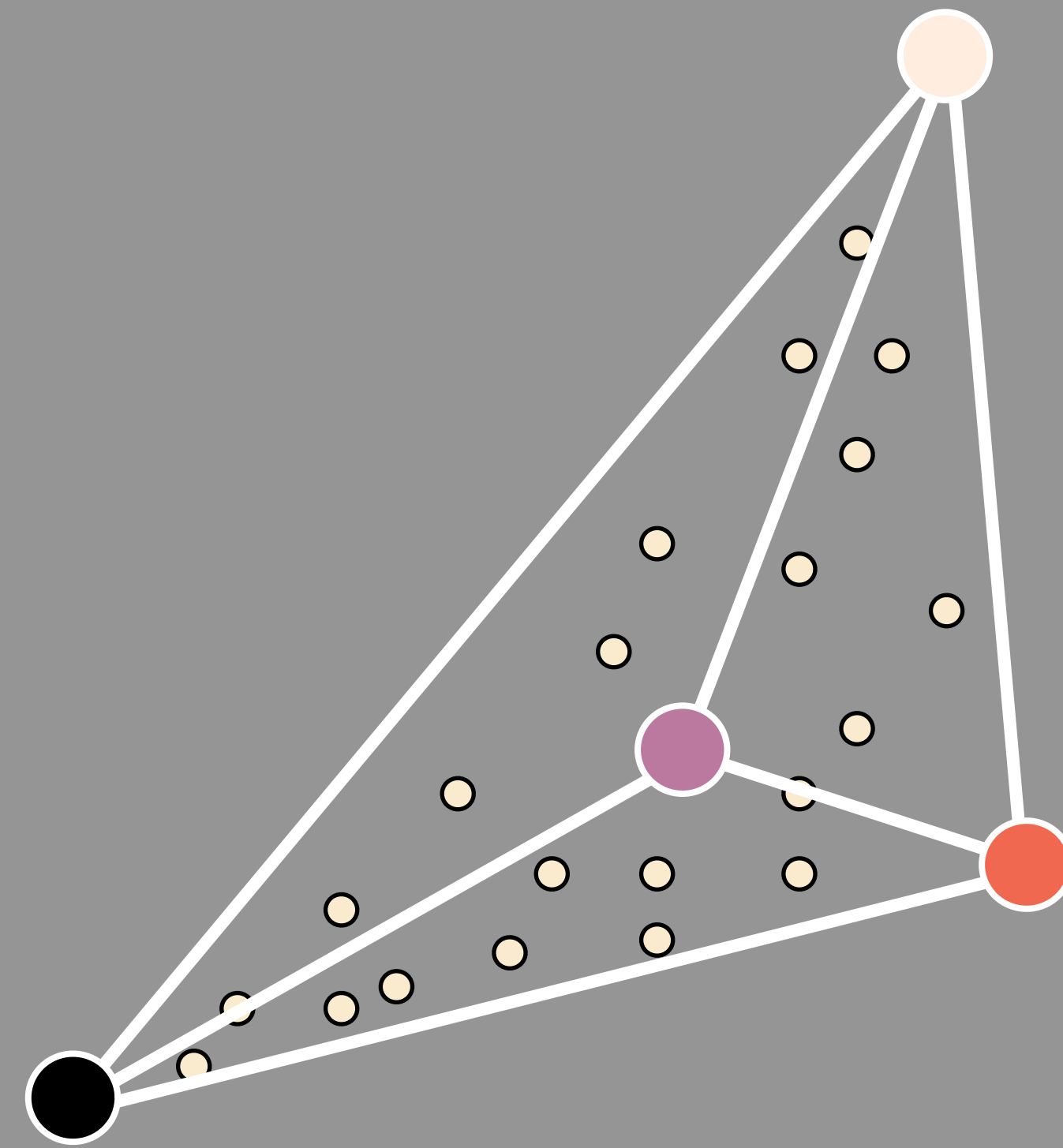
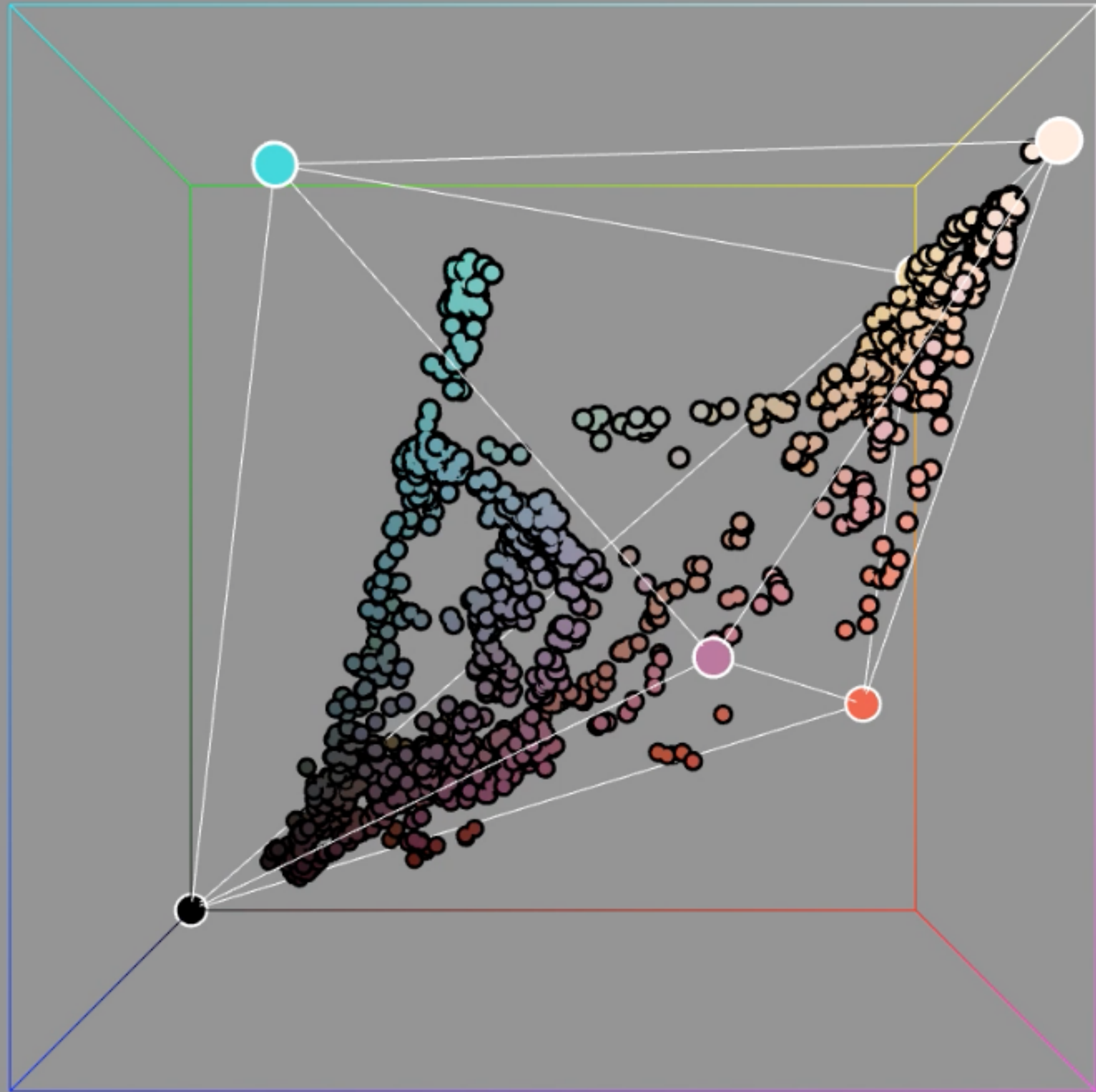
# Tessellation in RGB space



RGB simplex

Extract barycentric mixing weights  $\mathbf{W}_{\text{RGB}}$

# Tessellation in RGB space

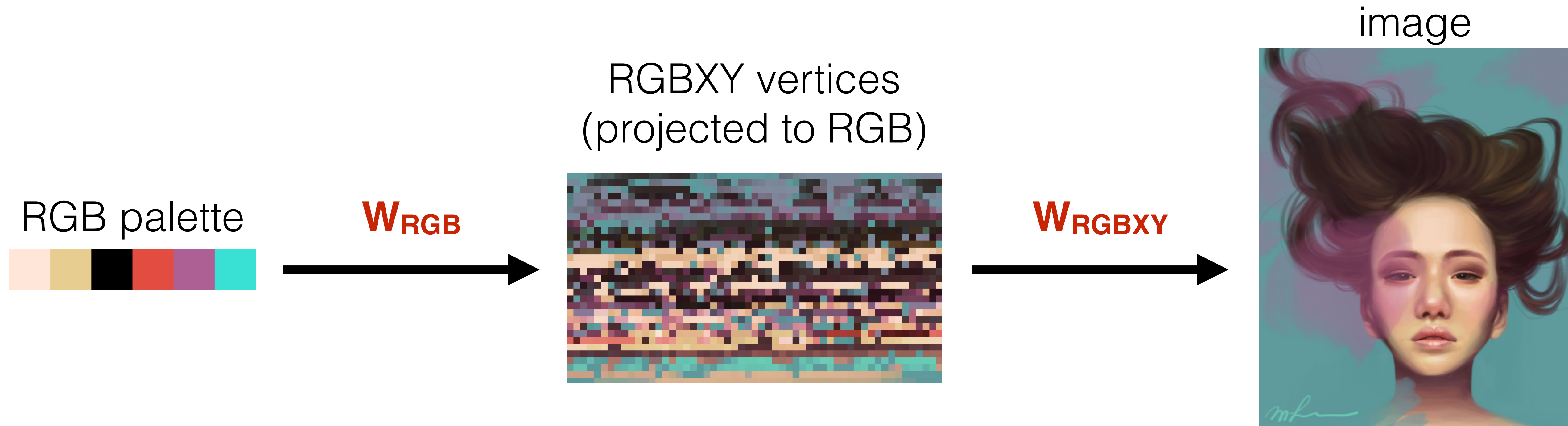


RGB simplex

Extract barycentric mixing weights  $\mathbf{W}_{\text{RGB}}$



# Two-level decomposition



# Two-level decomposition

image



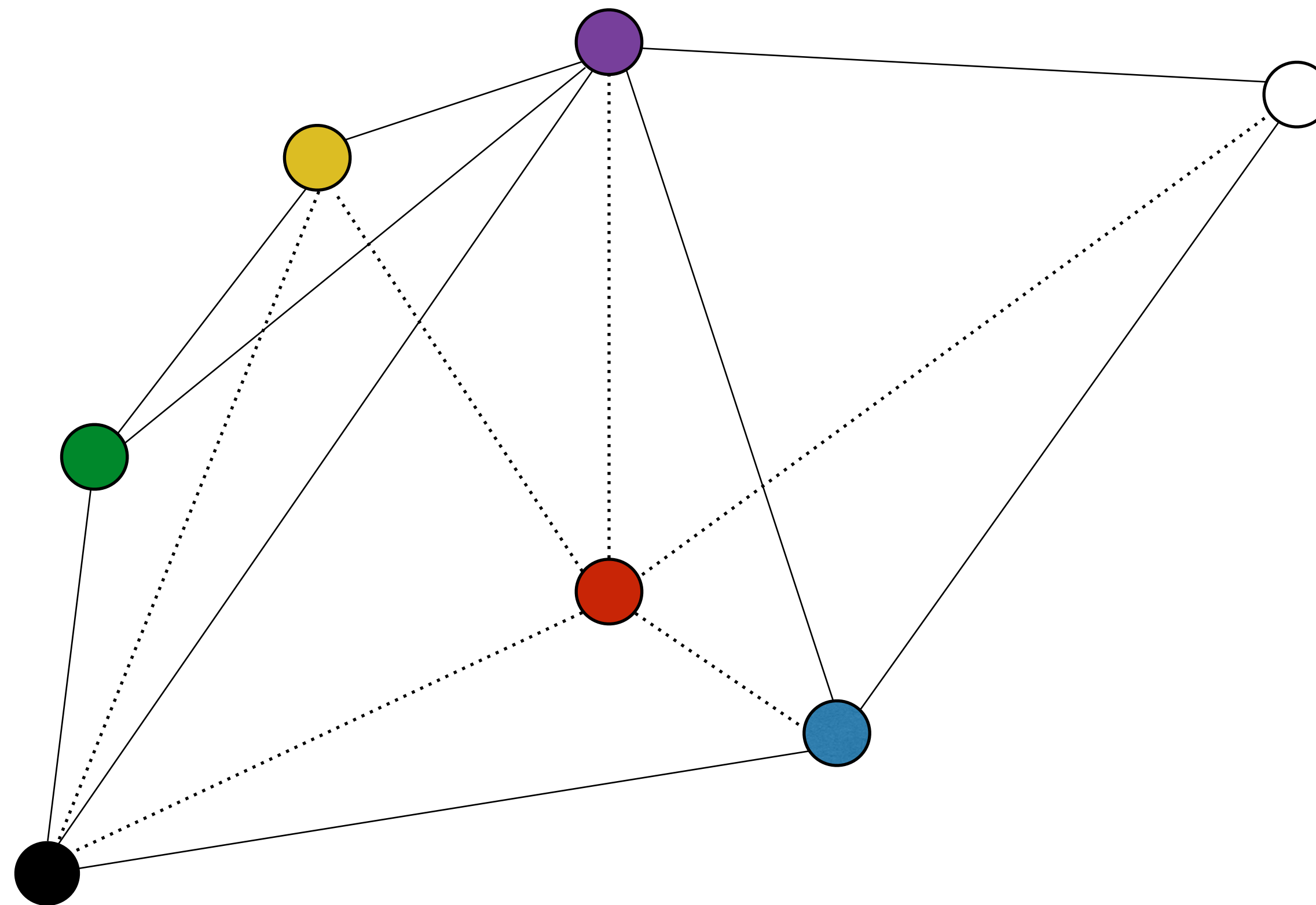
RGB palette



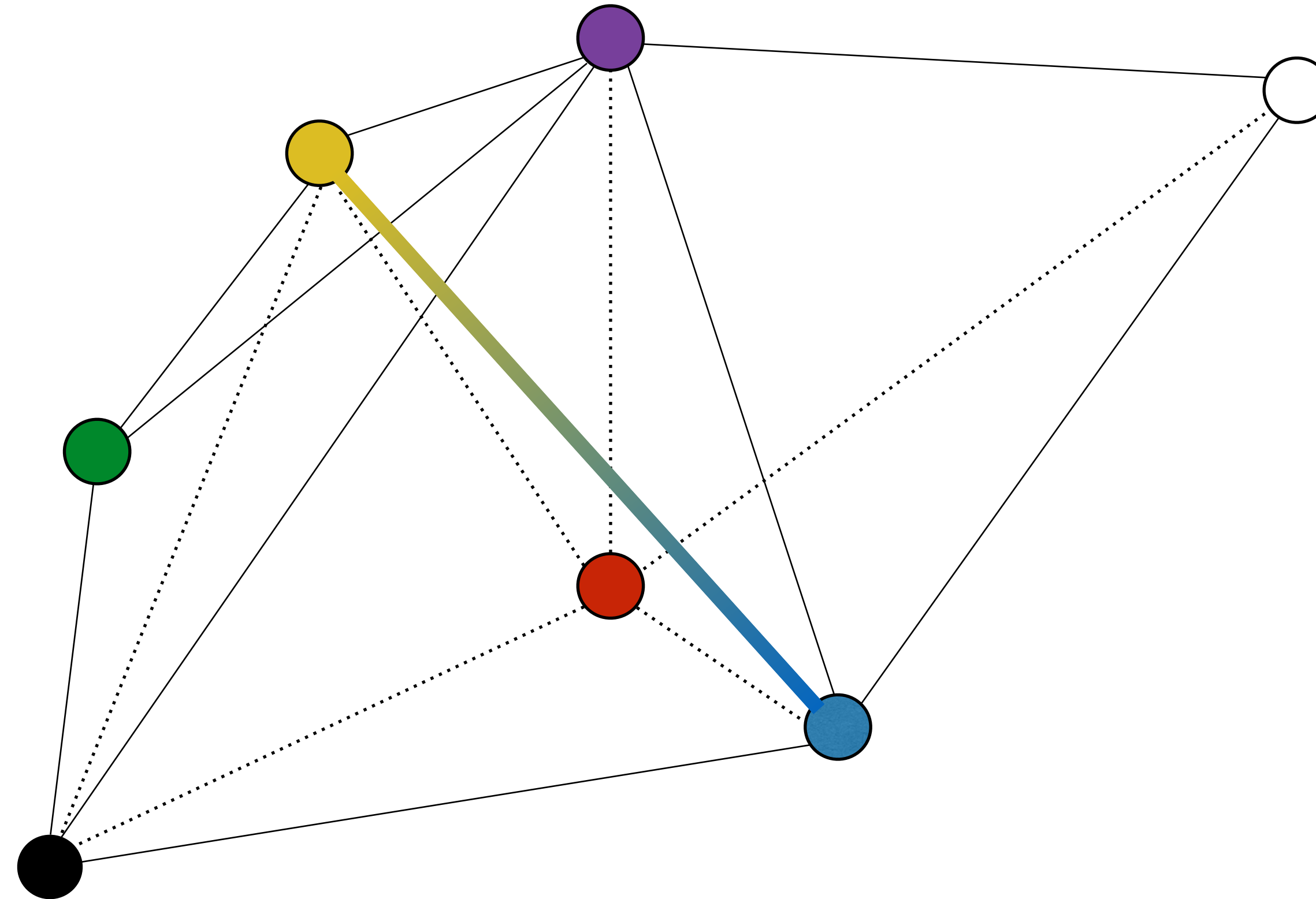
$$\mathbf{W} = \mathbf{W}_{\text{RGB}} * \mathbf{W}_{\text{RGBXY}}$$




# Tessellation in RGB space



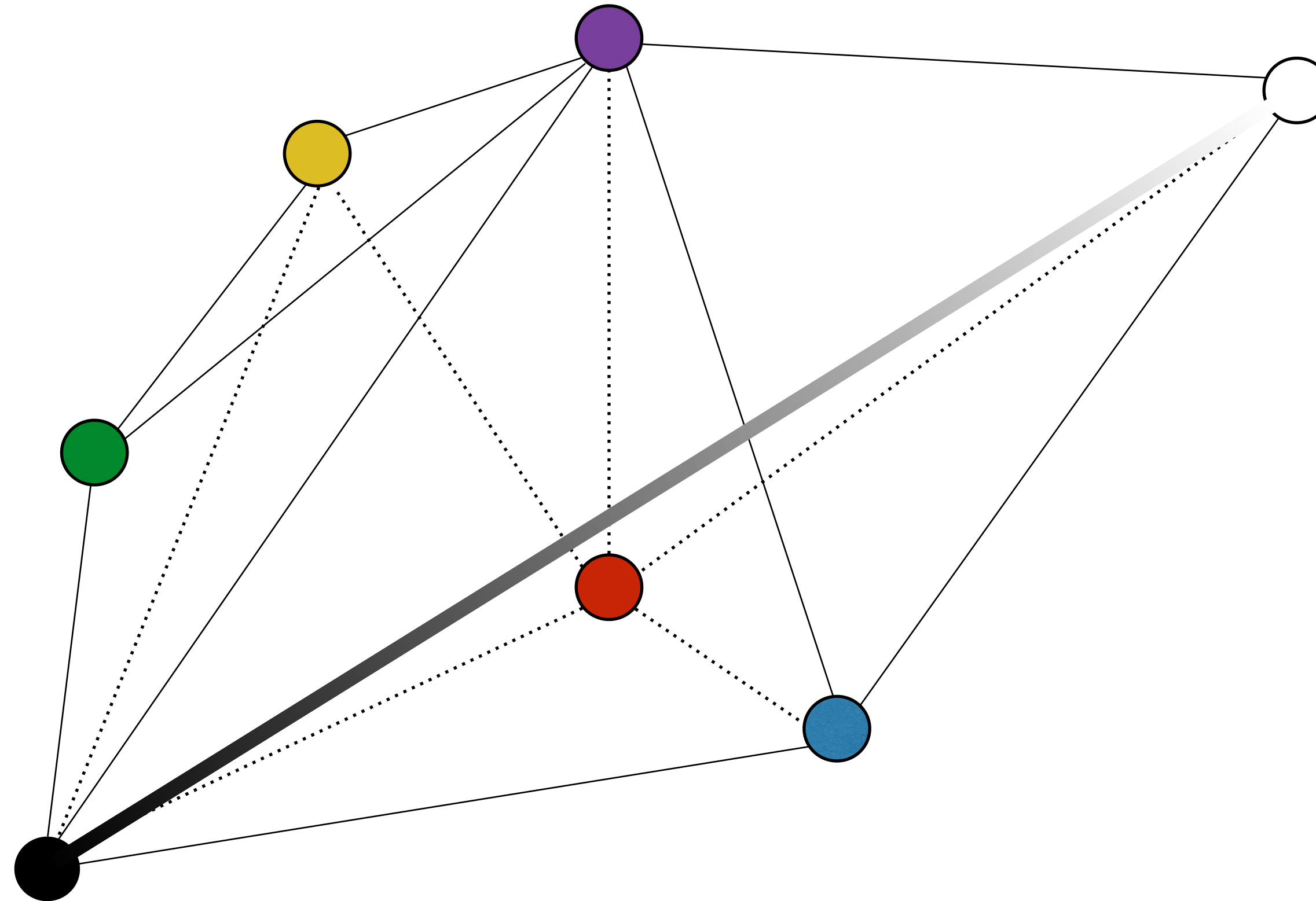
# Tessellation in RGB space



**Delaunay tessellation**

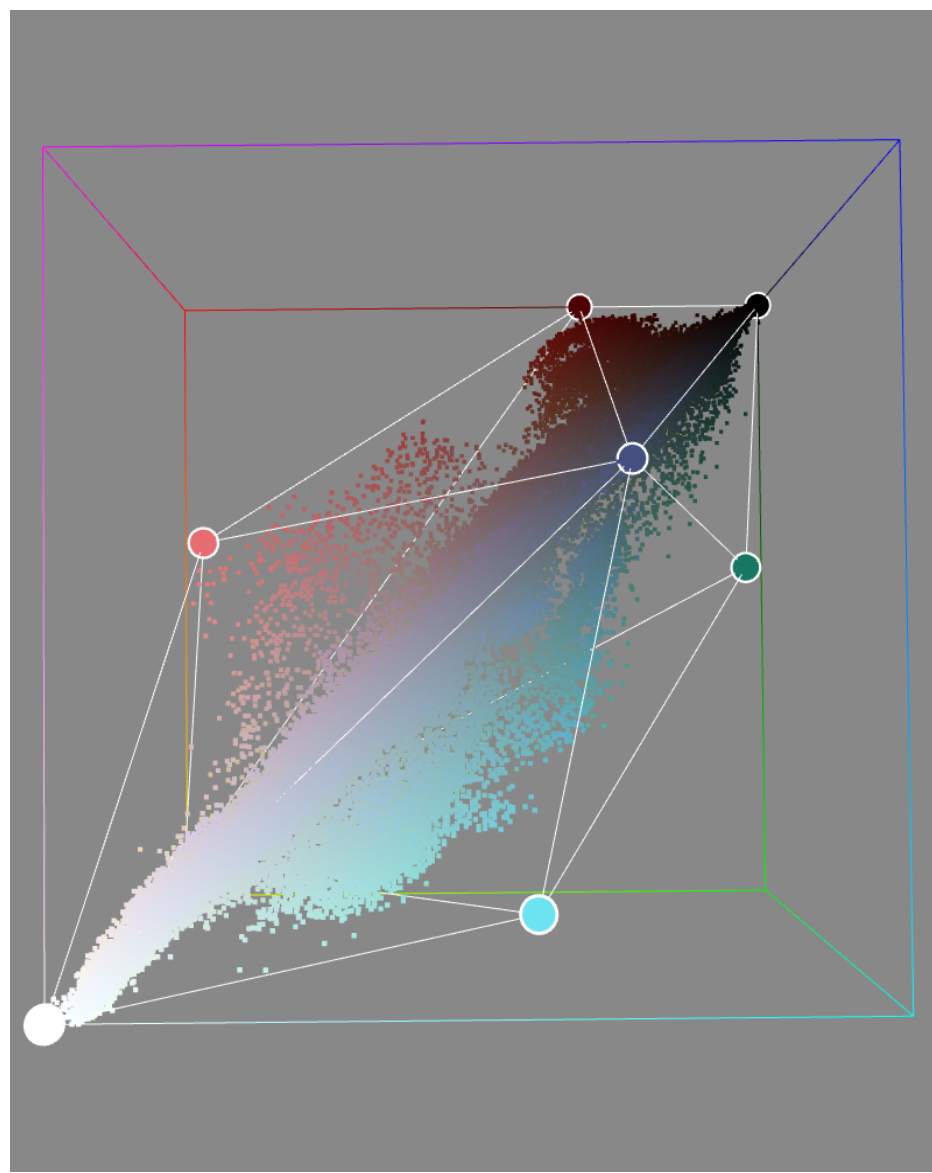
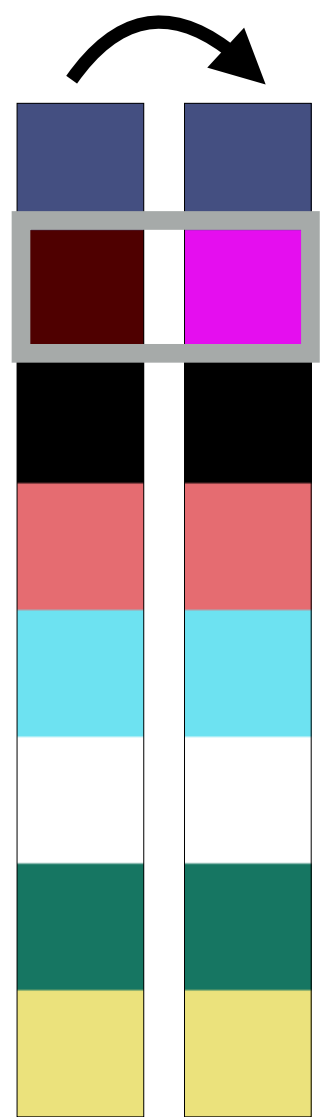
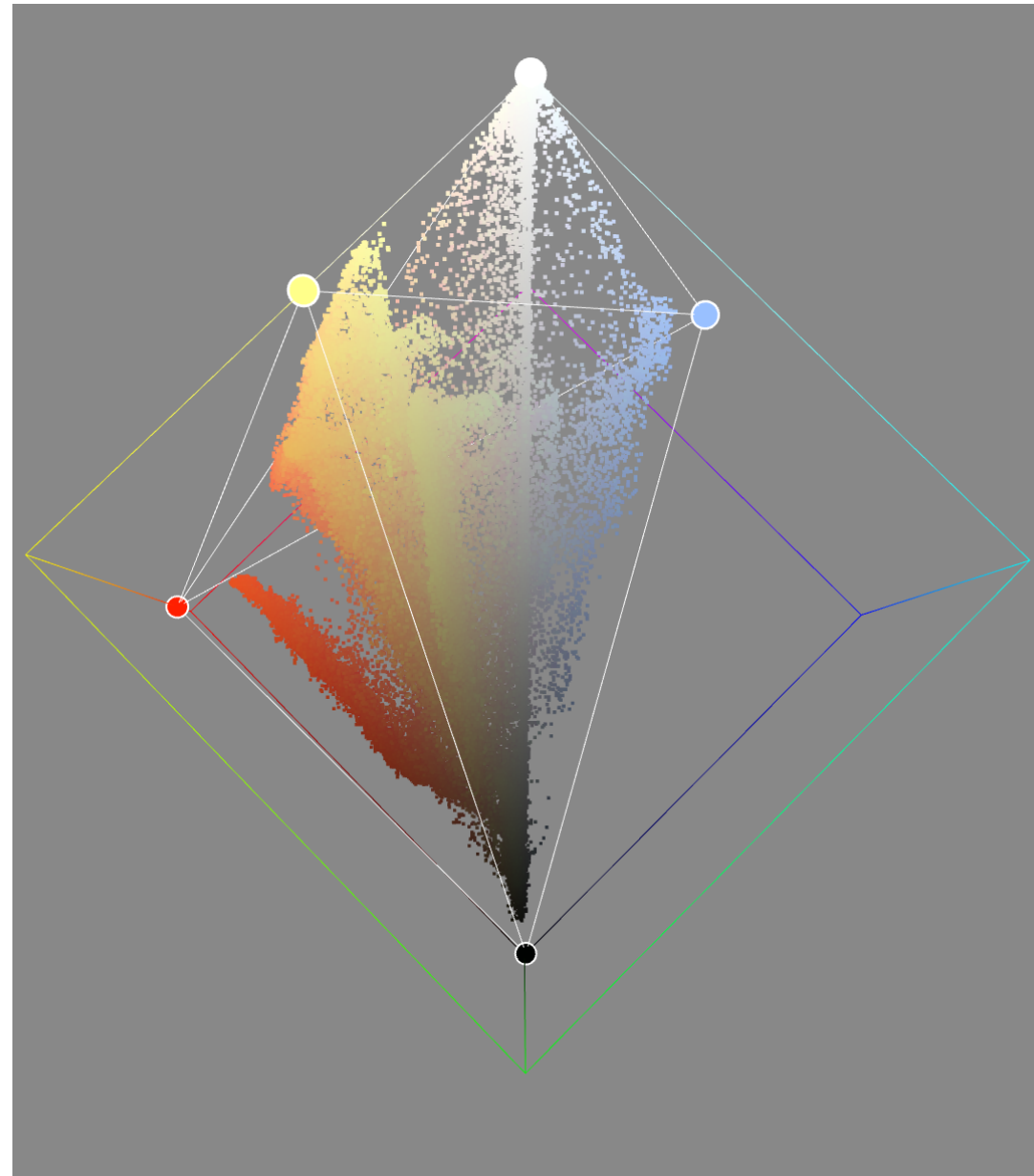
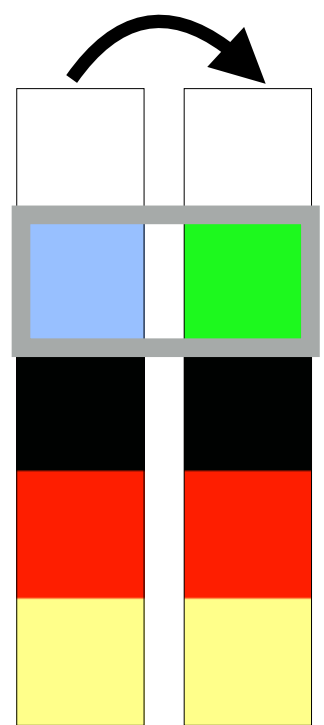


# Tessellation in RGB space



**Star tessellation**





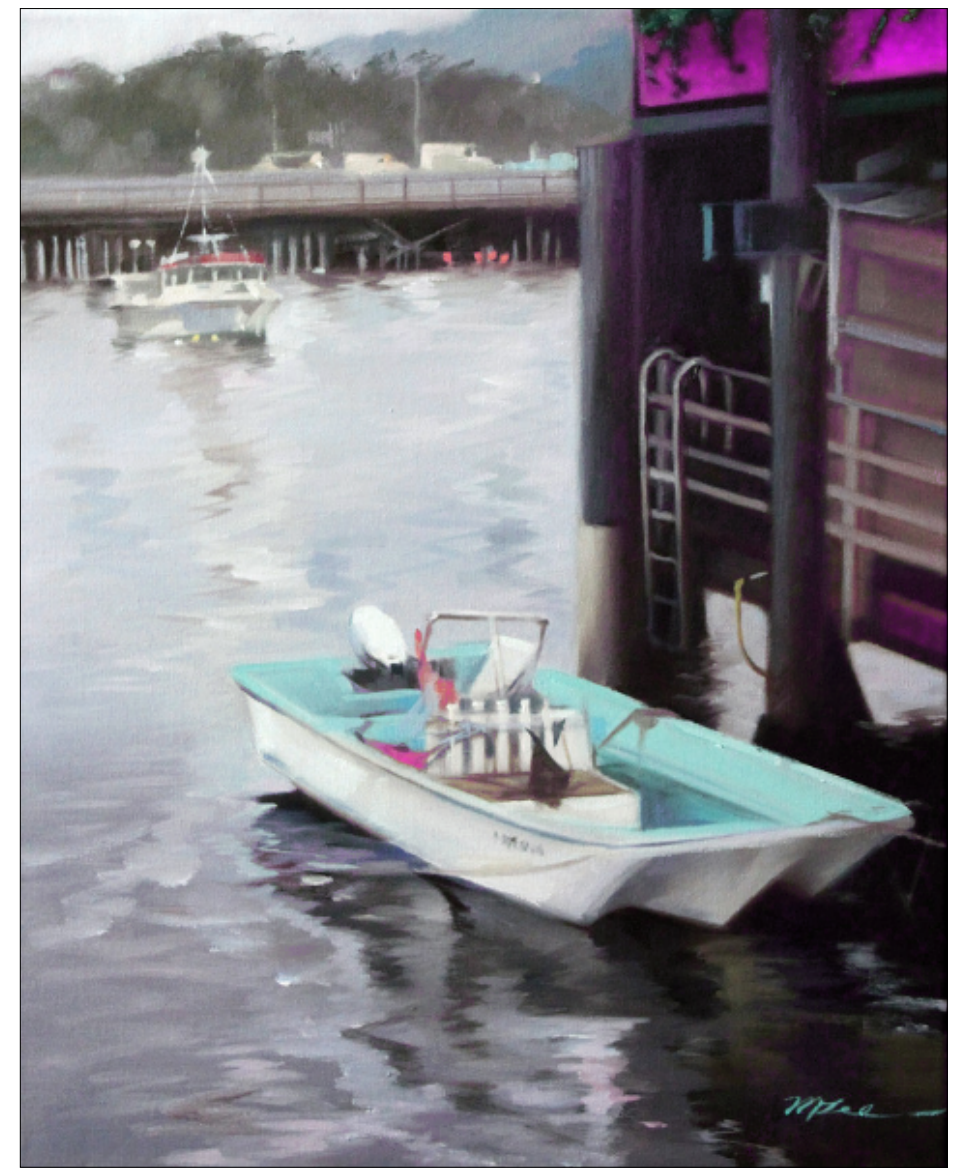
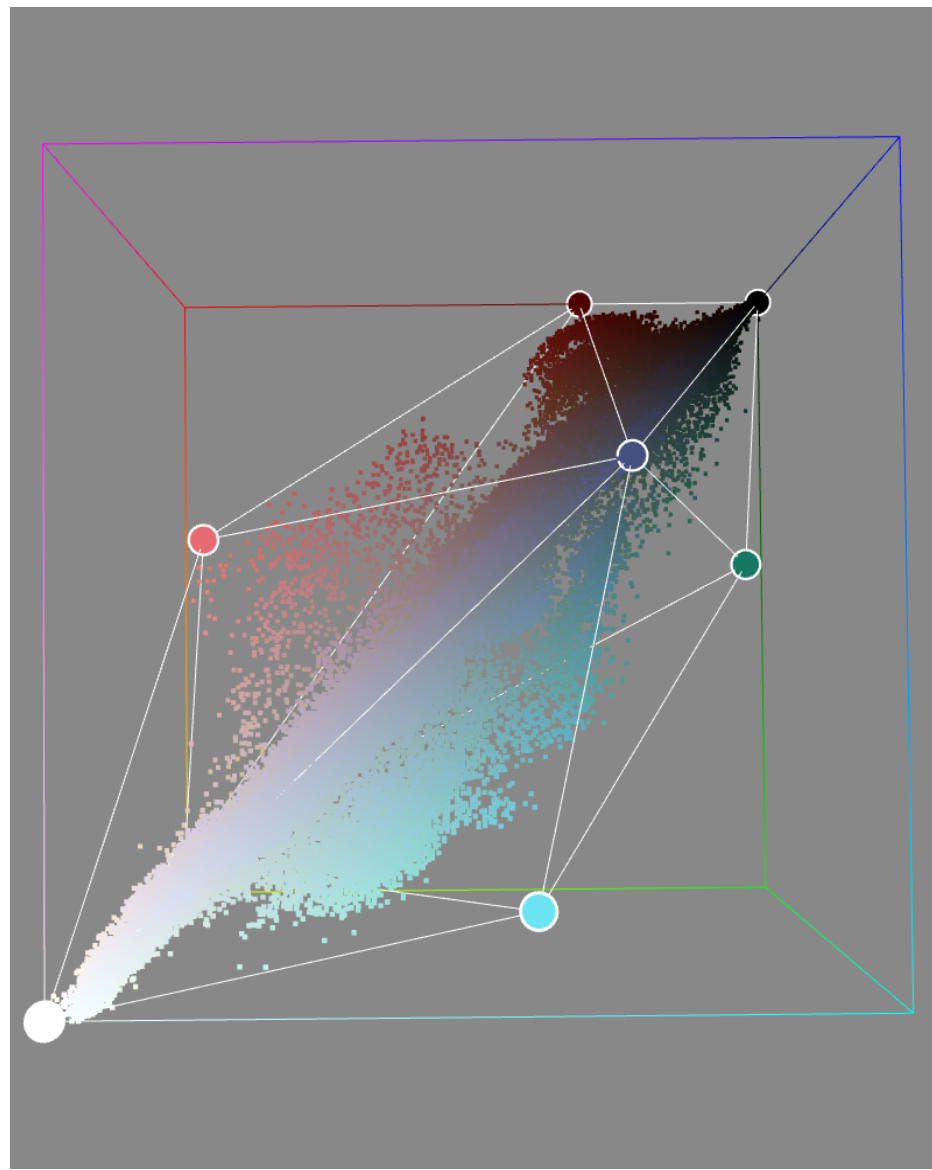
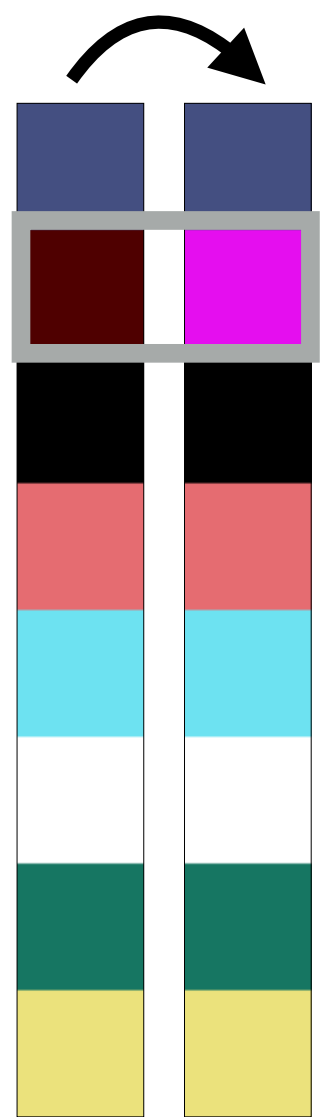
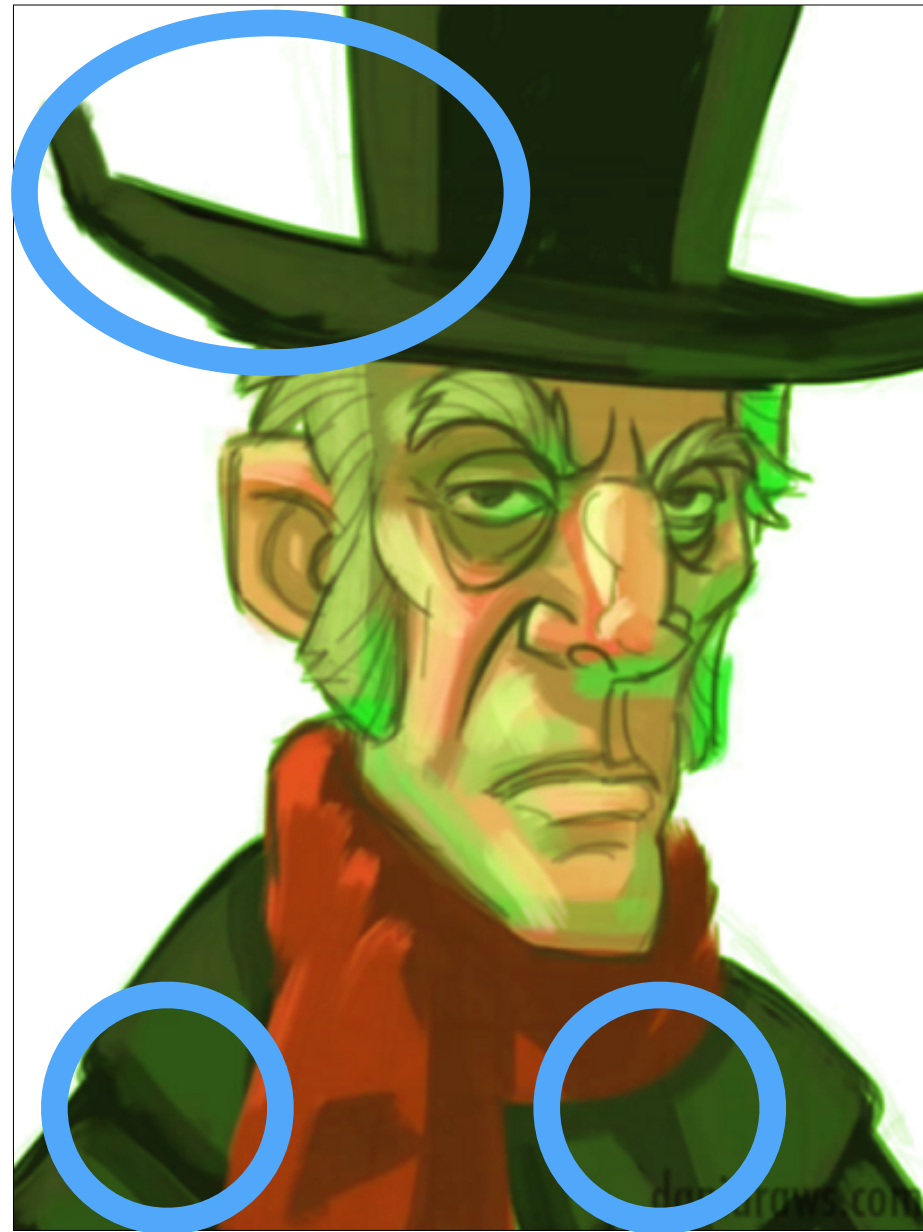
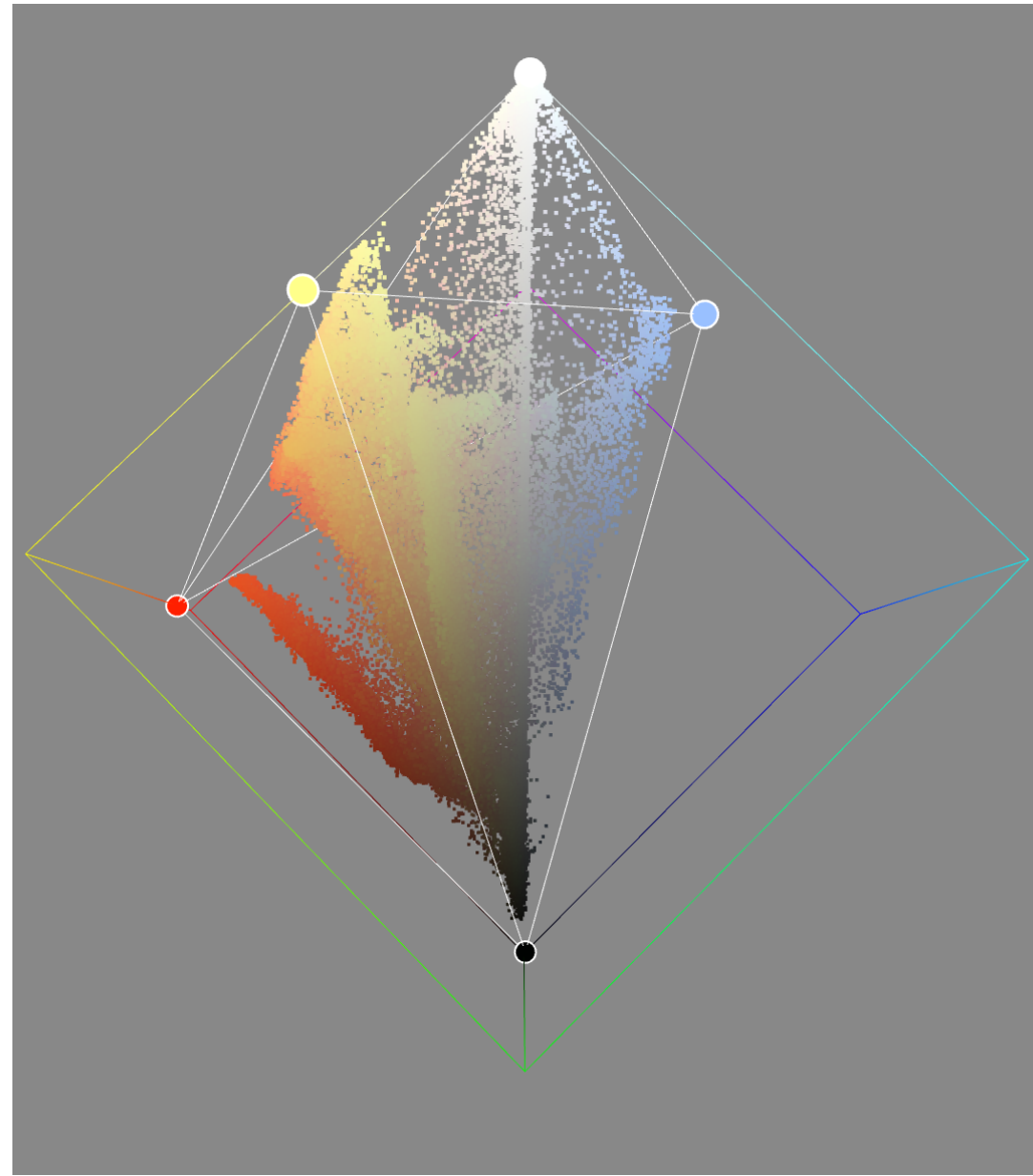
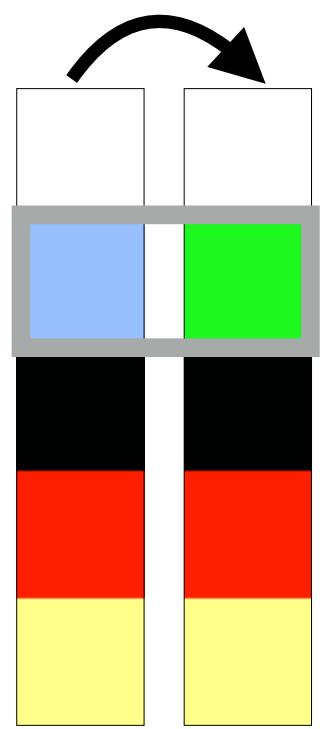
Original

Color distributions

Delaunay

Star





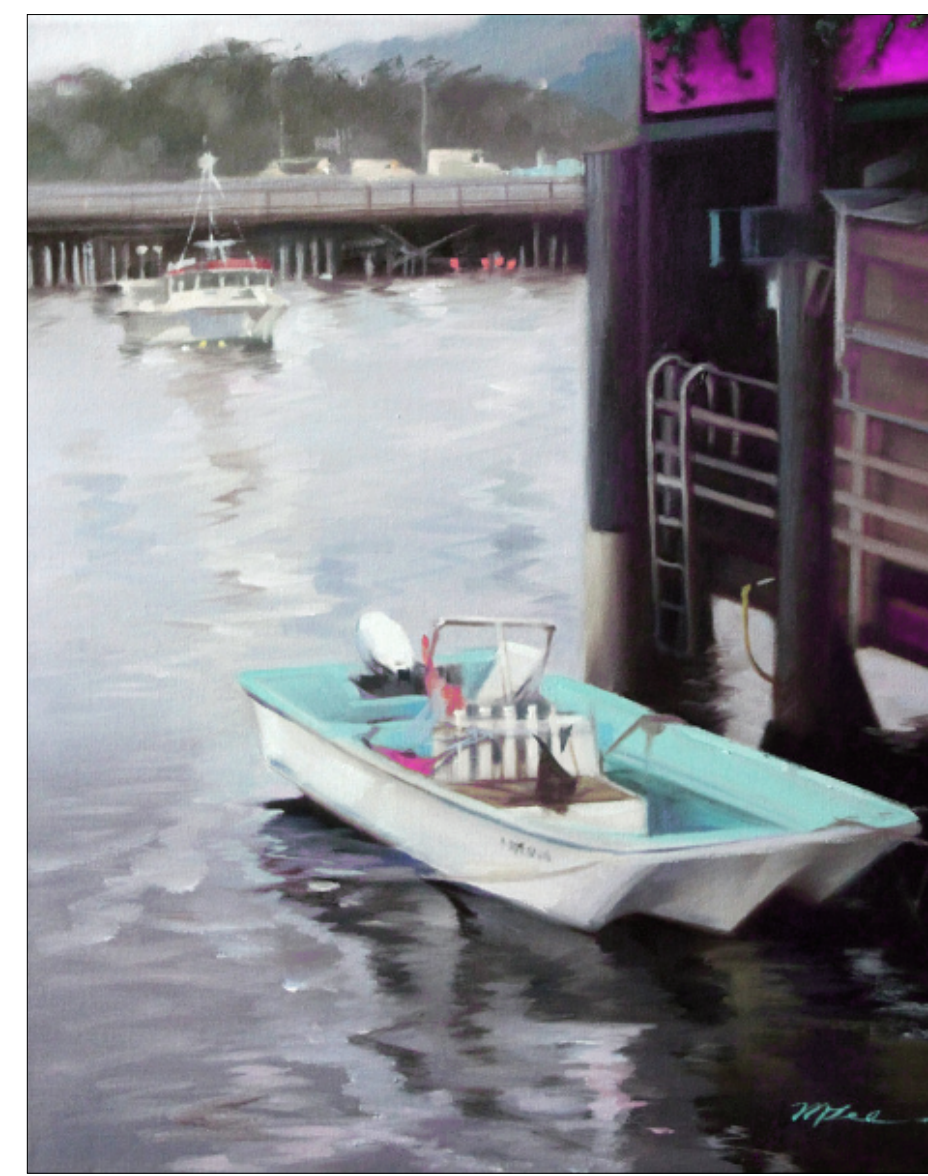
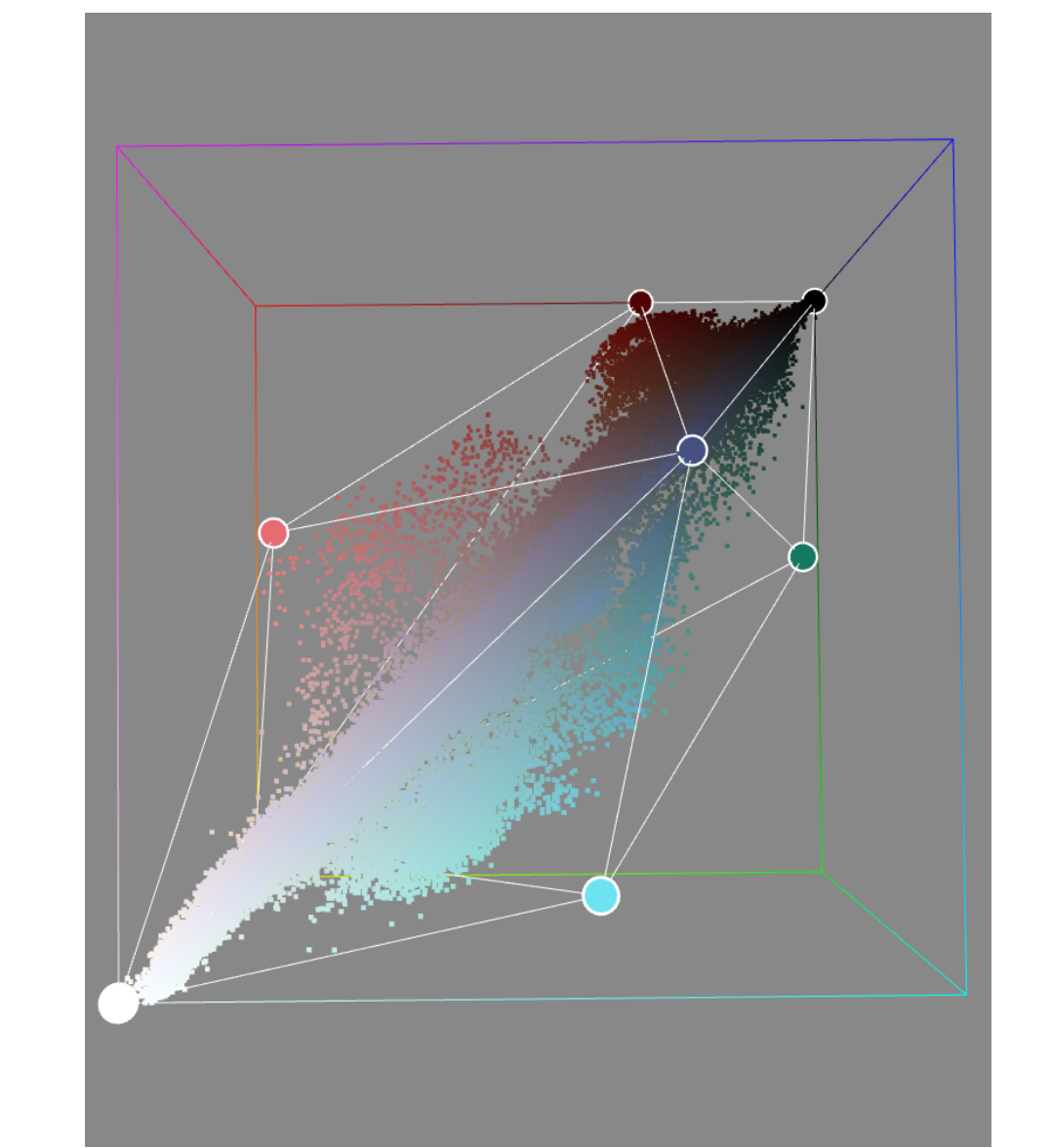
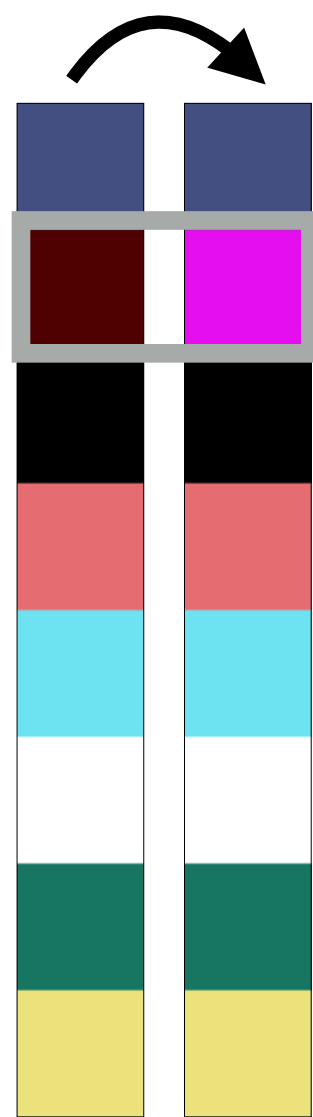
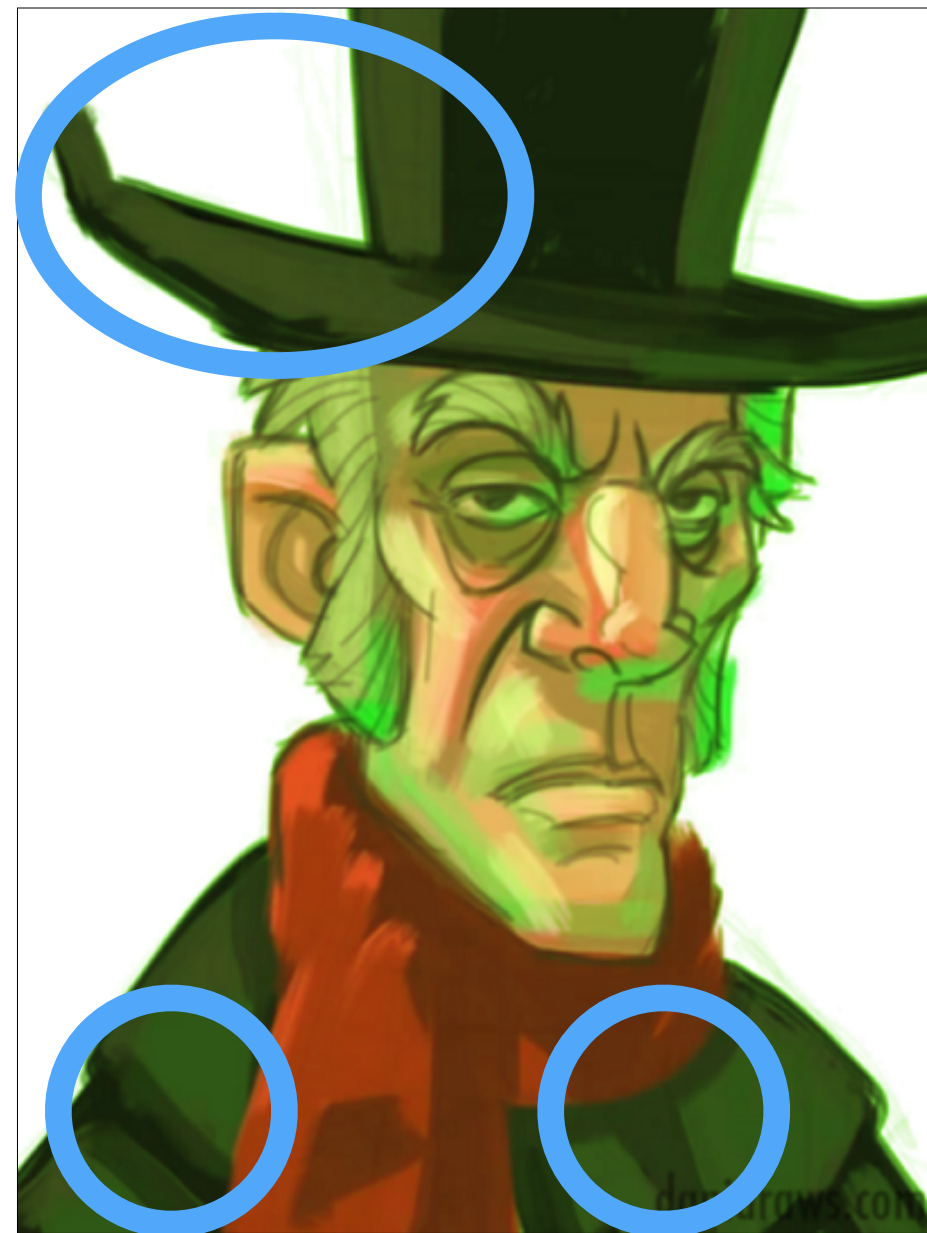
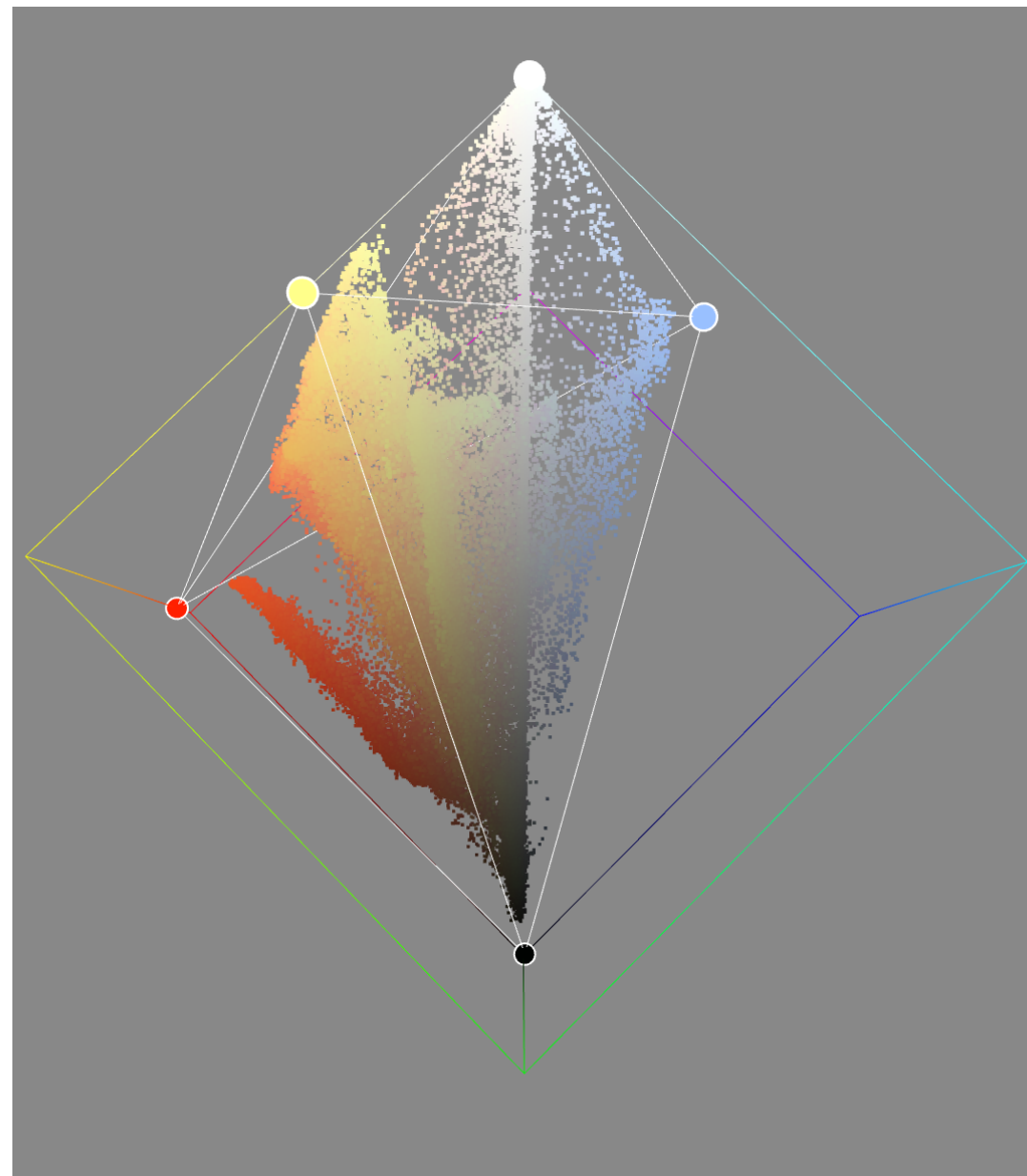
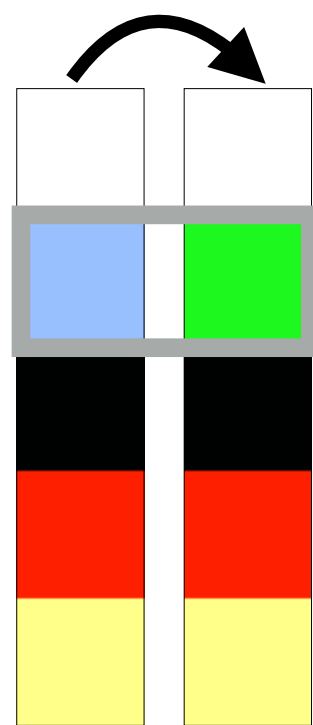
Original

Color distributions

Delaunay

Star





Original

Color distributions

Delaunay

Star



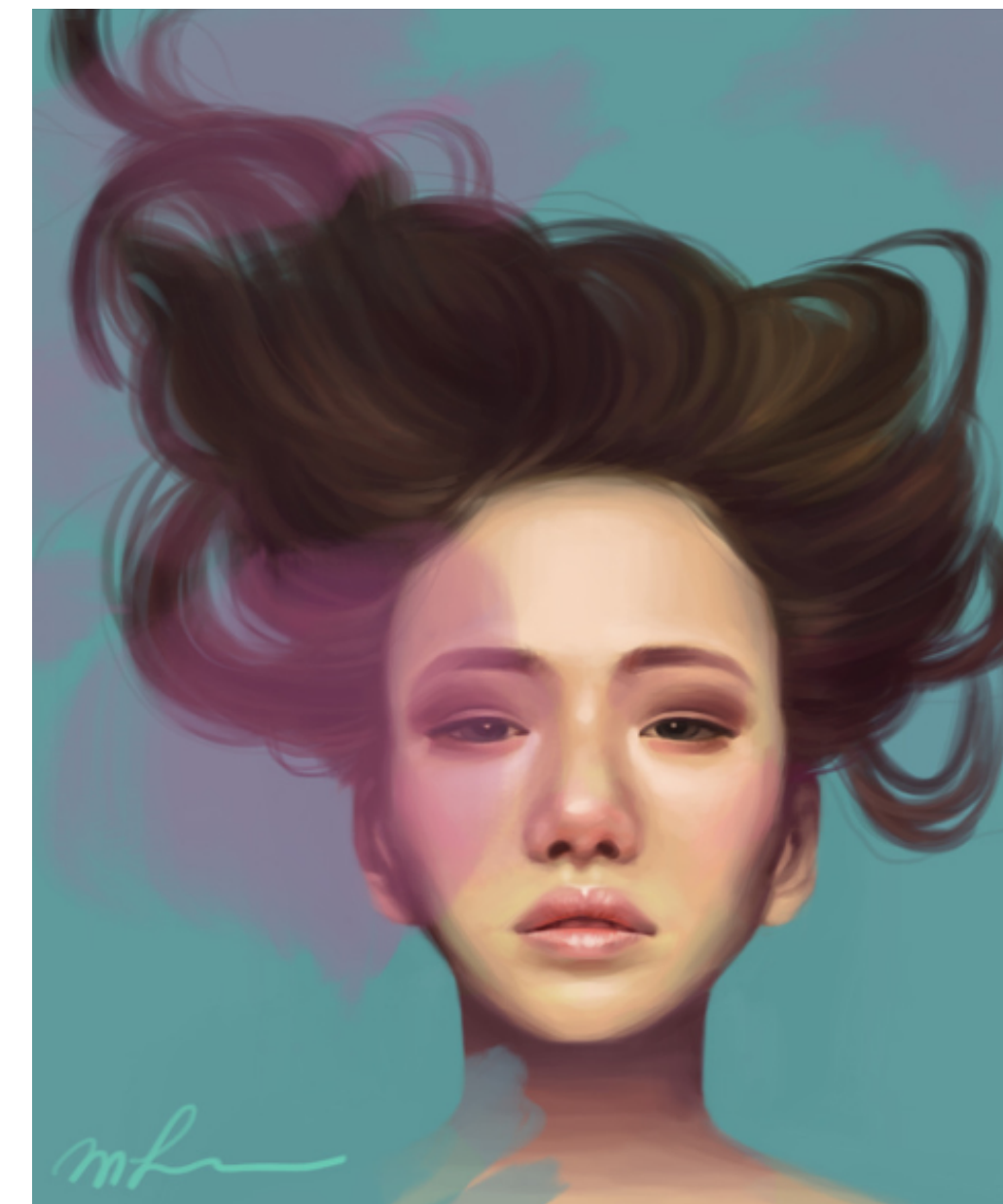
# Two-level decomposition

image

Fixed

$$\mathbf{W} = \mathbf{W}_{\text{RGB}} * \mathbf{W}_{\text{RGBXY}}$$

RGB palette



# Two-level decomposition

image

Palette updates

Fixed

$$\mathbf{W} = \mathbf{W}_{\text{RGB}} * \mathbf{W}_{\text{RGBXY}}$$

RGB palette





# Two-level decomposition

image



RGB palette



$$\mathbf{W} = \mathbf{W}_{\text{RGB}} * \mathbf{W}_{\text{RGBXY}}$$

Palette updates      Fixed

A thick black arrow points from the equation towards the image on the right.

# Two-level decomposition

image



RGB palette

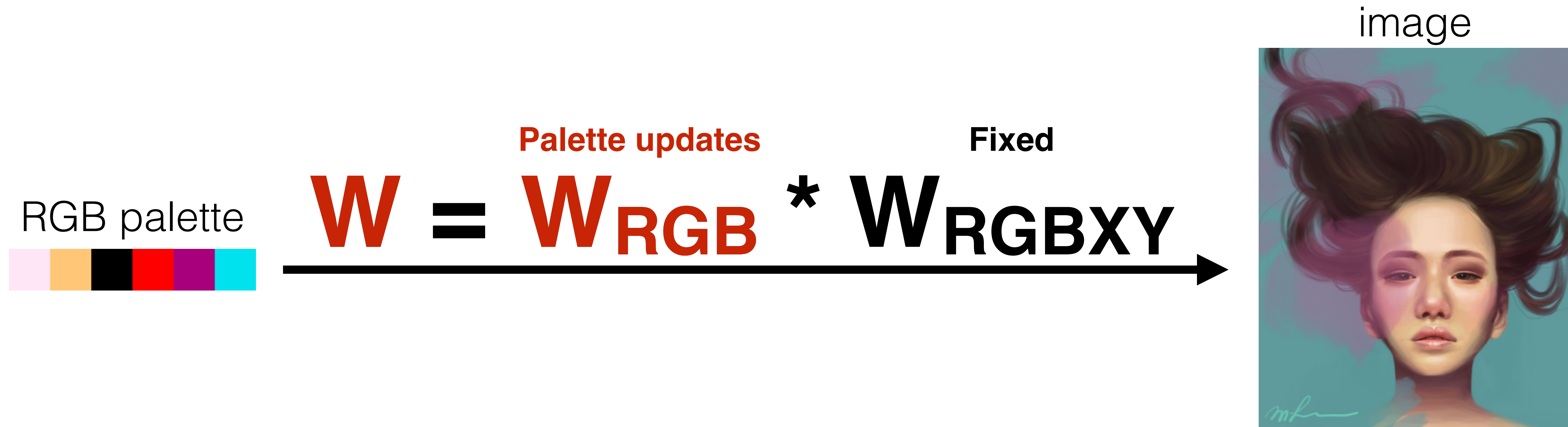


$$W = W_{\text{RGB}} * W_{\text{RGBXY}}$$

Palette updates      Fixed



# Two-level decomposition



Updating  $W_{RGB}$  is independent of image size.

# Two-level decomposition

image

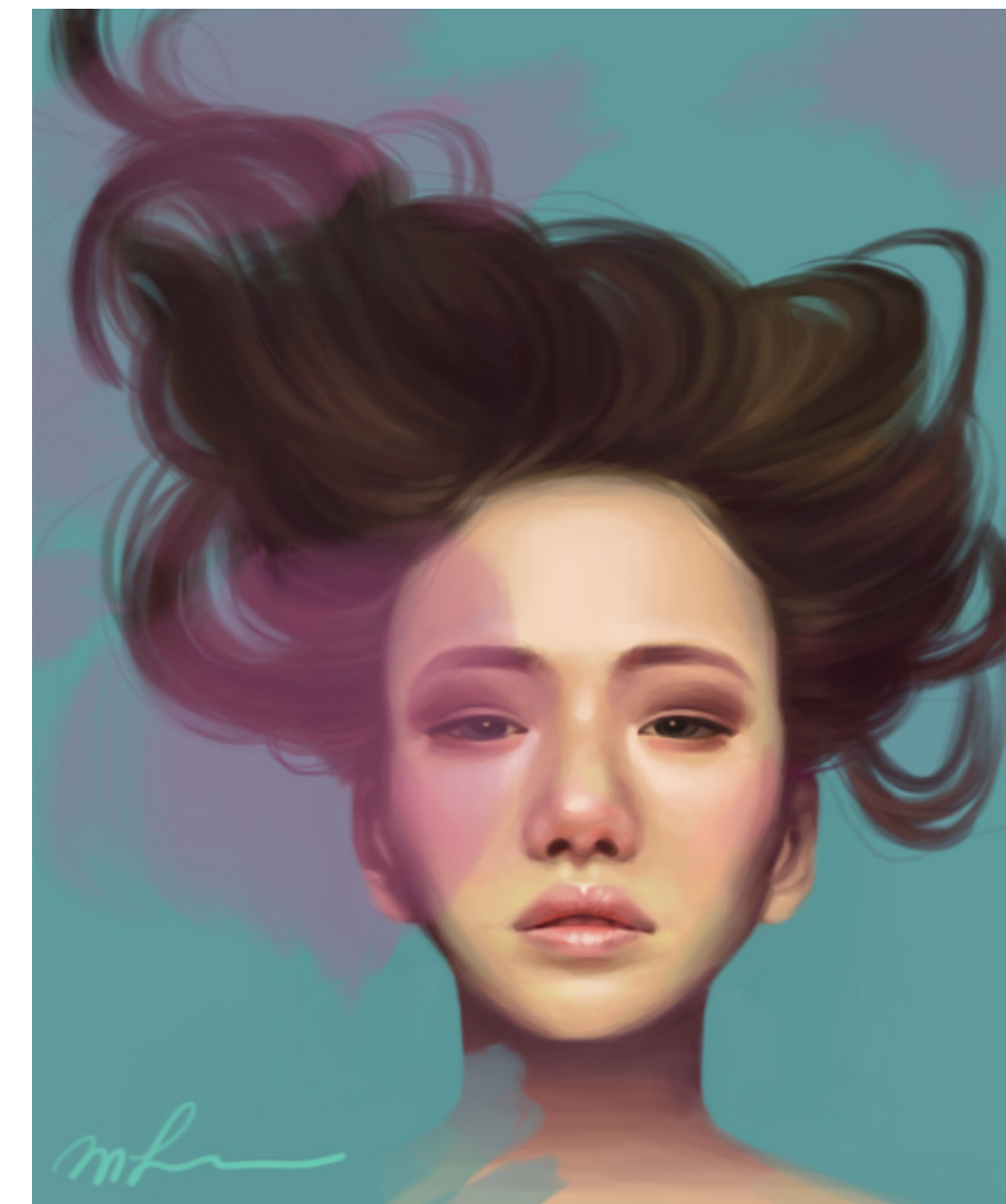
RGB palette



$$\mathbf{W} = \mathbf{W}_{\text{RGB}} * \mathbf{W}_{\text{RGBXY}}$$

Palette updates      Fixed

A large black arrow points from the equation towards the image on the right.

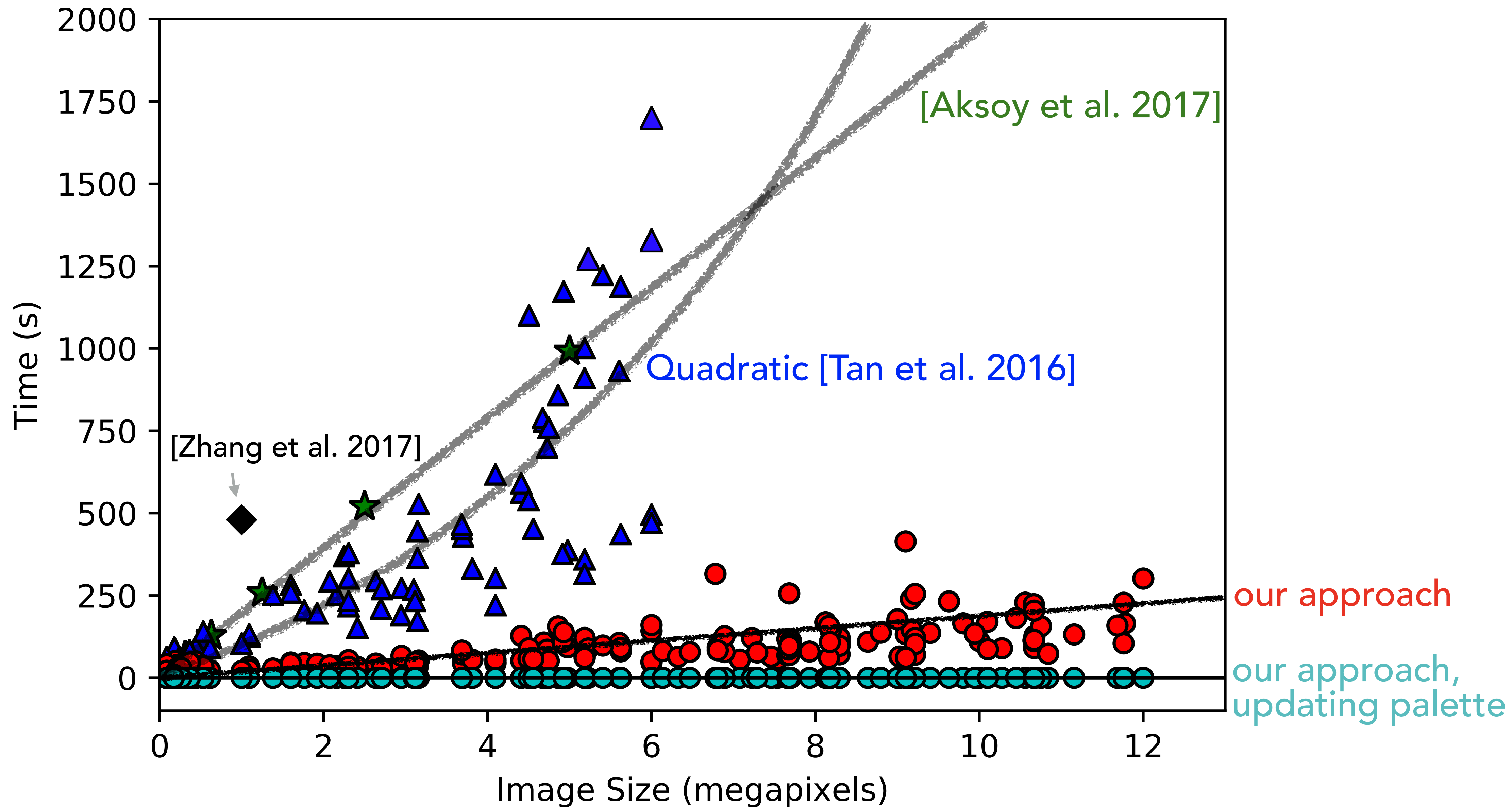


Updating  $\mathbf{W}_{\text{RGB}}$  is independent of image size.

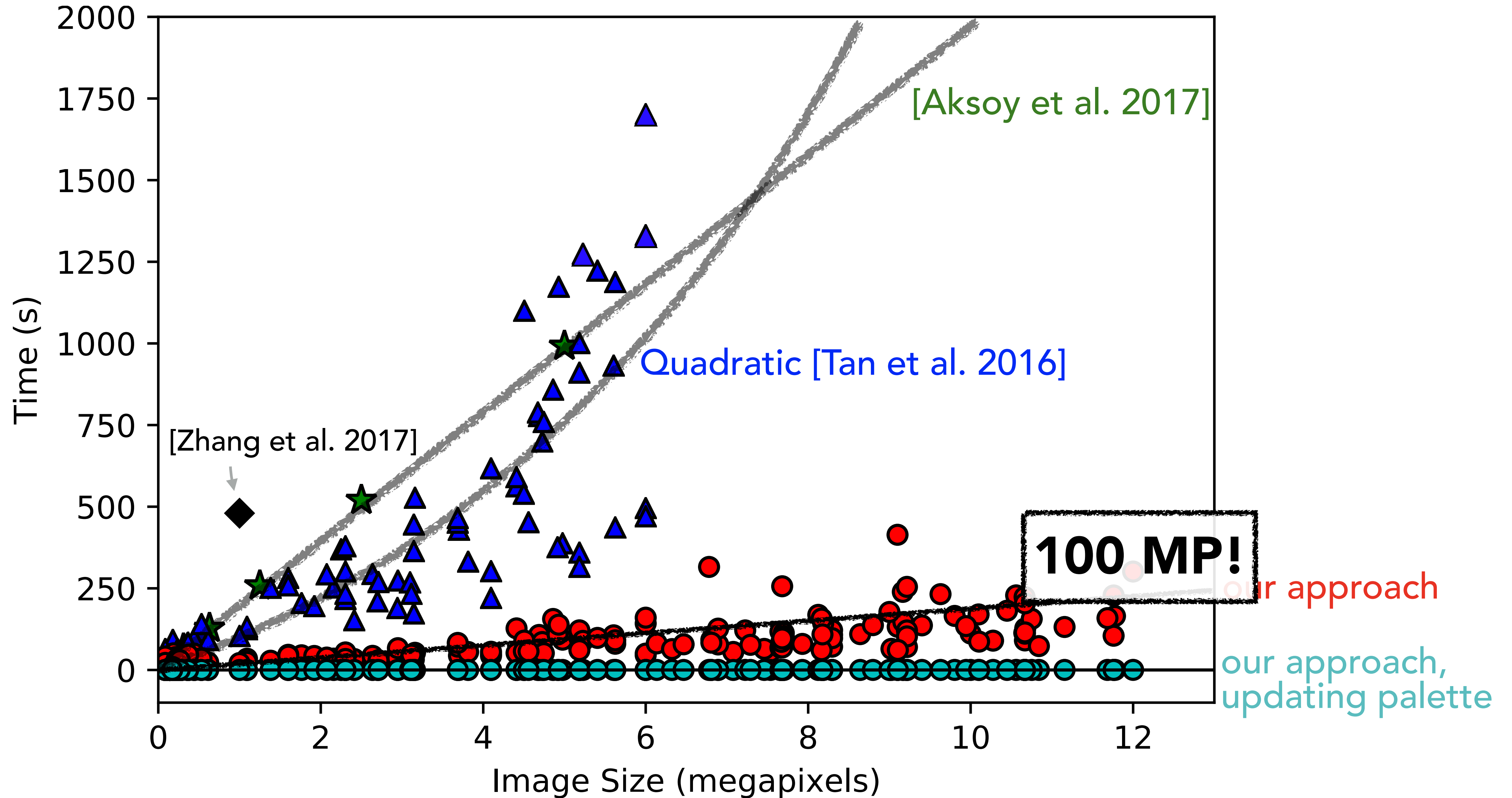
Other methods need to re-compute everything from scratch.



# Performance

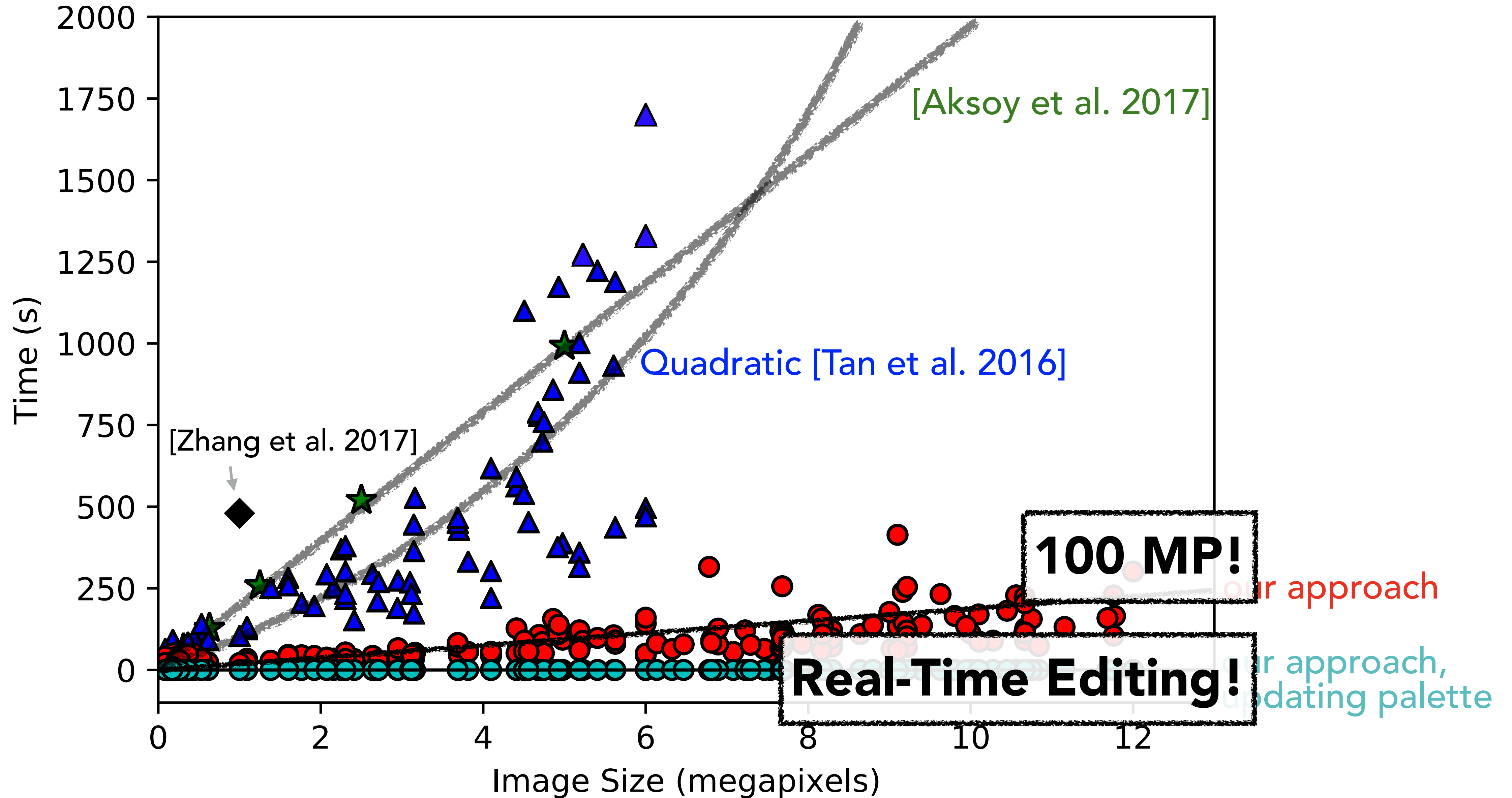


# Performance





# Performance



# Python Implementation

48 lines of code

```
from numpy import *
from scipy.spatial import ConvexHull, Delaunay
from scipy.sparse import coo_matrix

def RGBXY_weights( RGB_palette, RGBXY_data ):
    RGBXY_hull_vertices = RGBXY_data[ ConvexHull( RGBXY_data ).vertices ]
    W_RGBXY = Delaunay_coordinates( RGBXY_hull_vertices, RGBXY_data )
    # Optional: Project outside RGBXY_hull_vertices[:, :3] onto RGB_palette convex hull.
    W_RGB = Star_coordinates( RGB_palette, RGBXY_hull_vertices[:, :3] )
    return W_RGBXY.dot( W_RGB )

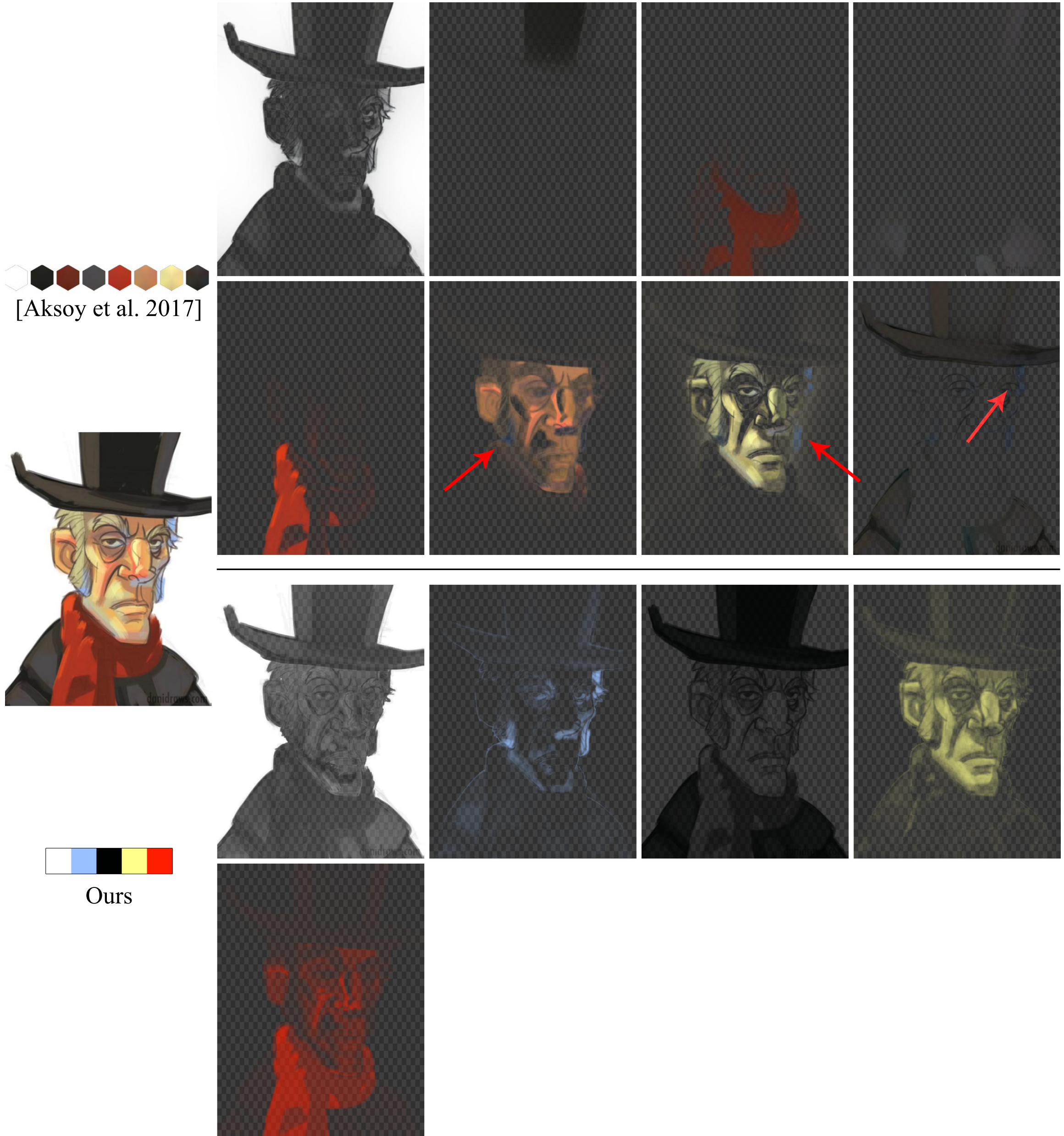
def Star_coordinates( vertices, data ):
    ## Find the star vertex
    star = argmin( linalg.norm( vertices, axis=1 ) )
    ## Make a mesh for the palette
    hull = ConvexHull( vertices )
    ## Star tessellate the faces of the convex hull
    simplices = [ [star] + list(face) for face in hull.simplices if star not in face ]
    barycoords = -1*ones( ( data.shape[0], len(vertices) ) )
    ## Barycentric coordinates for the data in each simplex
    for s in simplices:
        s0 = vertices[s[:1]]
        b = linalg.solve( (vertices[s[1:]]-s0).T, (data-s0).T ).T
        b = append( 1-b.sum(axis=1)[:None], b, axis=1 )
        ## Update barycoords whenever the data is inside the current simplex.
        mask = (b>=0).all(axis=1)
        barycoords[mask] = 0.
        barycoords[ix_(mask,s)] = b[mask]
    return barycoords

def Delaunay_coordinates( vertices, data ): # Adapted from Gareth Rees
    # Compute Delaunay tessellation.
    tri = Delaunay( vertices )
    # Find the tetrahedron containing each target (or -1 if not found).
    simplices = tri.find_simplex(data, tol=1e-6)
    assert (simplices != -1).all() # data contains outside vertices.
    # Affine transformation for simplex containing each datum.
    X = tri.transform[simplices, :data.shape[1]]
    # Offset of each datum from the origin of its simplex.
    Y = data - tri.transform[simplices, data.shape[1]]
    # Compute the barycentric coordinates of each datum in its simplex.
    b = einsum( '...jk,...k->...j', X, Y )
    barycoords = c_[b, 1-b.sum(axis=1)]
    # Return the weights as a sparse matrix.
    rows = repeat(arange(len(data)).reshape((-1,1)), len(tri.simplices[0]), 1).ravel()
    cols = tri.simplices[simplices].ravel()
    vals = barycoords.ravel()
    return coo_matrix( (vals,(rows,cols)), shape=(len(data),len(vertices)) ).tocsr()
```



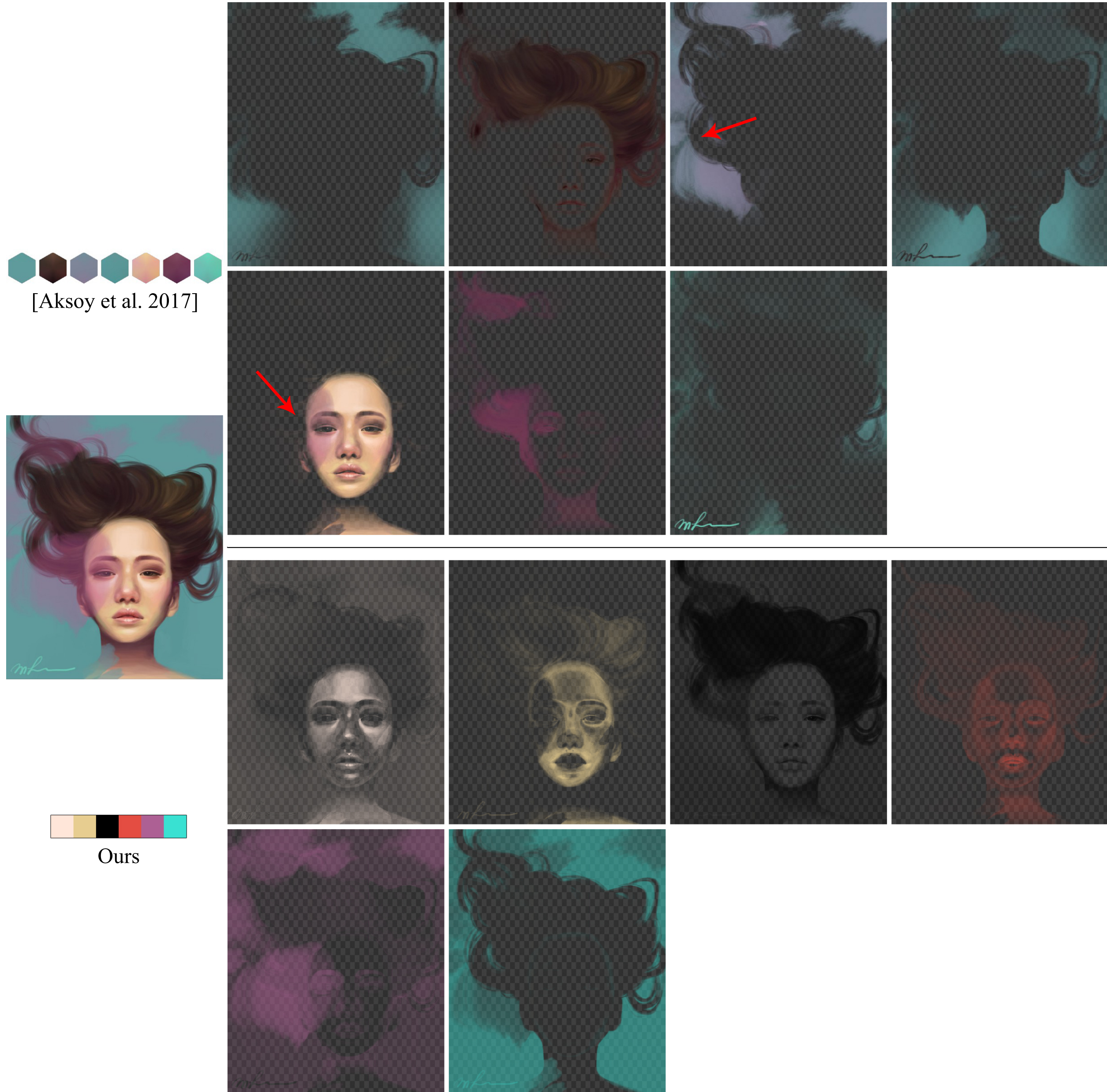
# Comparisons

# Layer quality comparison with [Aksoy et al. 2017]



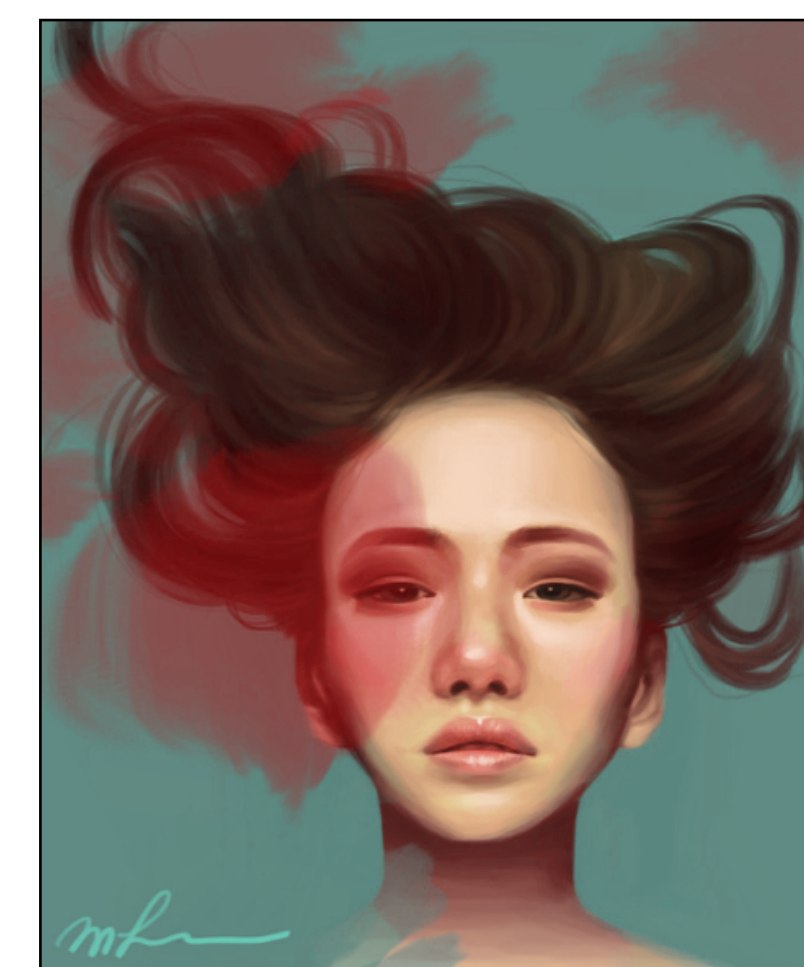
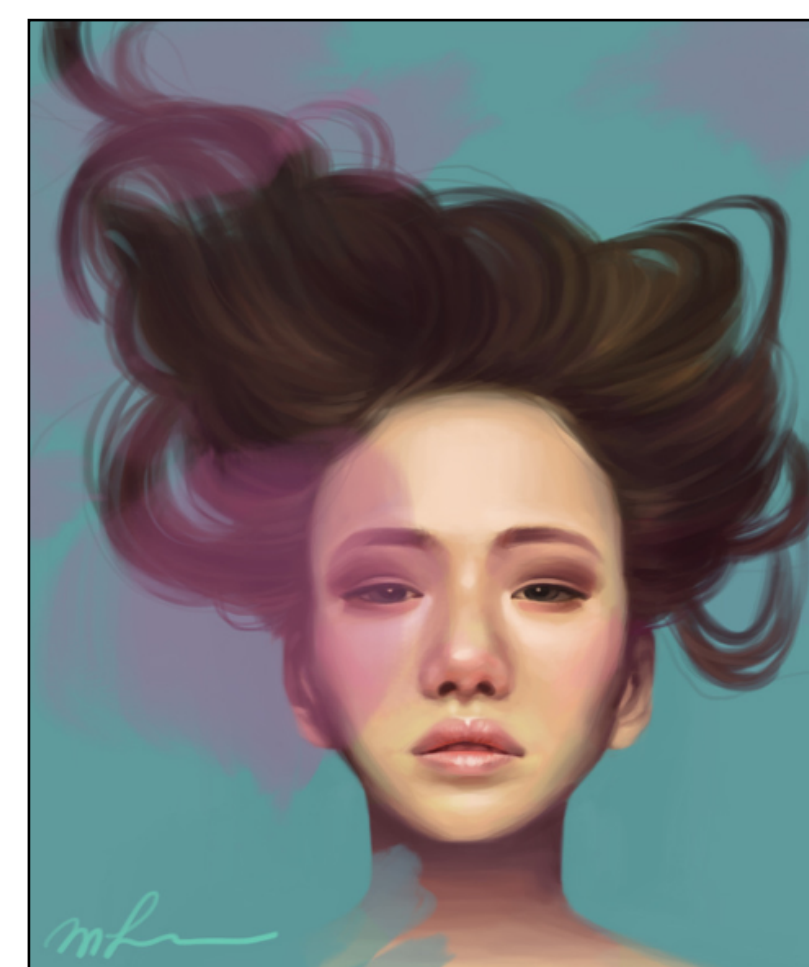


# Layer quality comparison with [Aksoy et al. 2017]





# Recoloring comparison with three previous methods

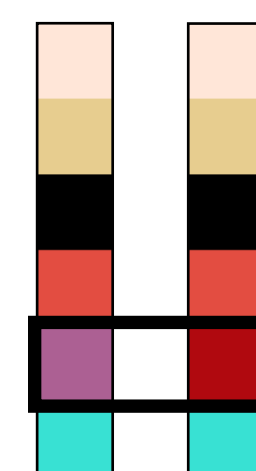
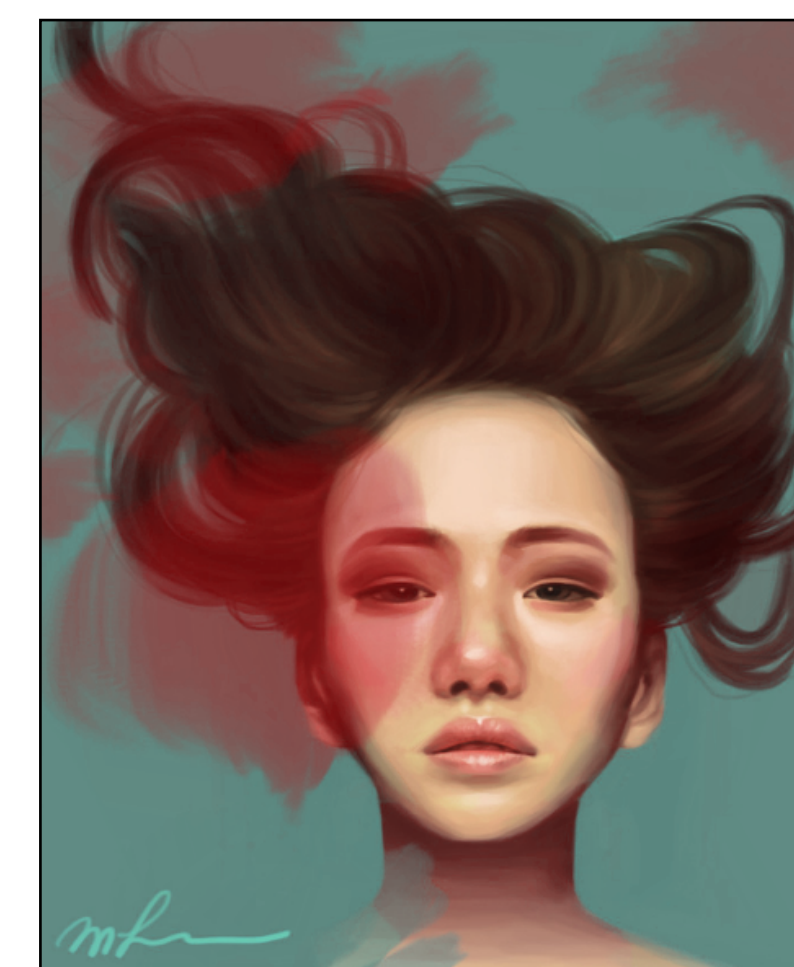
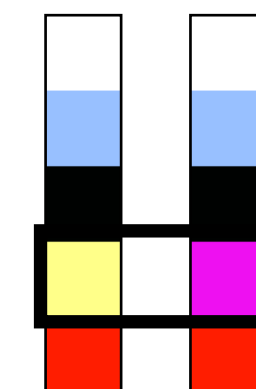


Original

Ours



# Recoloring comparison with three previous methods



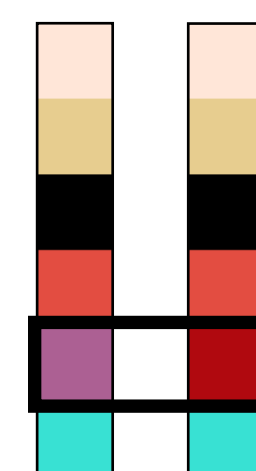
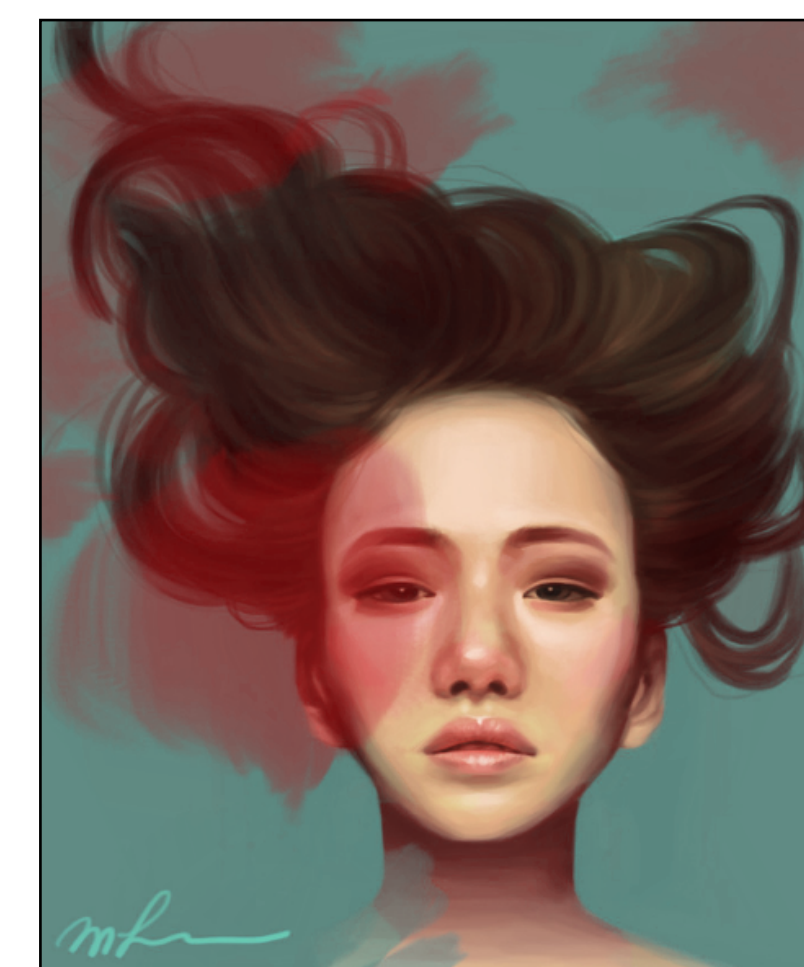
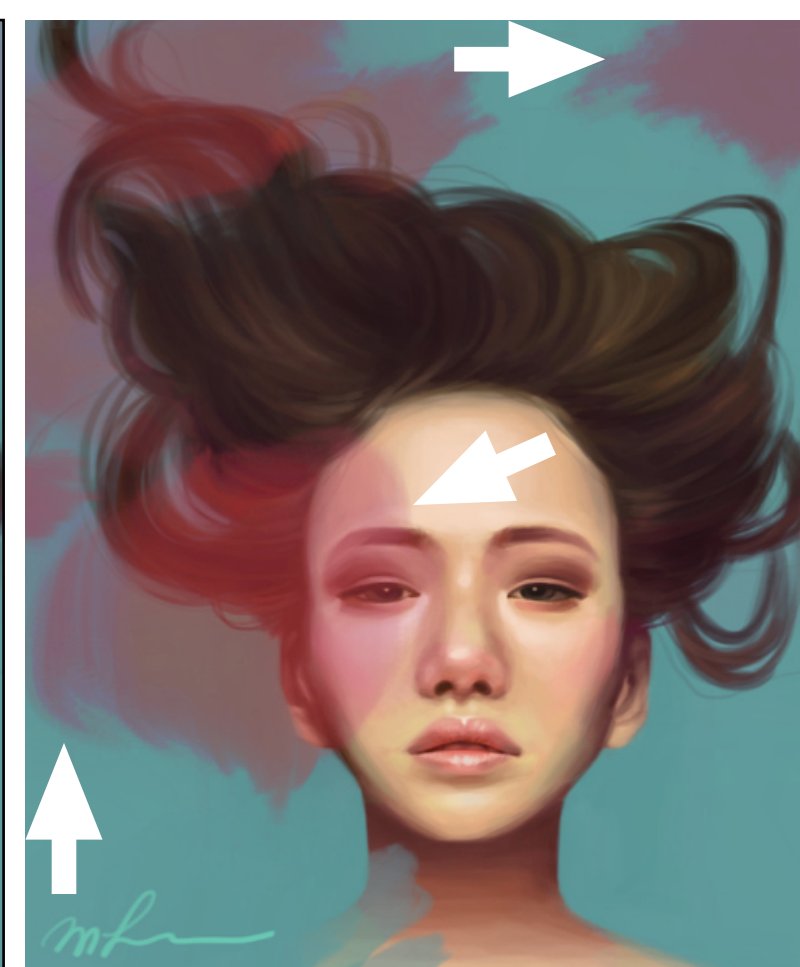
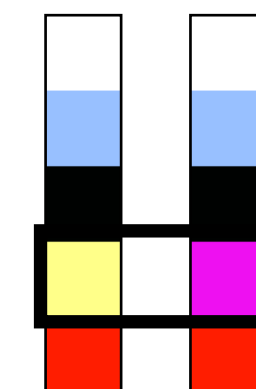
Original

Aksoy et al. 2017

Ours



# Recoloring comparison with three previous methods



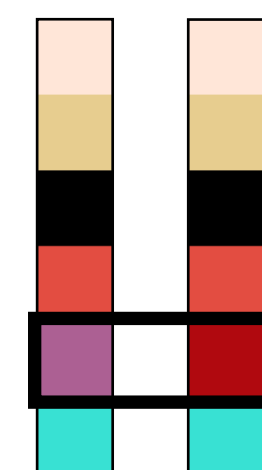
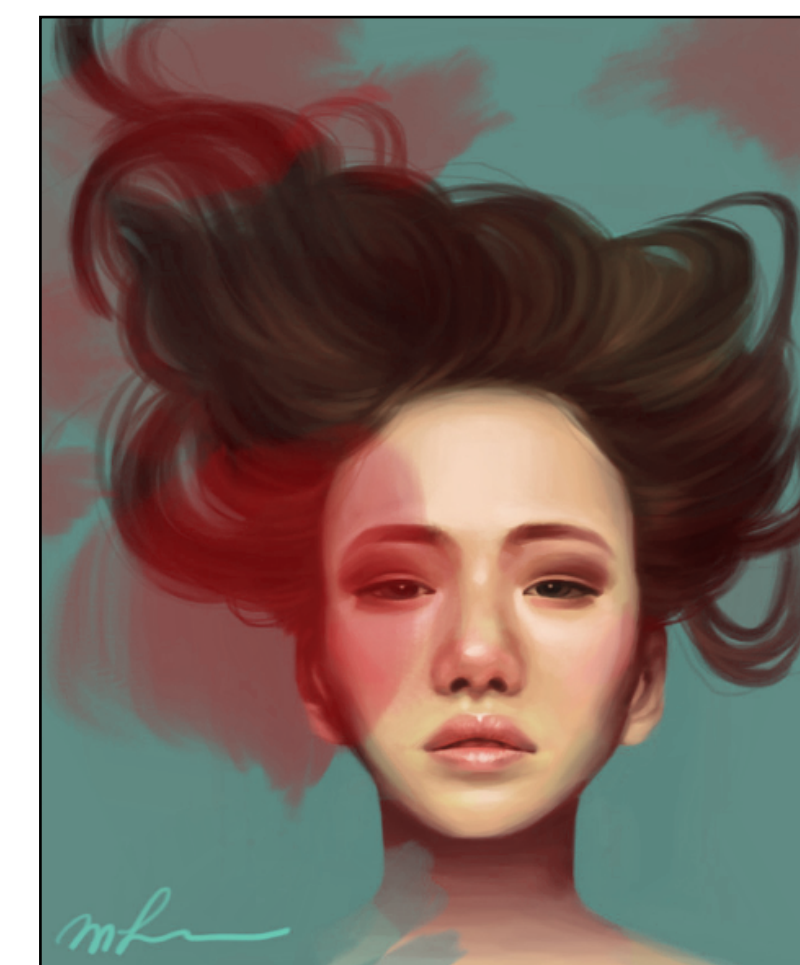
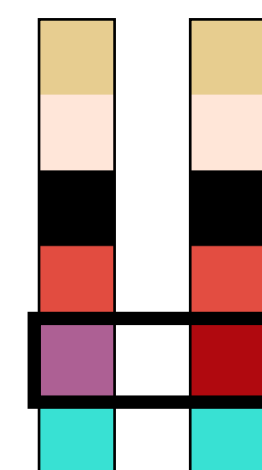
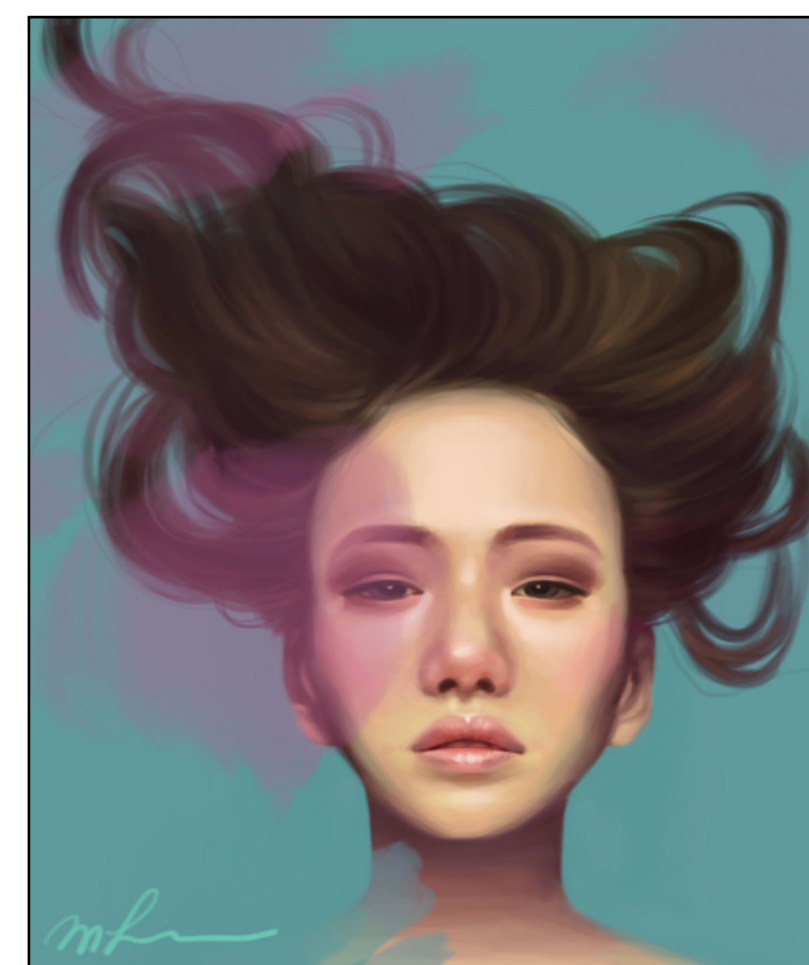
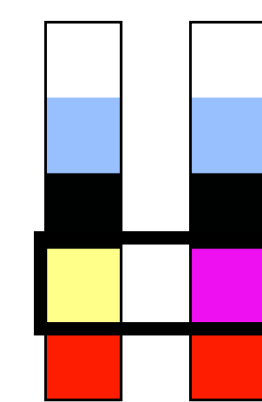
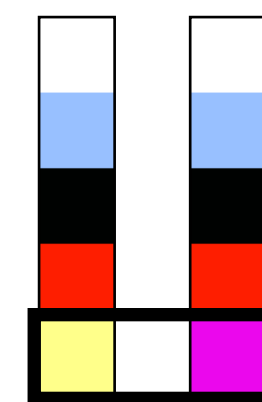
Original

Aksoy et al. 2017

Ours



# Recoloring comparison with three previous methods



Original

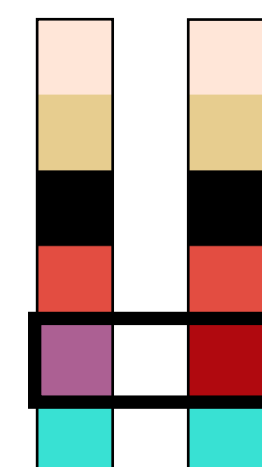
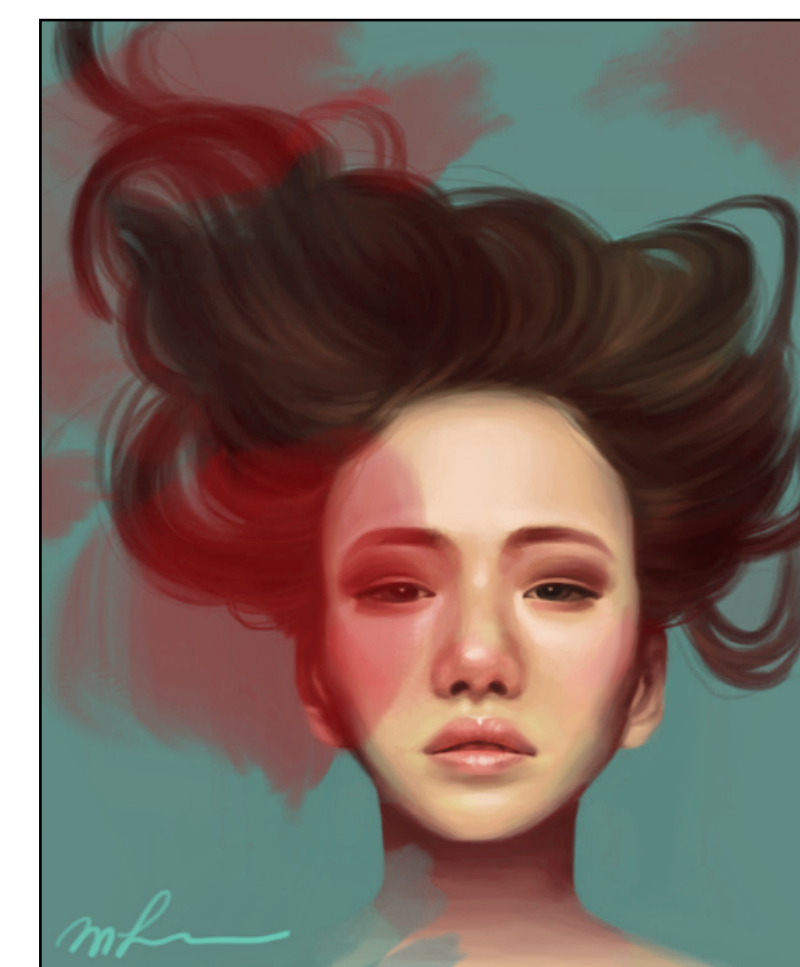
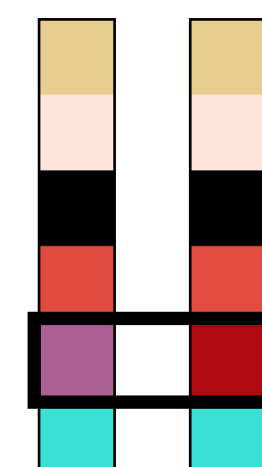
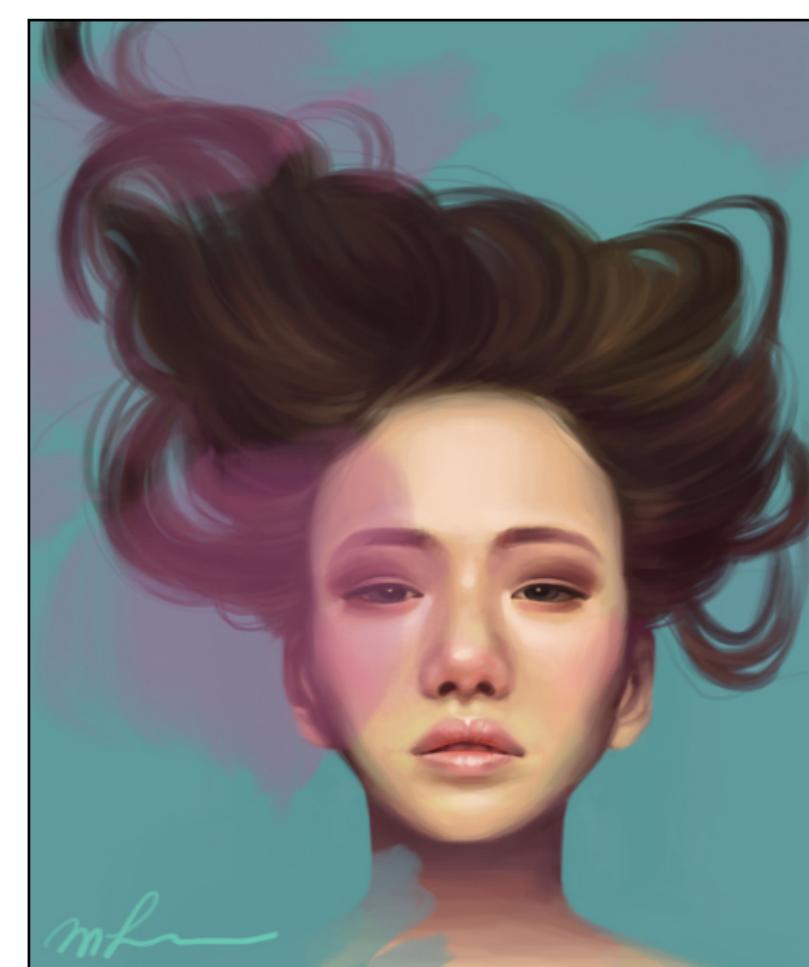
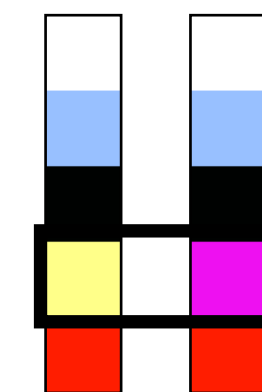
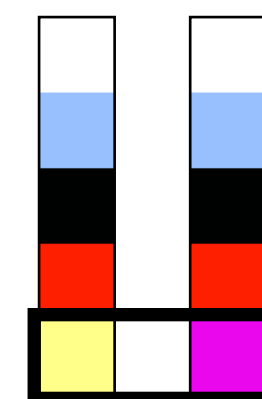
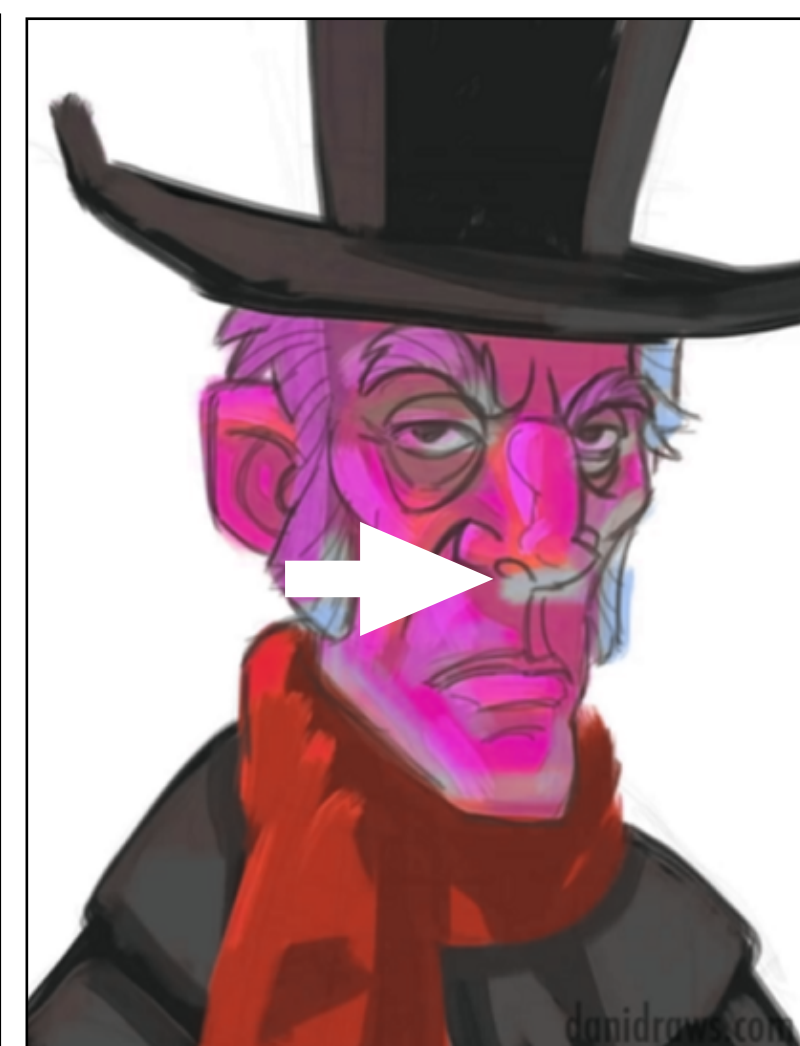
Aksoy et al. 2017

Tan et al. 2016

Ours



# Recoloring comparison with three previous methods



Original

Aksoy et al. 2017

Tan et al. 2016

Ours



# Recoloring comparison with three previous methods



Original

Aksoy et al. 2017

Tan et al. 2016

Chang et al. 2015

Ours



# Recoloring comparison with three previous methods



Original

Aksoy et al. 2017

Tan et al. 2016

Chang et al. 2015

Ours



# Demo

**Javascript + Python with PyOpenCL**

# **Layer creation from scratch**

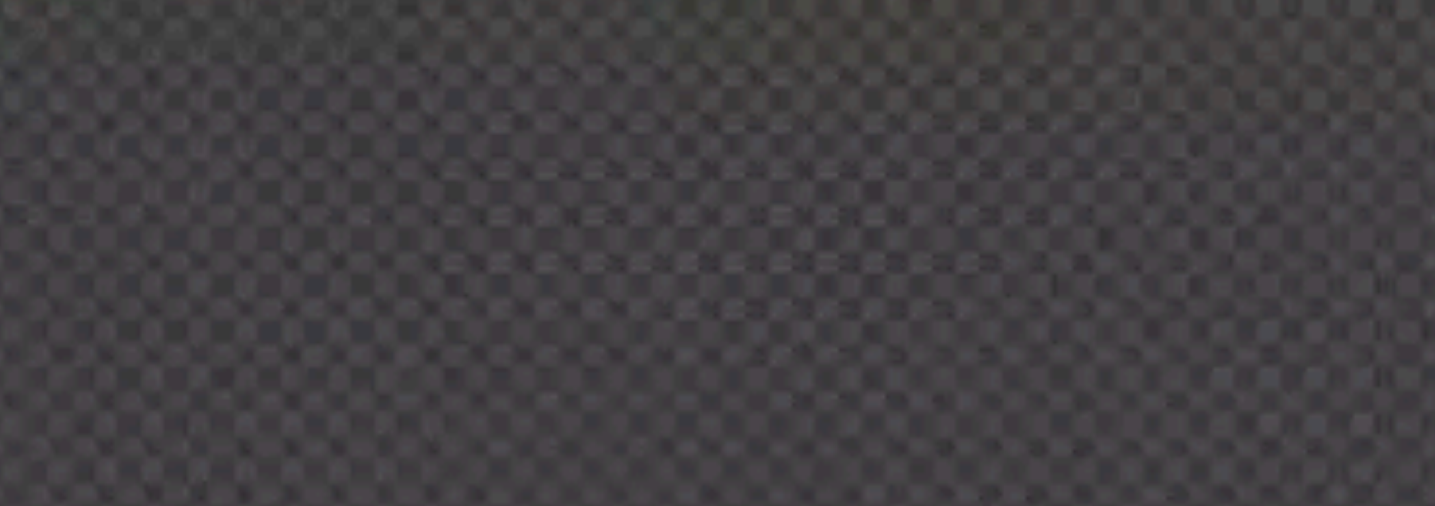


Image: [girls.png](#)

Reconstruction

Difference

Layers:



Choose File No file chosen

re-compute RGBXY weights

create automatic palette

Prescribed number of layers:

colorful

Add Random Palette Color

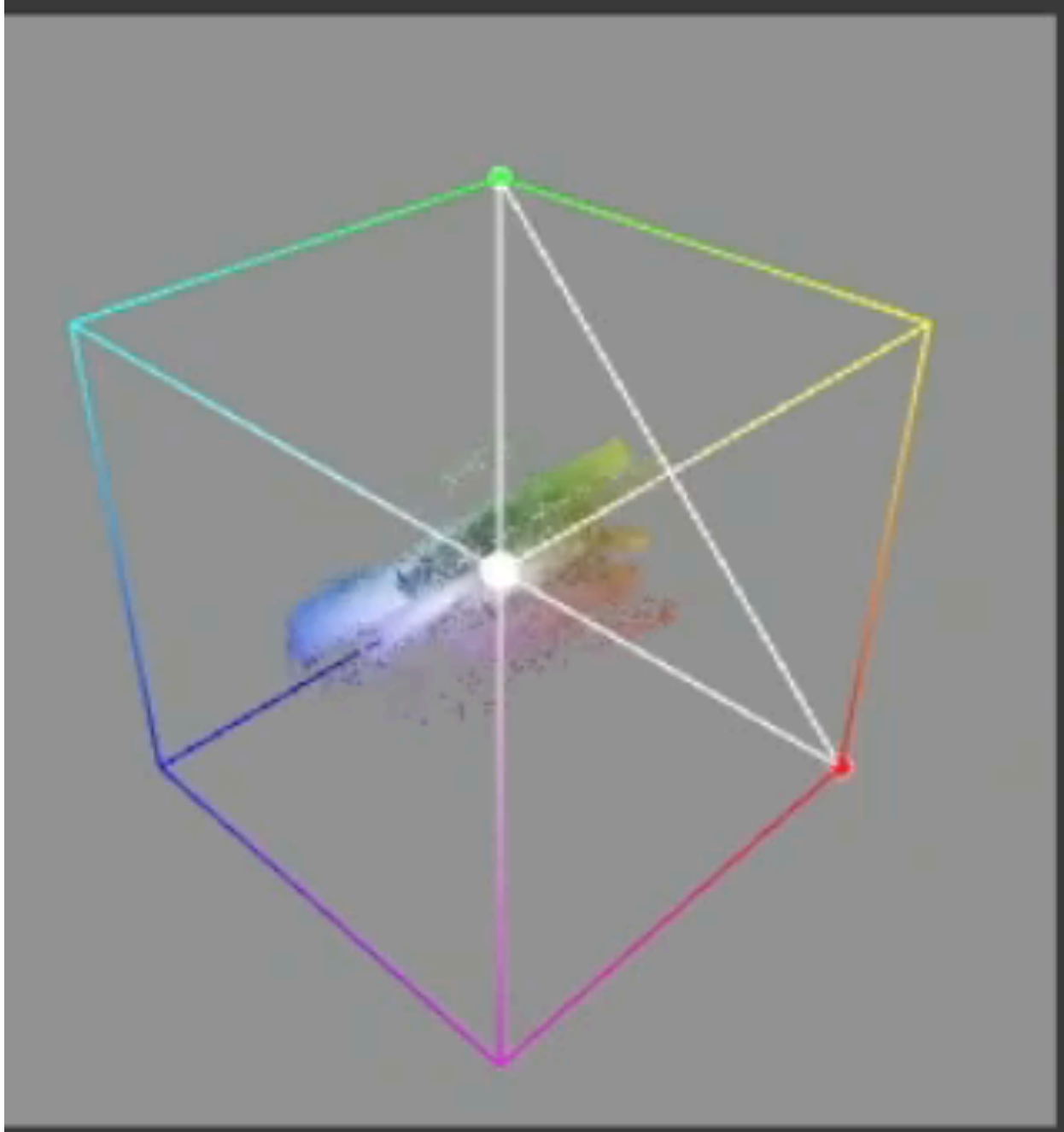


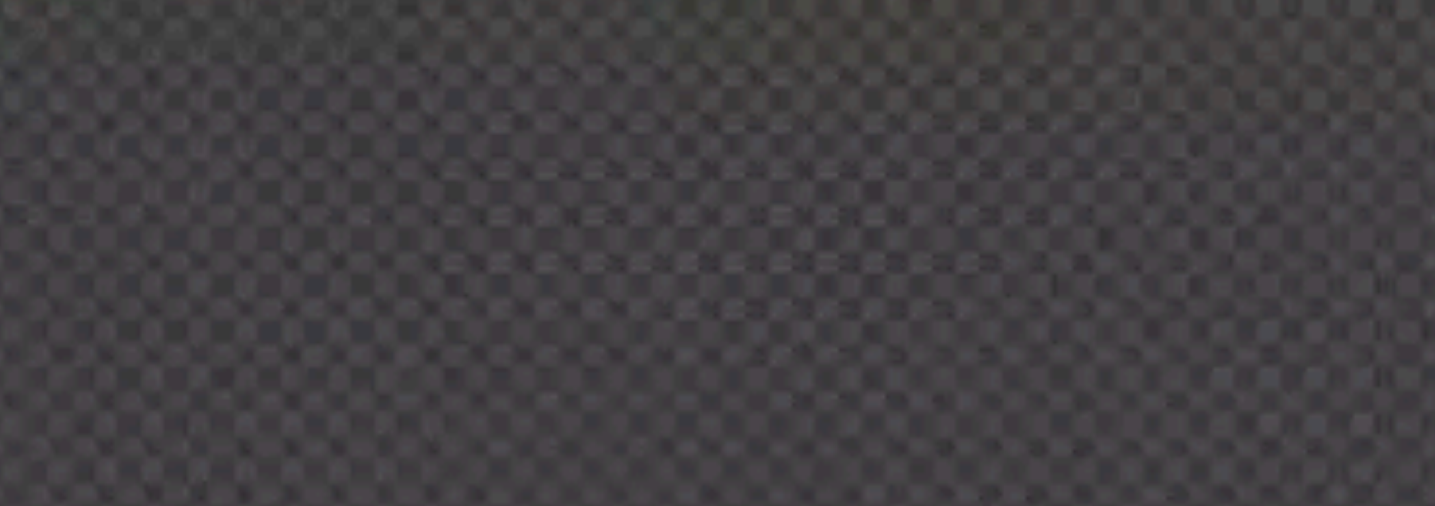


Image: [girls.png](#)

Reconstruction

Difference

Layers:



Choose File No file chosen

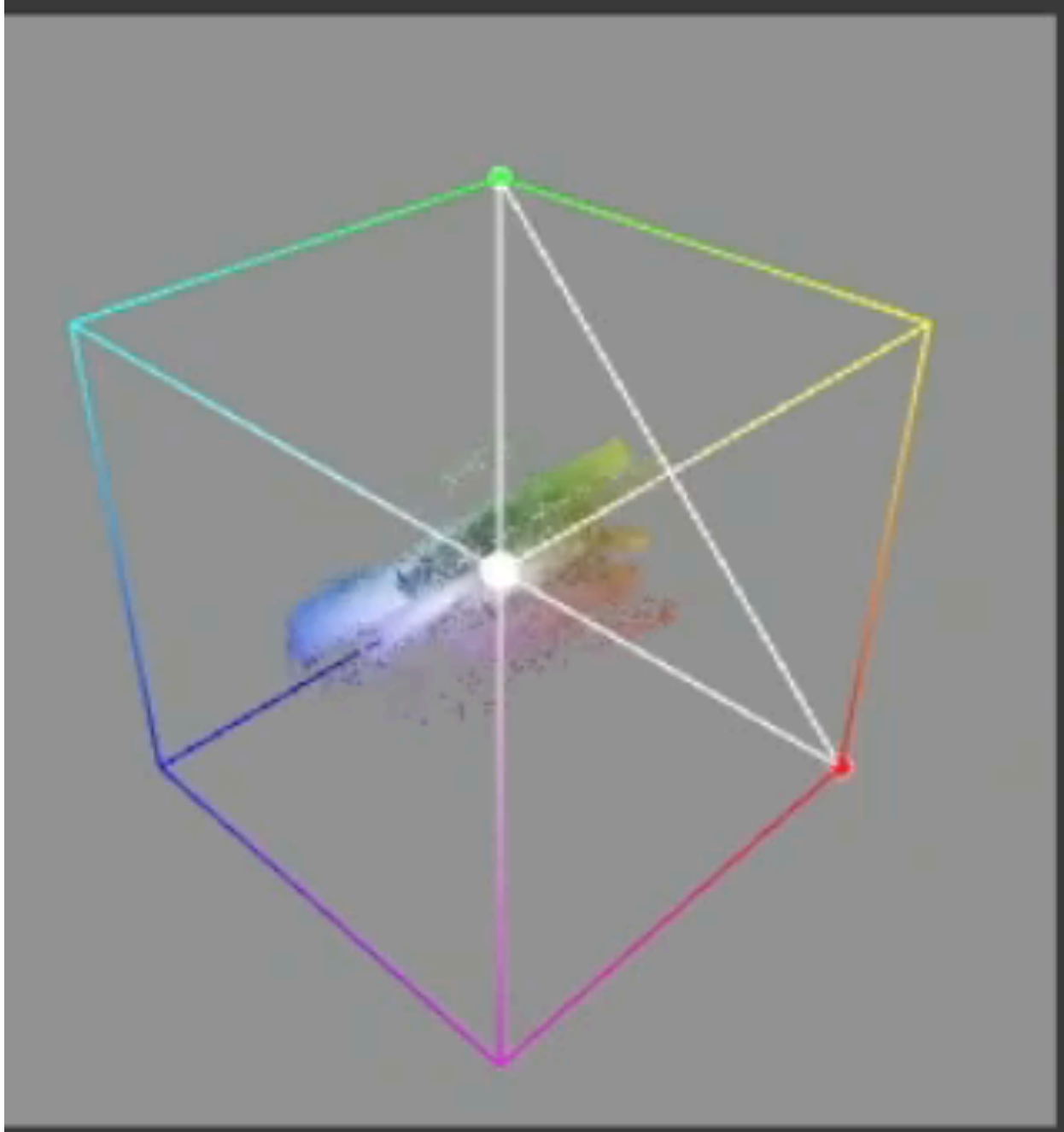
re-compute RGBXY weights

create automatic palette

Prescribed number of layers:

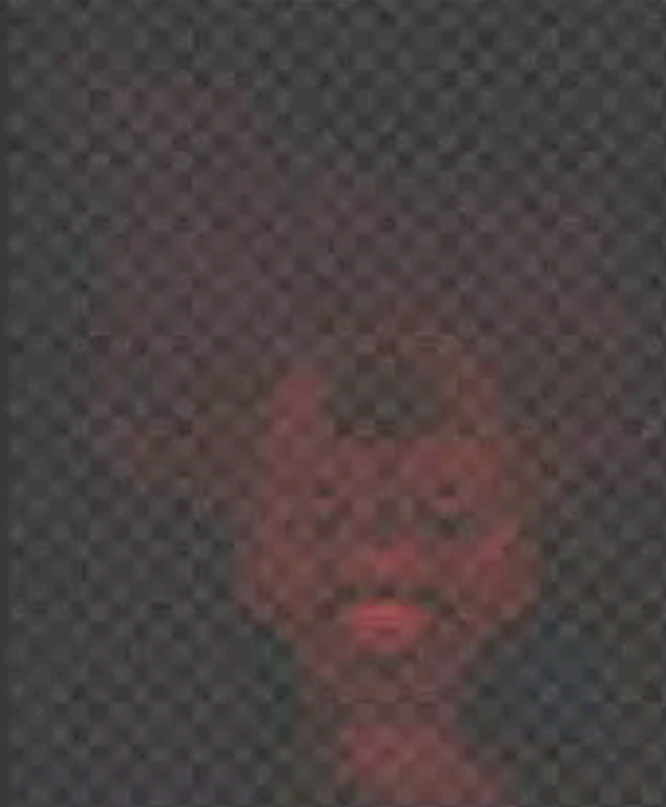
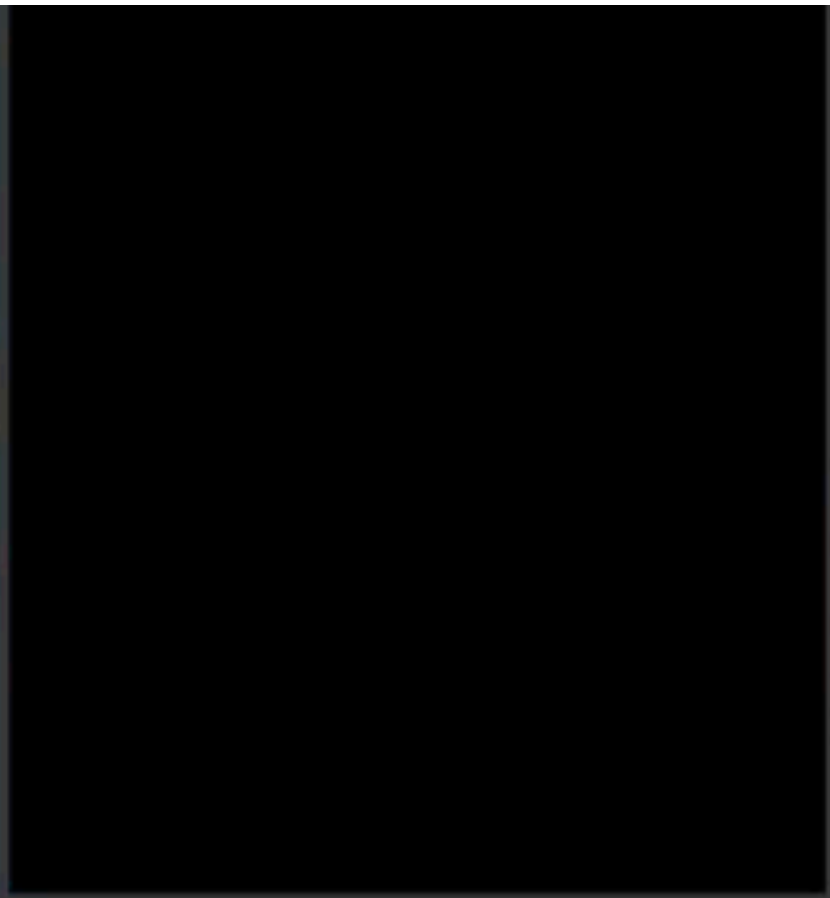
colorful

Add Random Palette Color





**Layer creation from an automatic palette**



Choose File No file chosen

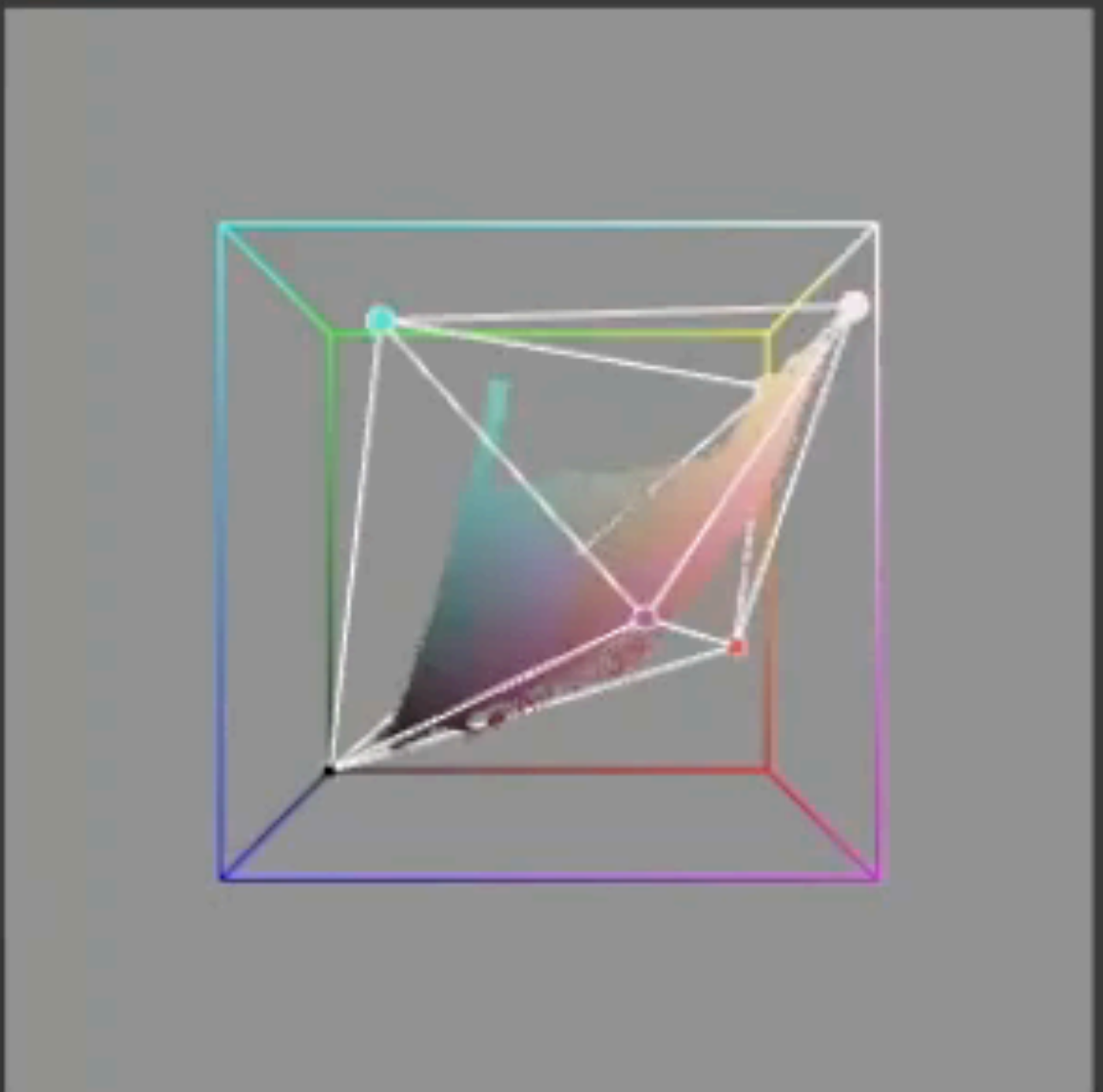
Precompute ROEXY weights

Create automatic palette

Prescribed number of layers: 6

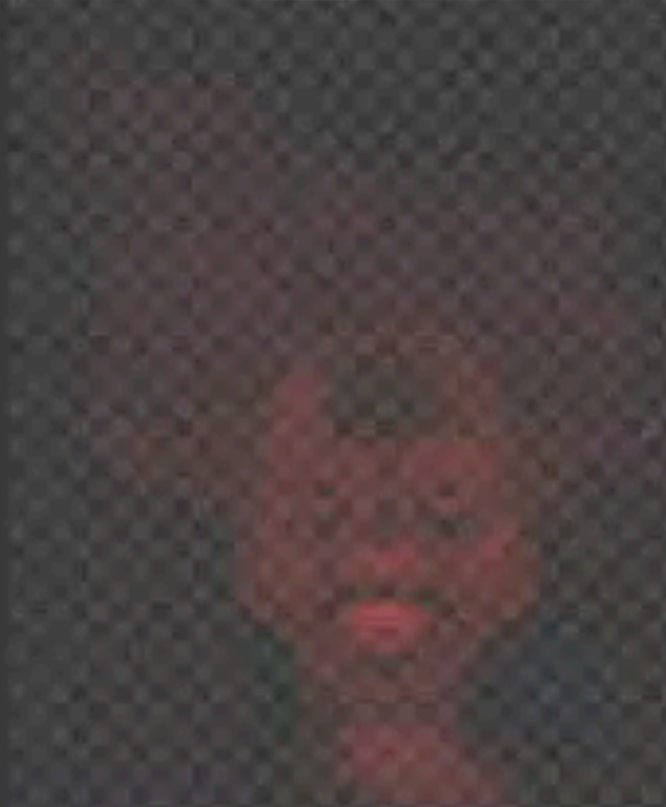
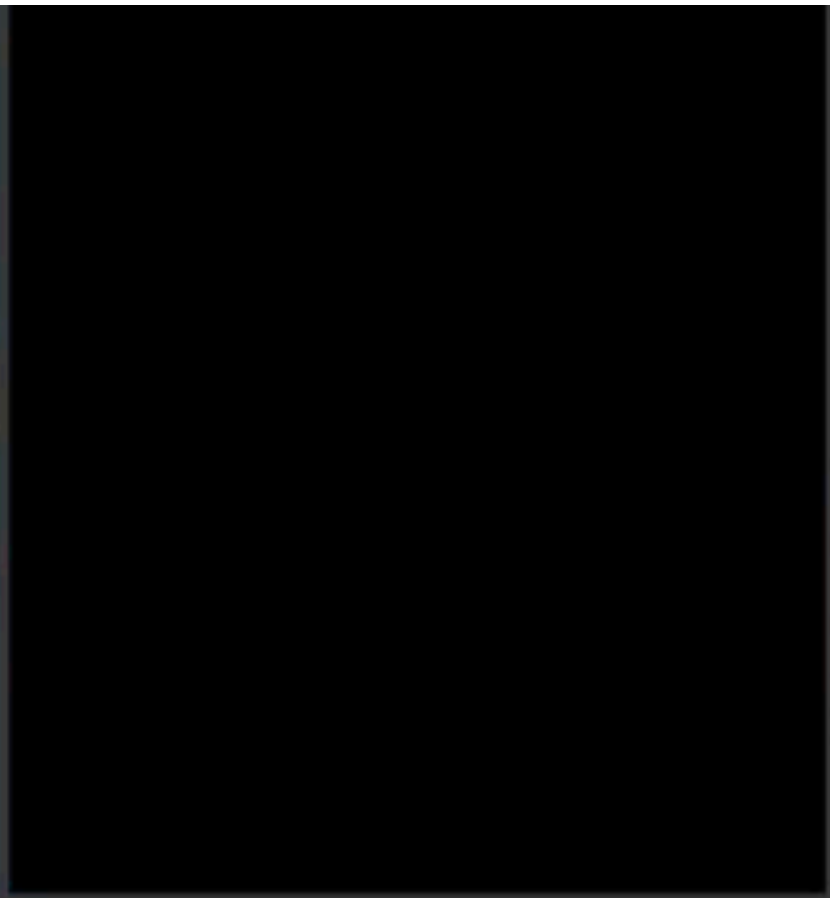
Add Random Palette Color

colorful



Rotation has inertia:





Choose File No file chosen

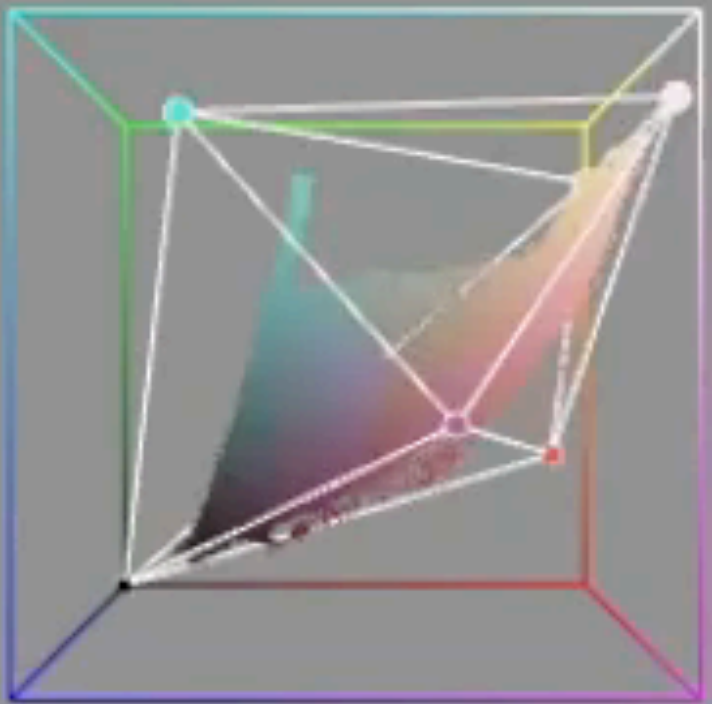
Precompute ROEXY weights

Create automatic palette

Prescribed number of layers: 6

Add Random Palette Color

colorful



Rotation has inertia:



# Interactive decomposition gives more control to the users

original



recoloring with  
interactively edited palette



recoloring with  
automatic palette





# Interactive decomposition gives more control to the users

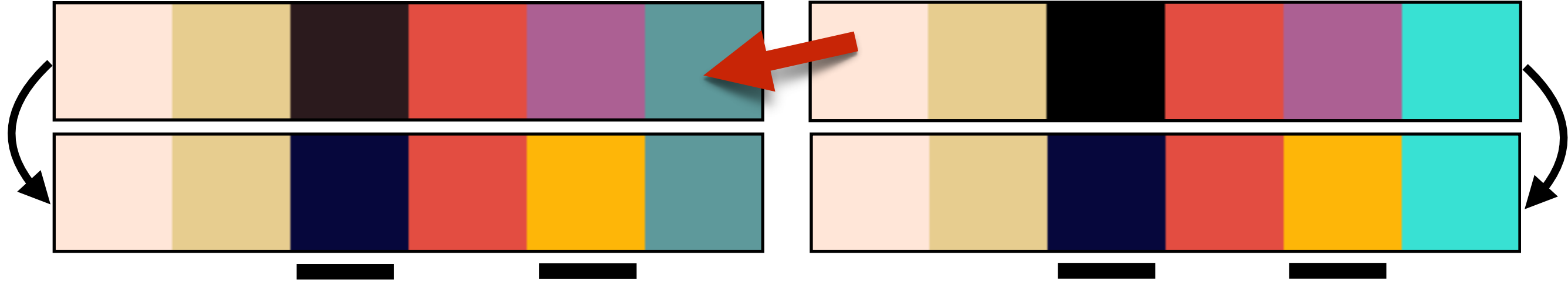
original



recoloring with interactively edited palette



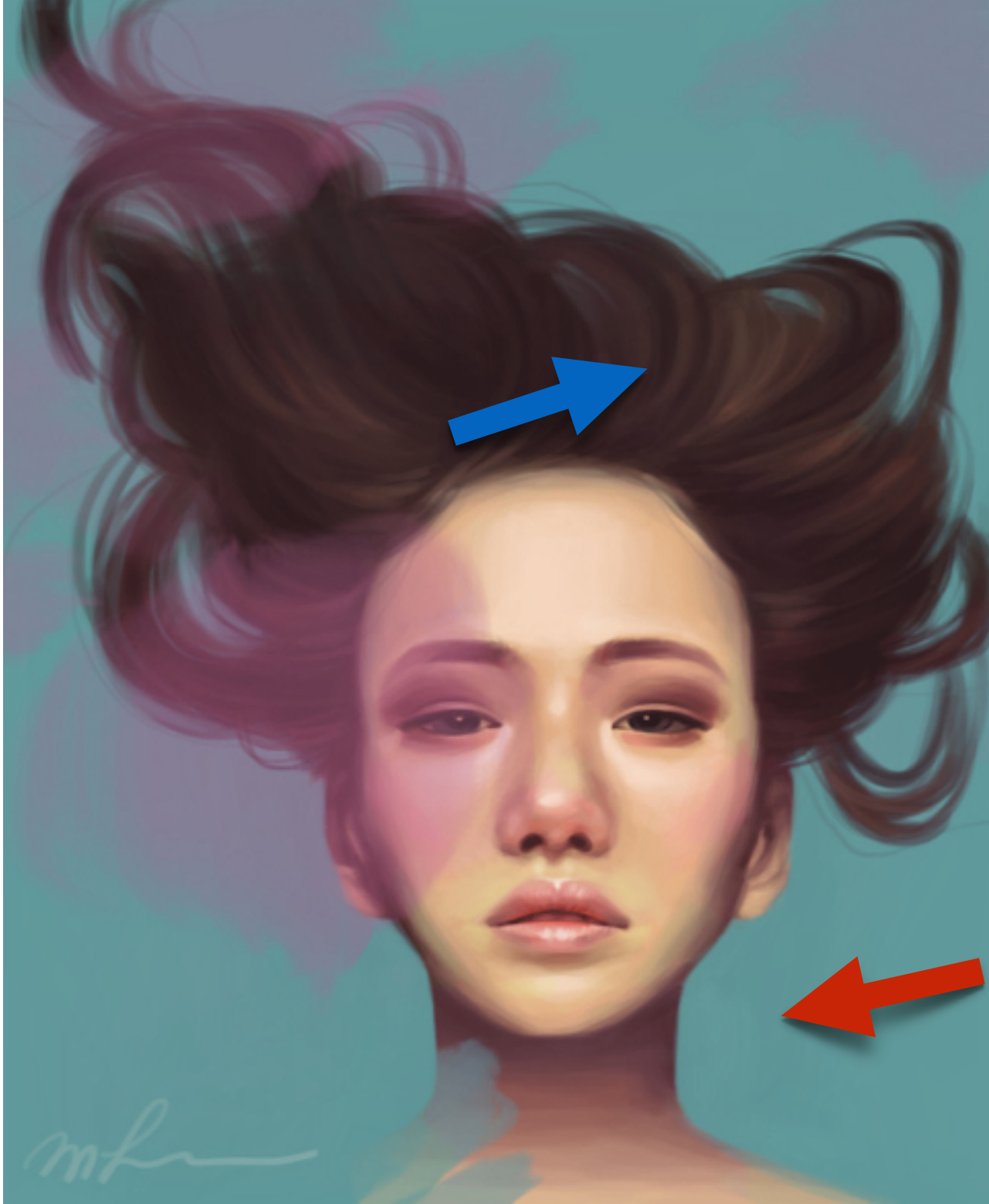
recoloring with automatic palette





# Interactive decomposition gives more control to the users

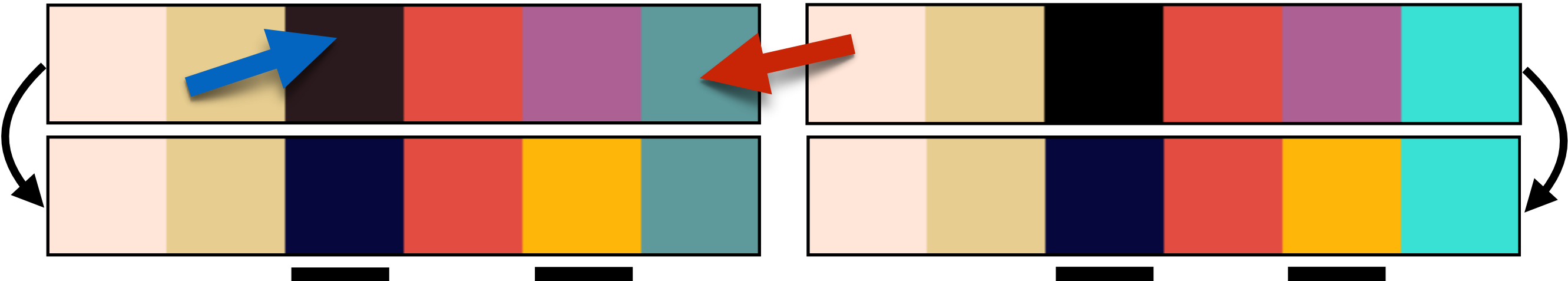
original



recoloring with interactively edited palette



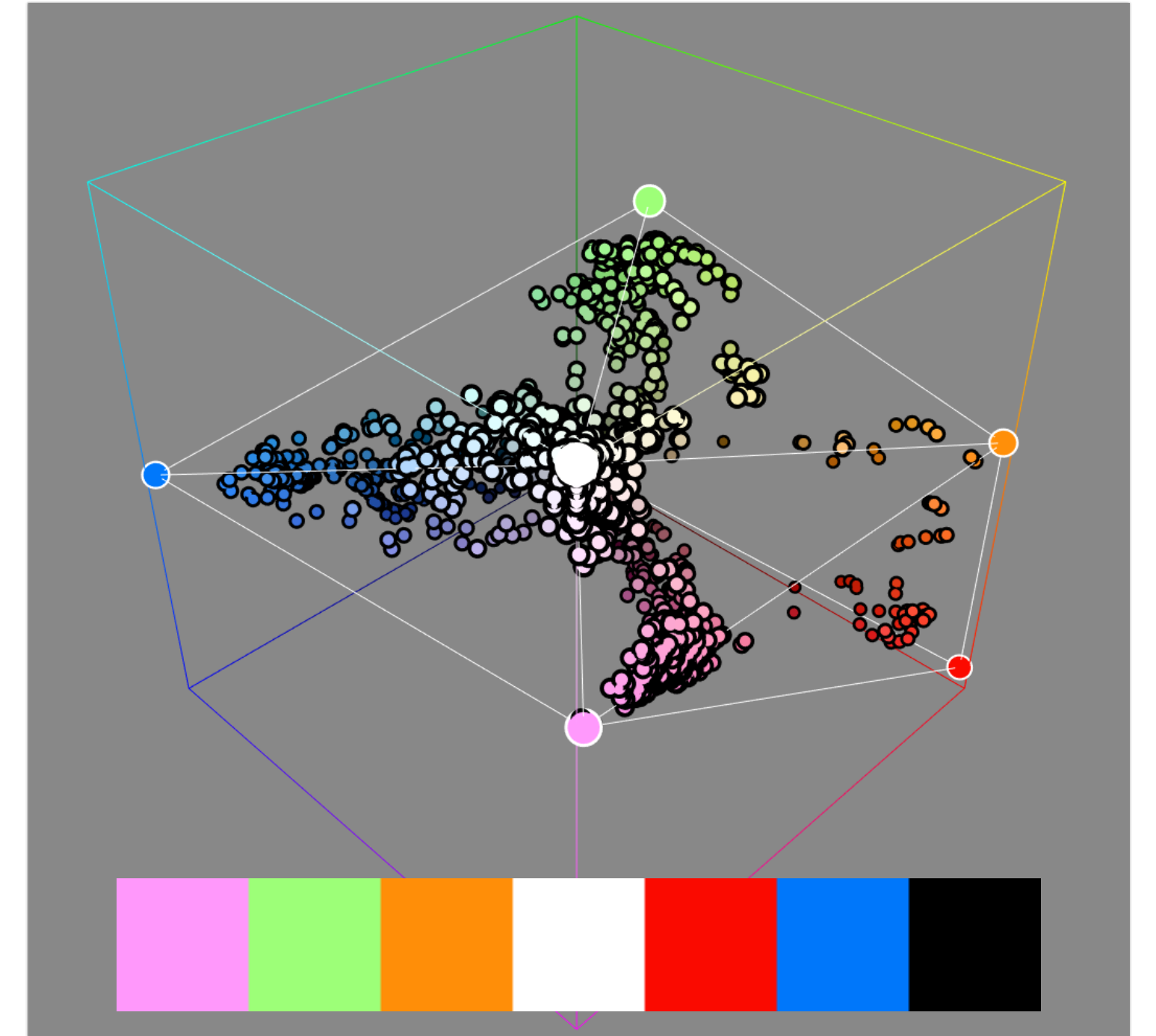
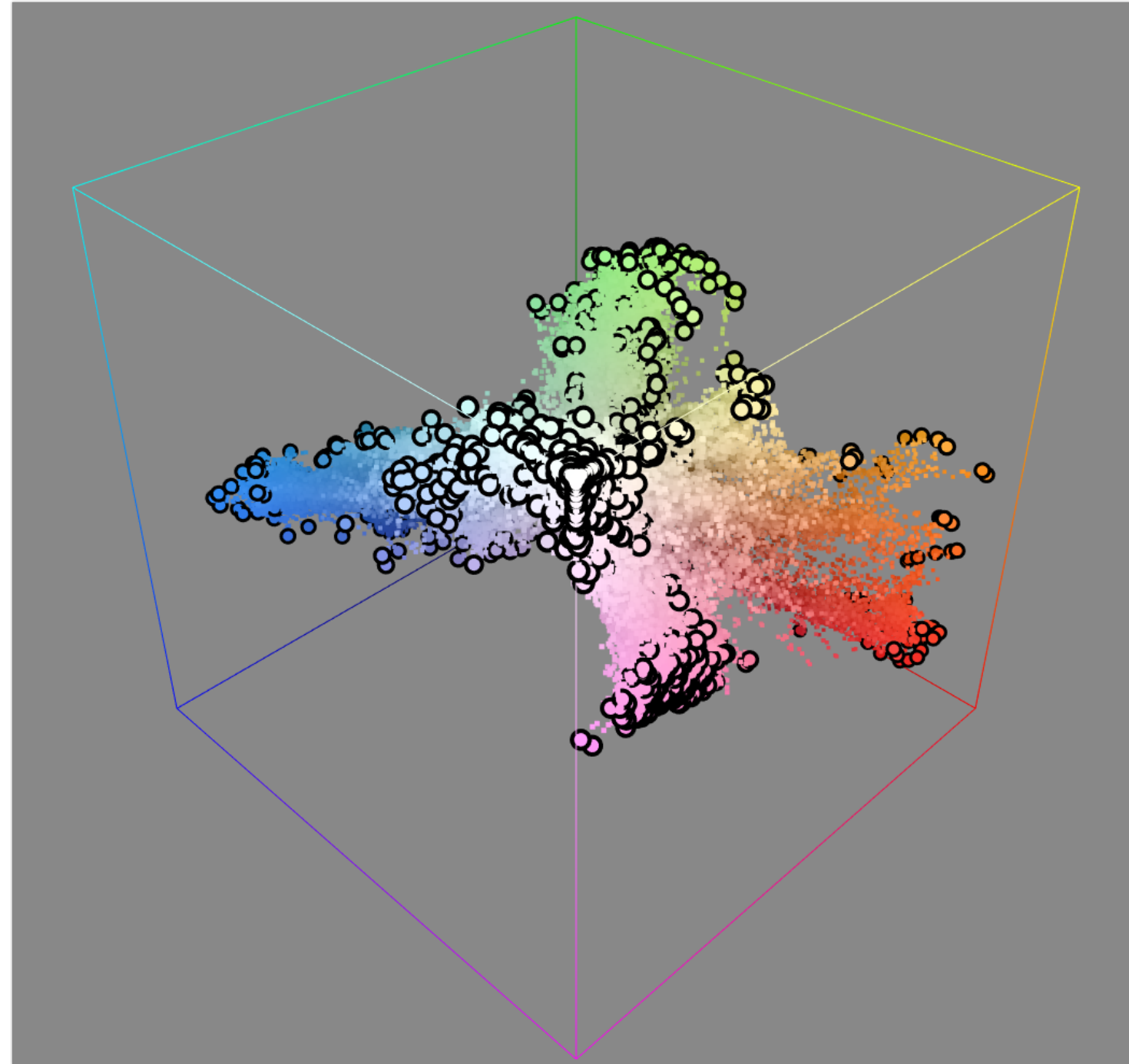
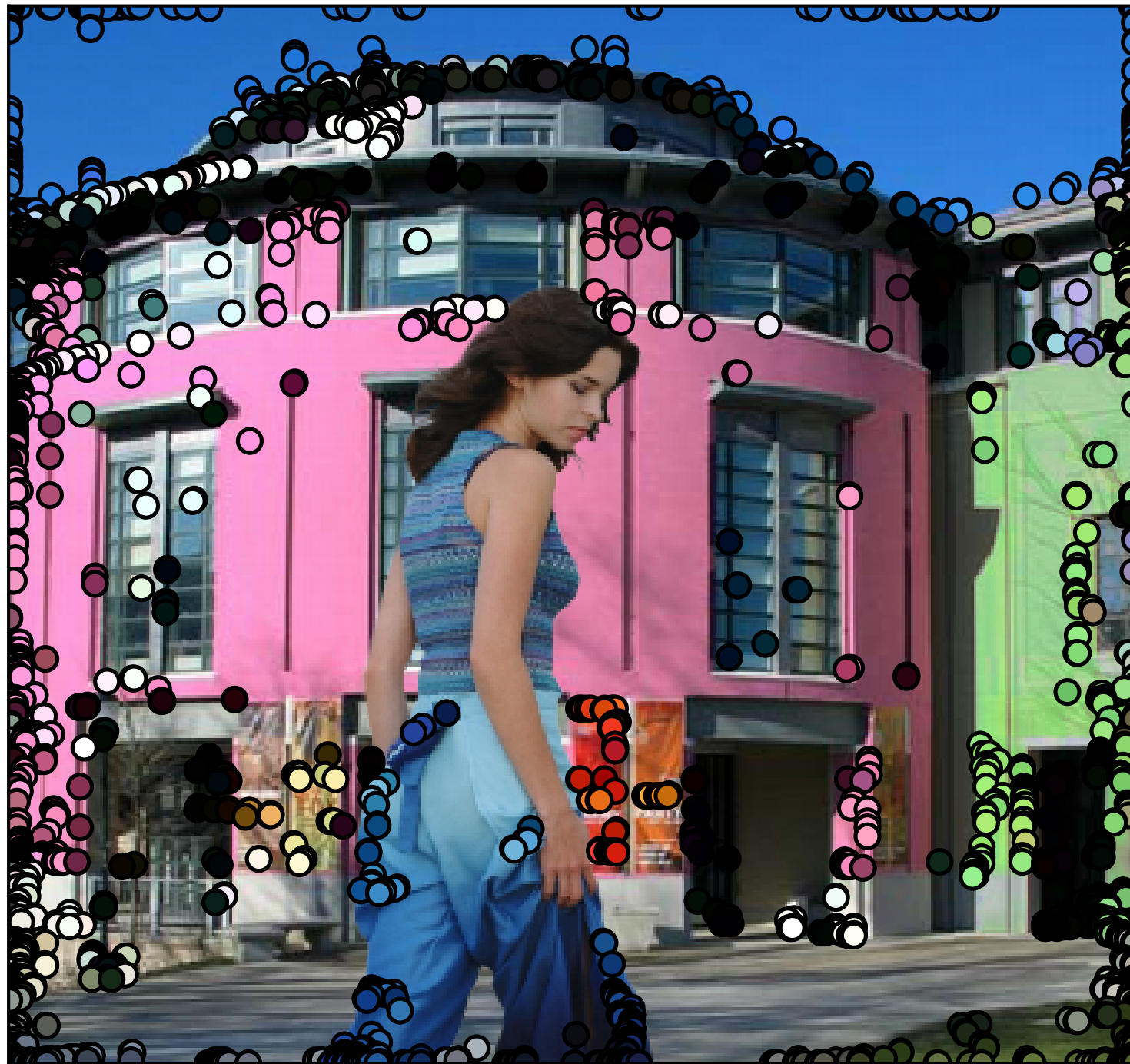
recoloring with automatic palette





# Conclusion

- An extremely efficient approach to layer decomposition via RGBXY geometry



# Conclusion

- Our two-level decomposition supports real-time decomposition when palette editing.

**Palette updates**

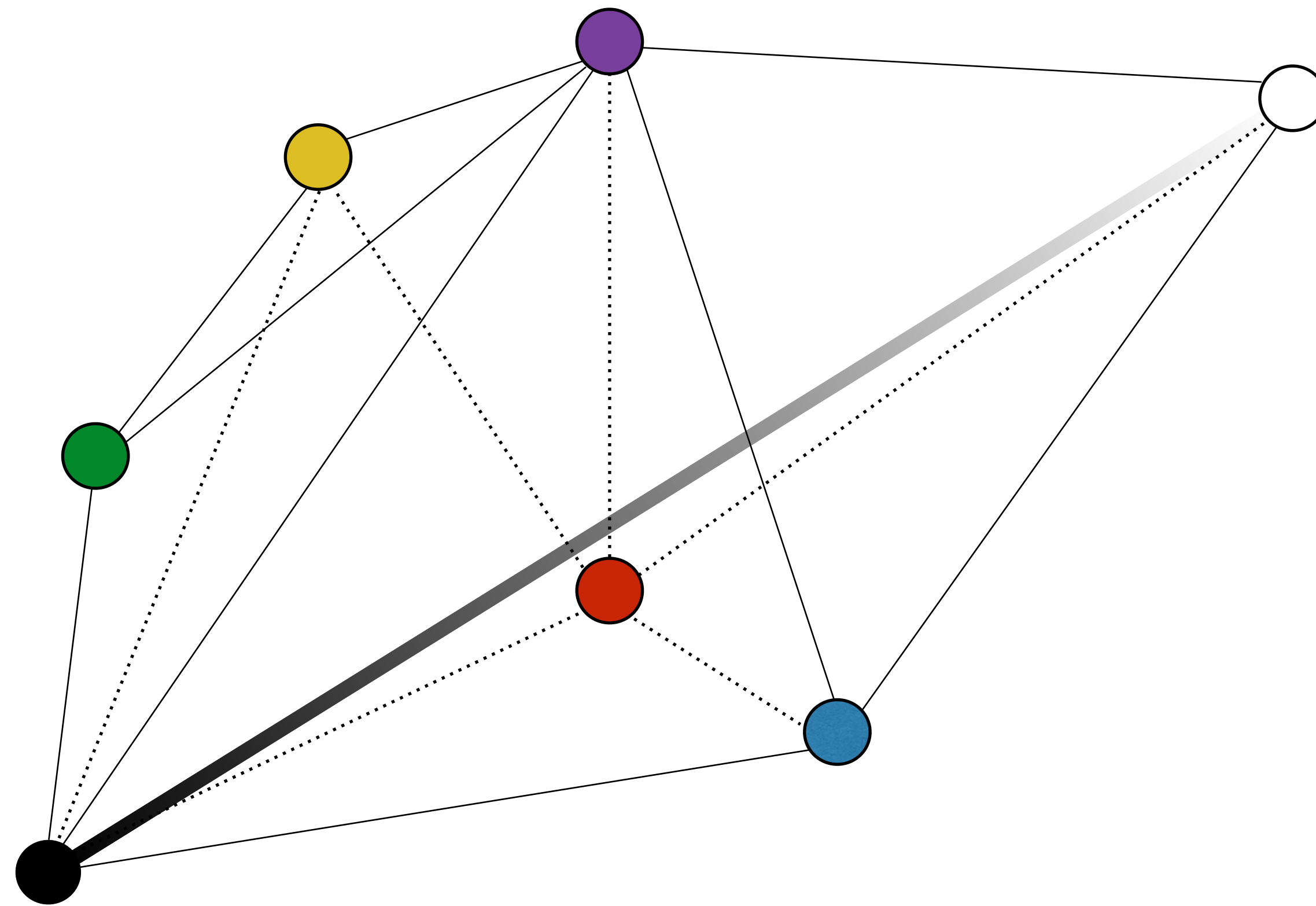
**Fixed**

$$W = W_{\text{RGB}} * W_{\text{RGBXY}}$$



# Conclusion

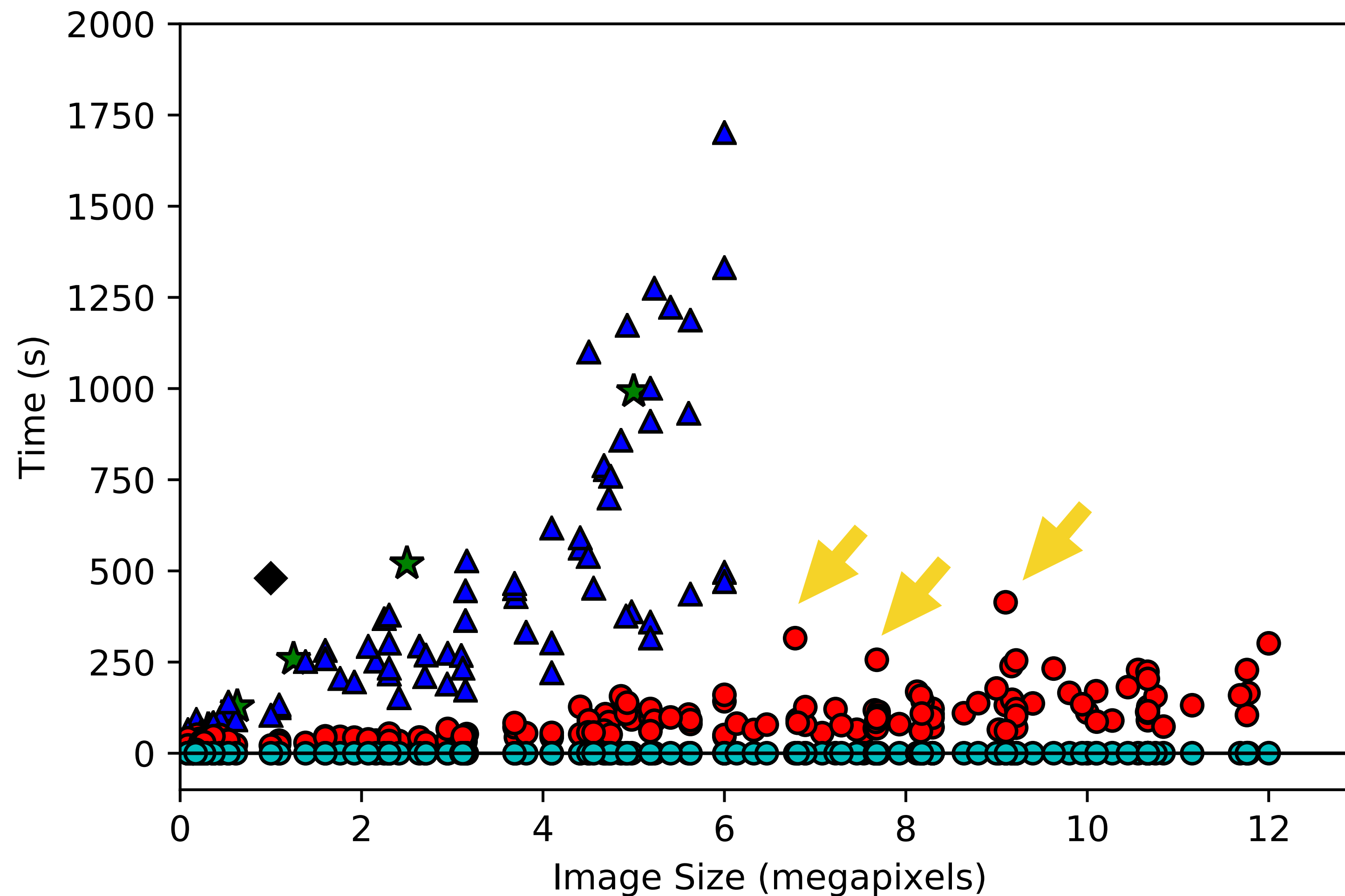
- It's important to capture the "line of greys".



**Star tessellation**

# Limitations

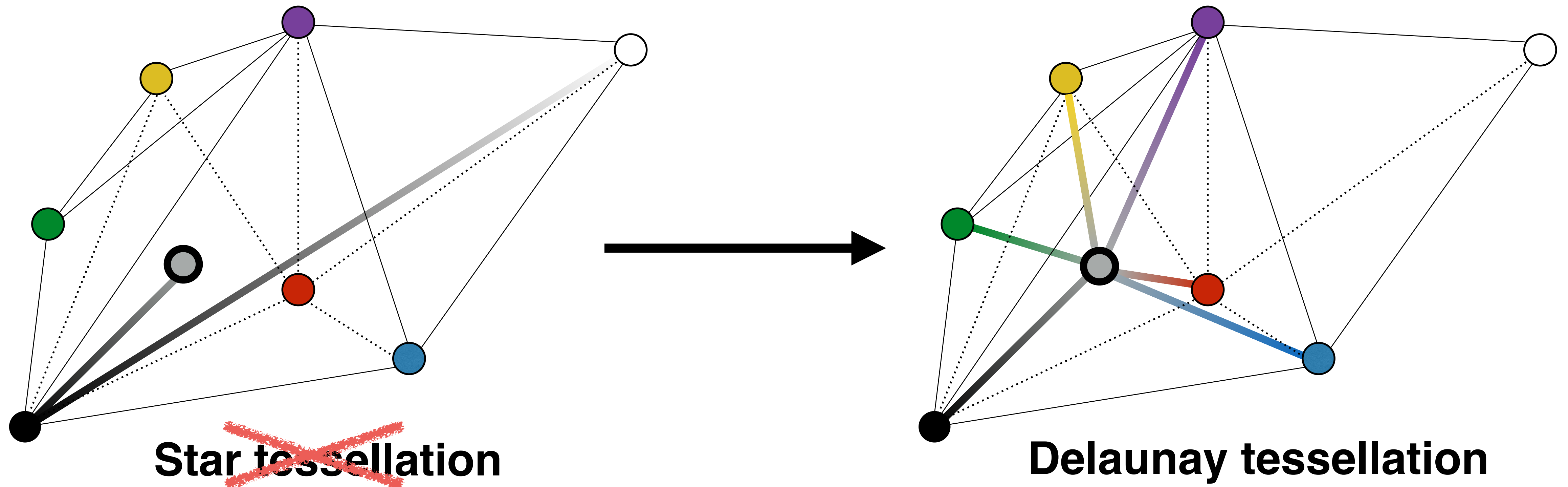
- In isolated cases, the 5D convex hull takes somewhat longer than usual to compute.





# Limitations

- Our star tessellation assumes that palette colors are vertices of a convex polyhedron.
  - For palette colors in the interior, must use inferior Delaunay tessellation.

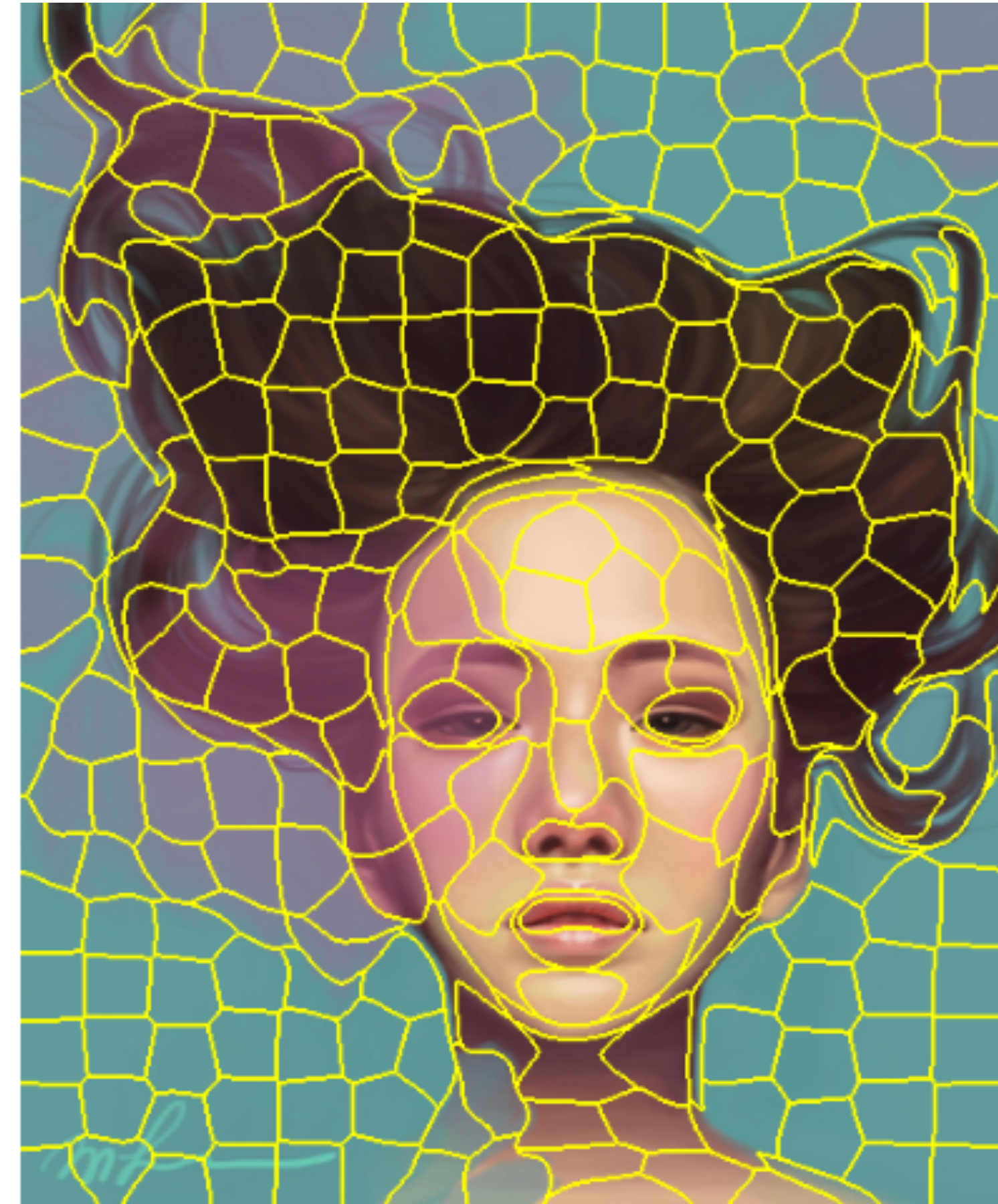


# Future Work

- More speed via super-pixels or parallel convex hull algorithms.



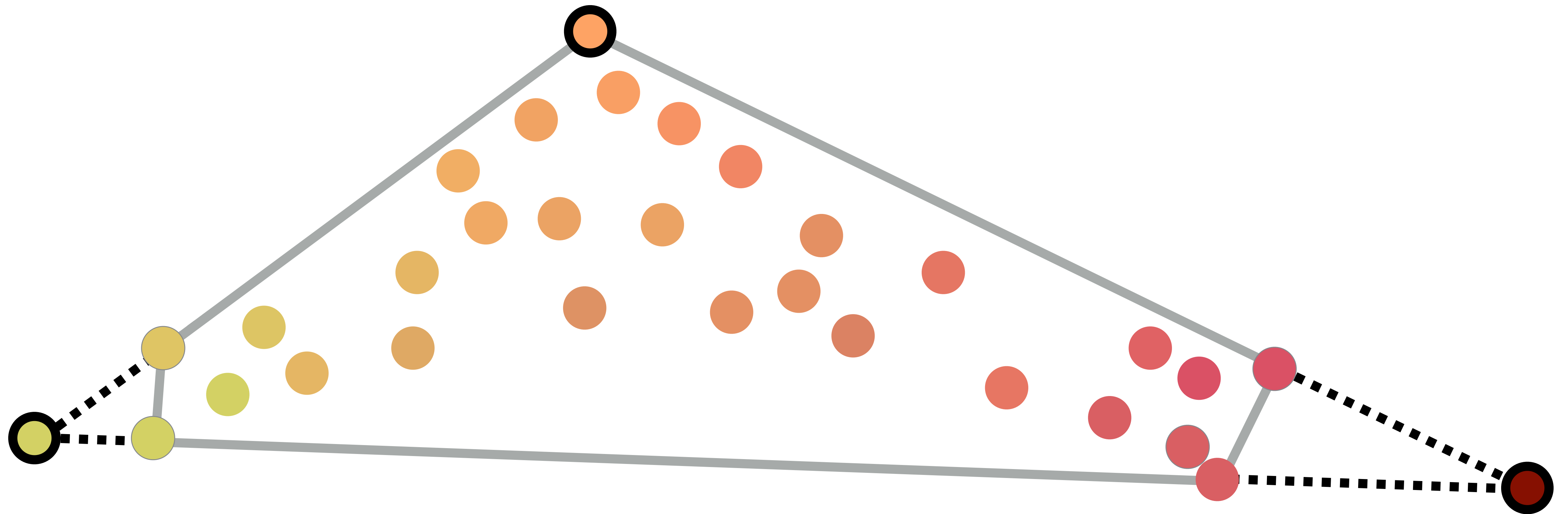
+





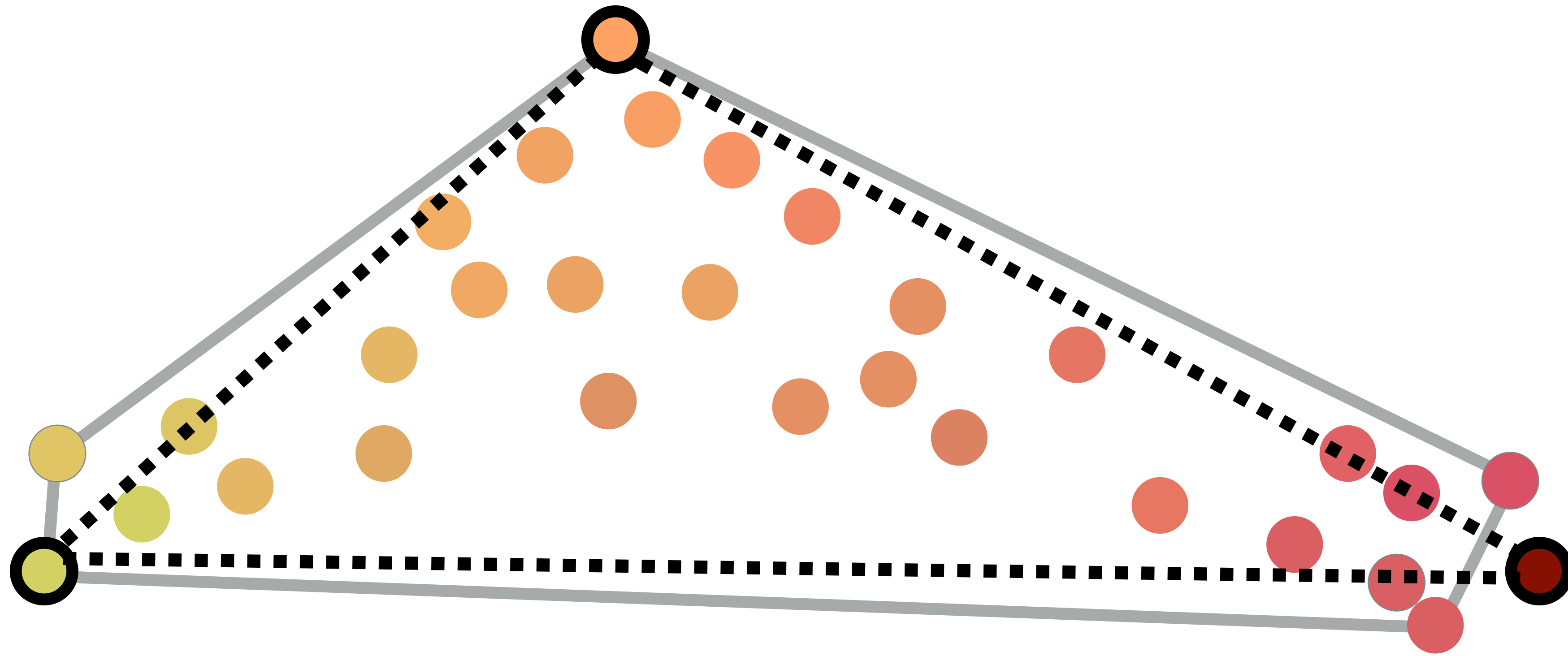
# Future Work

- Robustness via approximate convex hull algorithms.



# Future Work

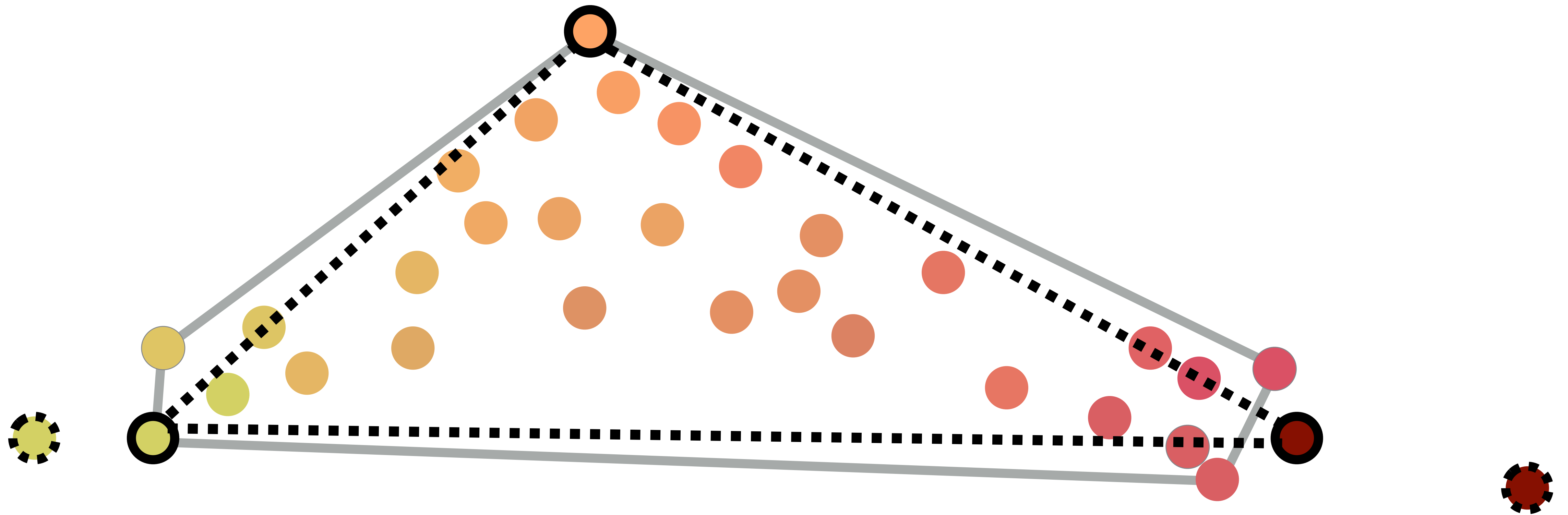
- Robustness via approximate convex hull algorithms.





# Future Work

- Robustness via approximate convex hull algorithms.



# Thank You!

- Contact Information:
  - Jianchao Tan: [jtan8@gmu.edu](mailto:jtan8@gmu.edu)
  - Jose Echevarria: [echevarr@adobe.com](mailto:echevarr@adobe.com)
  - Yotam Gingold: [ygingold@gmu.edu](mailto:ygingold@gmu.edu)
- Project Website (GUI, code, data): <https://cragl.cs.gmu.edu/fastlayers/>
- Artists: Adelle Chudleigh; Dani Jones; Karl Northfell; Michelle Lee; Adam Saltsman; Yotam Gingold; DeviantArt user Sylar113; Fabio Bozzone; Piper Thibodeau; Spencer Nugent; George Dolgikh; DeviantArt user Ranivius.
- Sponsors:
  - NSF, Adobe, Google.



**Extra slides**

# Possible questions

- Star triangulation starting from black palette color, what if no black color in extracted palette?
- Does your method require palette to cover all pixel colors when editing palette in GUI? What if I want some palette colors that is inside color point cloud?
- In your performance figure, there are one or two cases that are slower than many others. Can you describe the worst case performance of your method?
- Do you have failure case?
- How do you measure the quality of your layer results and your interactive editing GUI?